

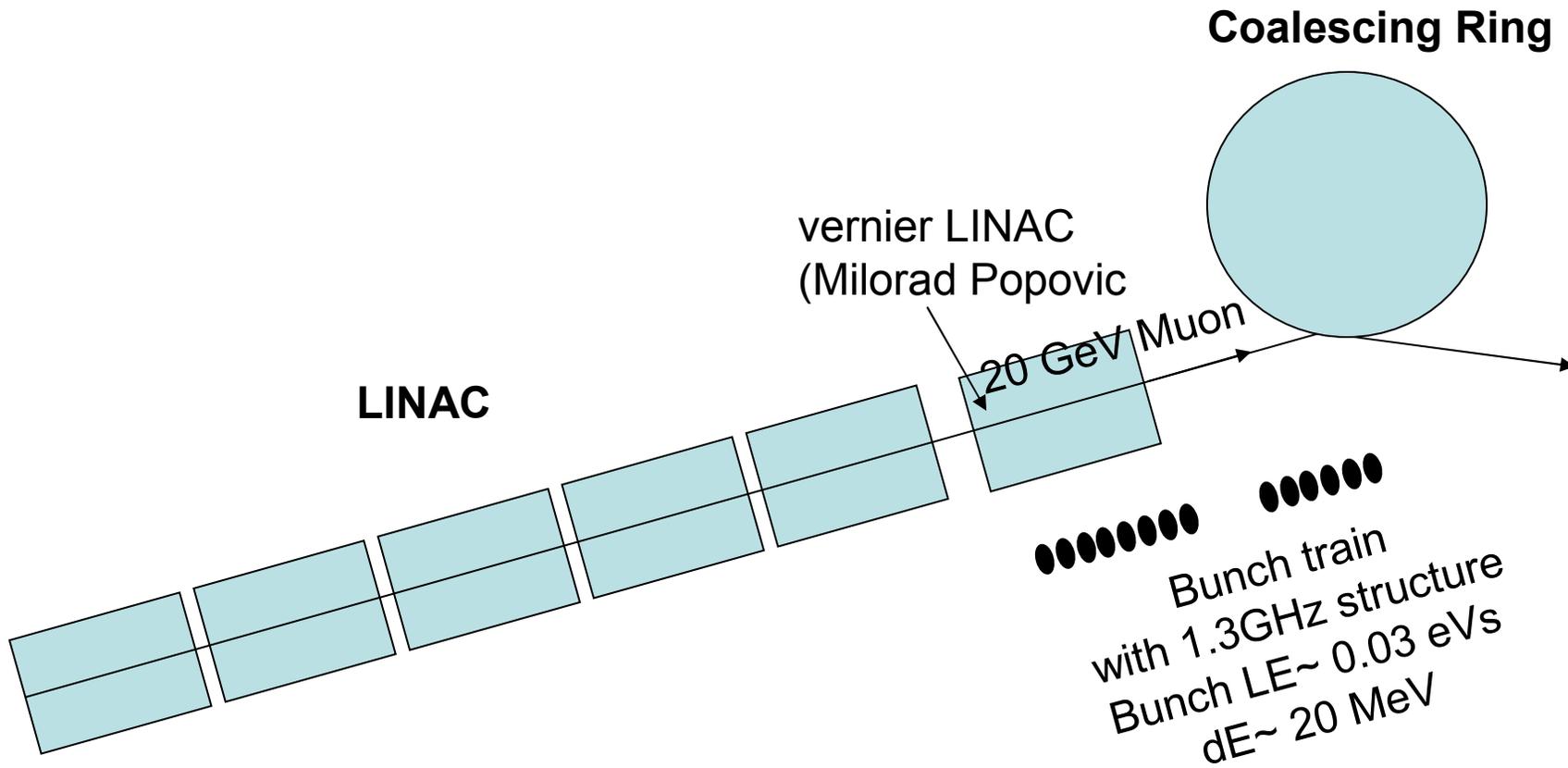
A 20 GeV Coalescing Ring for a Muon Collider

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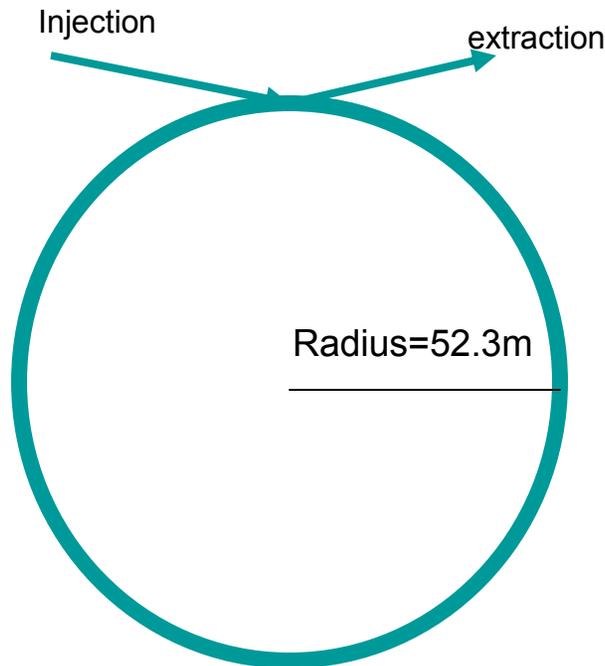
Low Emittance Muon Workshop
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Schematic of the LINAC+Coalescing Ring



Muon Coalescing Ring.

Based on the information given to me by Chuck Ankenbrandt following parameters are derived for the Coalescing Ring



Constraints:

Muon mean-life = 2.2 μ s (rest frame)

**Muon half-life in lab = 288 μ s
for 20 GeV beam**

Time (90% survival) = 43.8 μ s

Injection beam : 1.3GHz bunch structure

of bunches/train = 17

Ring Radius = 52.33m; Revolution period= 1.09 μ s

Energy of the muon = 20 GeV (gamma = 189.4)

gamma_t of the ring = 4

If we assume

Ring-Radius/rho (i.e., fill factor) = 2, then B-Field = 2.54T
(This field seems to be reasonable)

h for the coalescing cavity = 42, 84

Number of trains/injection = less than 37

(assuming ~100ns for injection/extraction)

RF voltage for the coalescing cavity = 1.9 MV (h=42)

= 0.38 MV (h=84)

f_{sy} ~ 5.75E3Hz

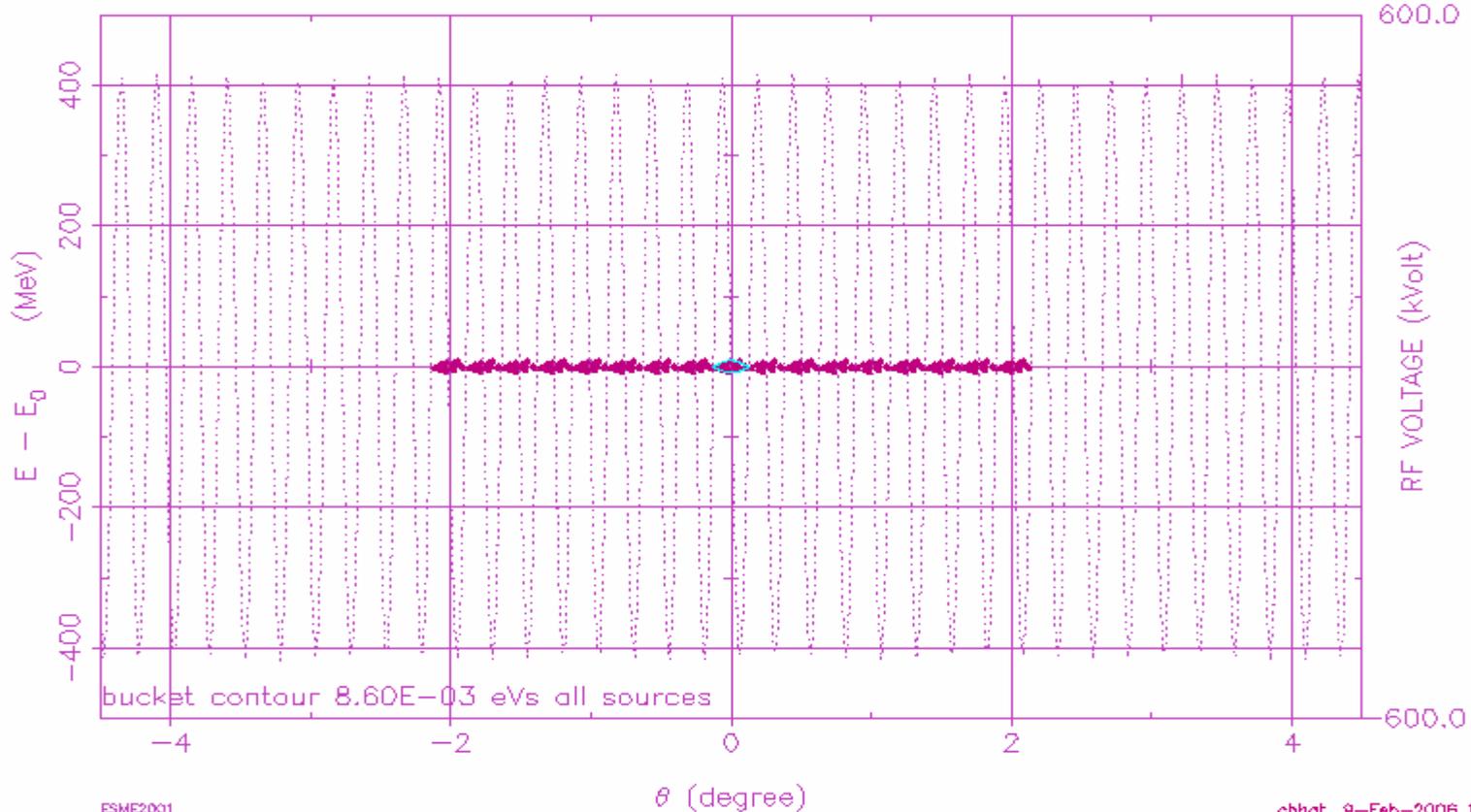
T_{sy}/4 = 43.5 μ s

Number of turns in the ring ~40

1st Scenario

Muon Bunch train from the LINAC

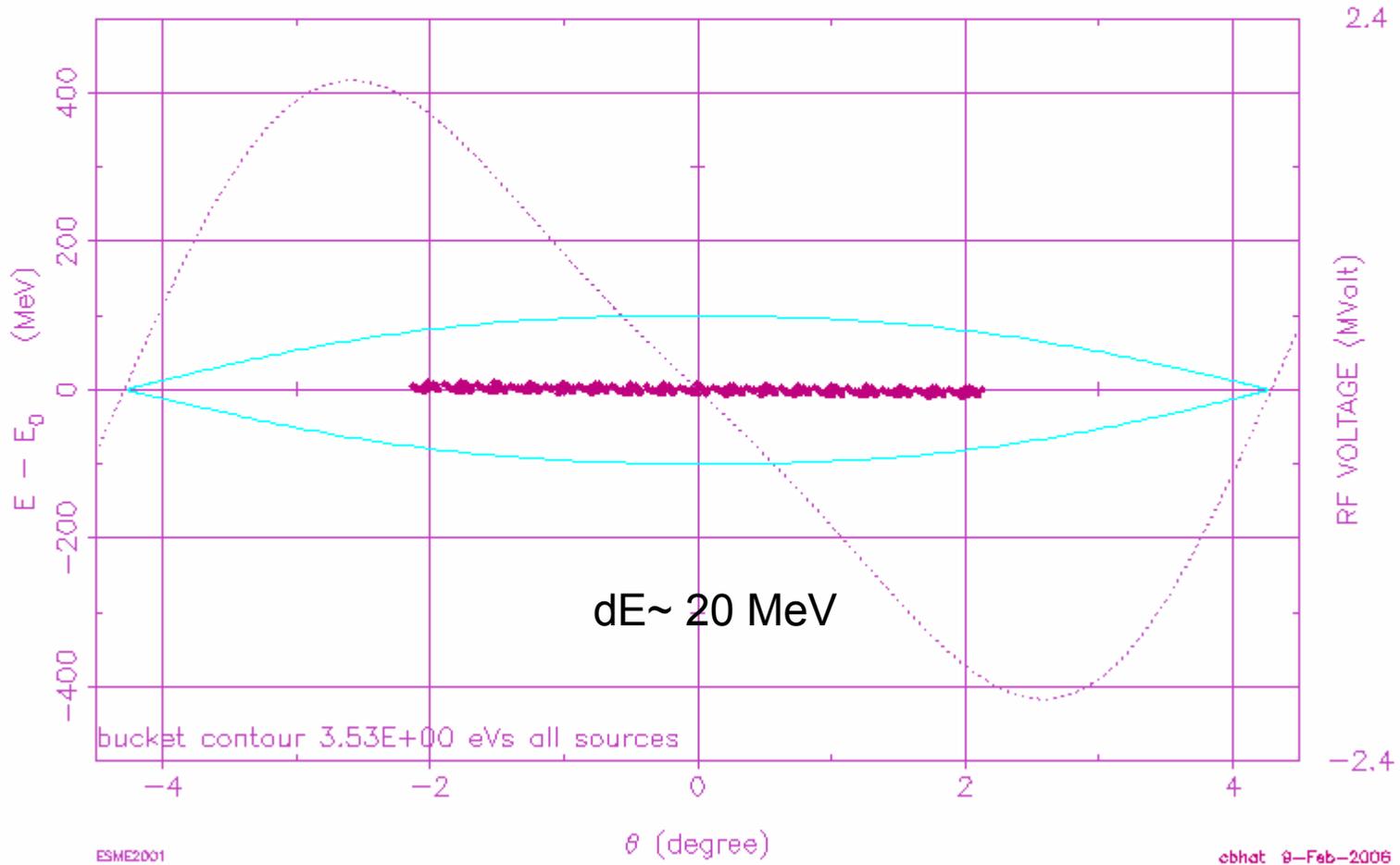
H_B (MeV)	S_B (eV s)	E_S (MeV)	h	V (MV)	ψ (deg)
8.7883E+00	8.5959E-03	2.1021E+04	1428	5.000E-01	1.800E+02
ν_S (turn ⁻¹)	pdot (MeV s ⁻¹)	η			
1.8104E-02	0.0000E+00	6.0508E-02			
τ (s)	S_b (eV s)	N			
1.0978E-06	4.3727E-02	340			



Muon Bunch train in the coalescing bucket

T=0 sec

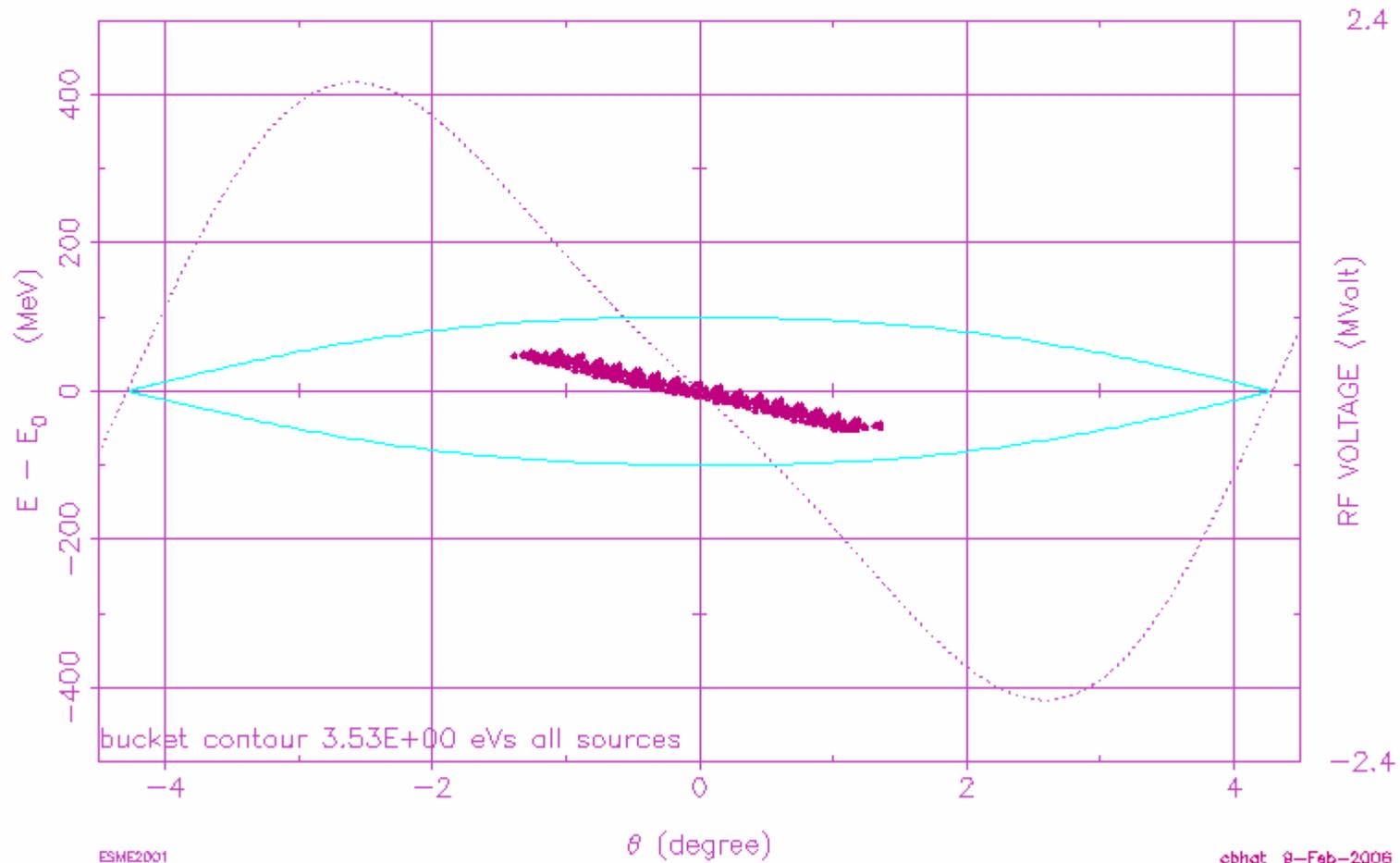
H_B (MeV)	ω_B (eV s)	E_S (MeV)	n	v (MeV)	ψ (deg)
9.9923E+01	3.5345E+00	2.1021E+04	42	1.900E+00	1.800E+02
ν_S (turn ⁻¹)	pdot (MeV s ⁻¹)	η	84	3.800E-01	0.000E+00
6.0523E-03	2.1216E-10	6.0508E-02			
τ (s)	S_b (eV s)	N			
1.0978E-06	3.8696E-02	340			



Muon Bunch train in the coalescing bucket

$T = 31.6 \mu\text{sec}$

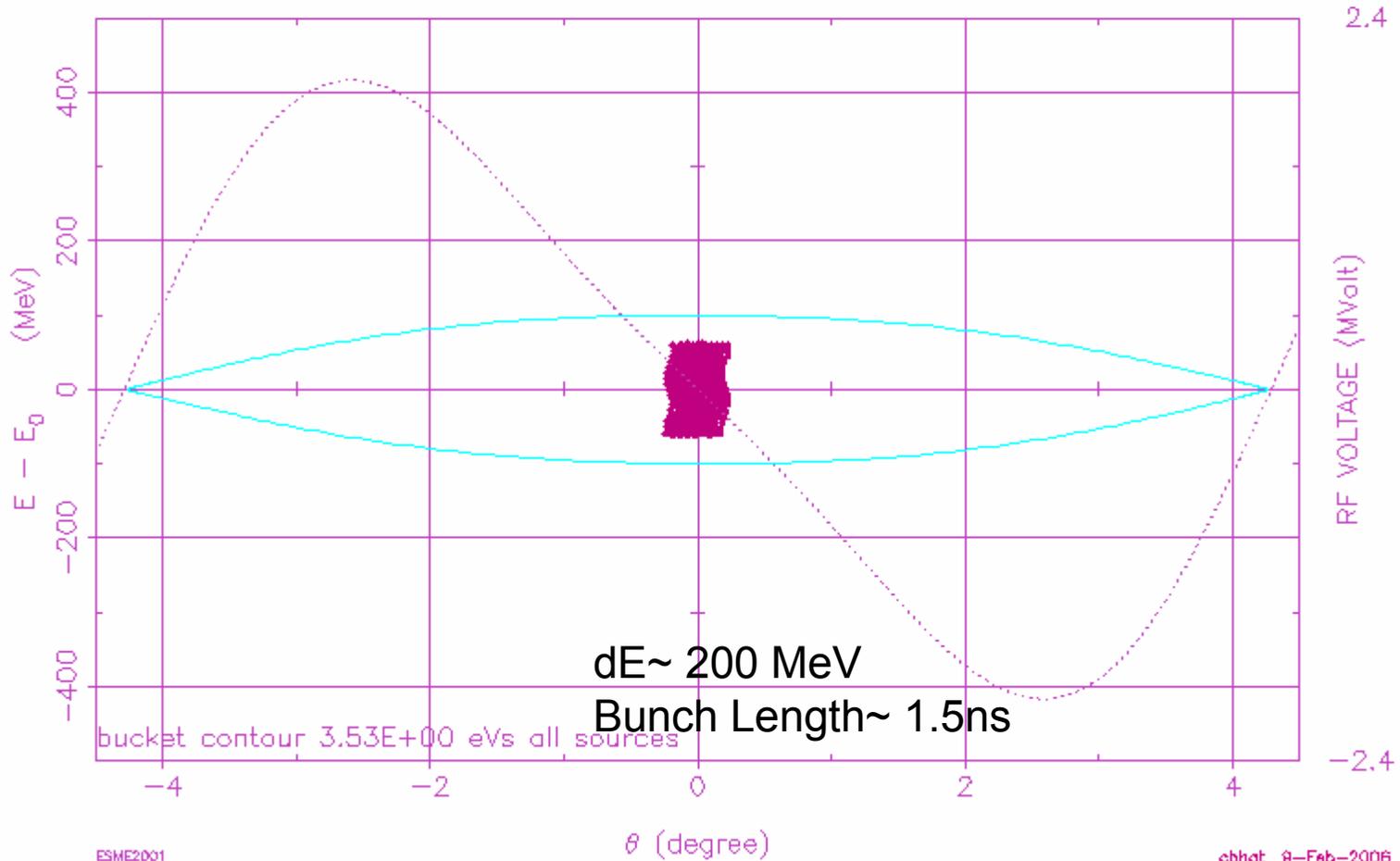
H_B (MeV)	S_B (eV s)	E_S (MeV)	h	V (MV)	ψ (deg)
9.9923E+01	3.5345E+00	2.1021E+04	42	1.900E+00	1.800E+02
ν_S (turn $^{-1}$)	pdot (MeV s $^{-1}$)	η	84	3.800E-01	0.000E+00
6.0523E-03	2.1216E-10	6.0508E-02			
τ (s)	S_b (eV s)	N			
1.0978E-06	3.8969E-02	340			



Muon Bunch train in the coalescing bucket

$T = 54 \mu\text{sec}$

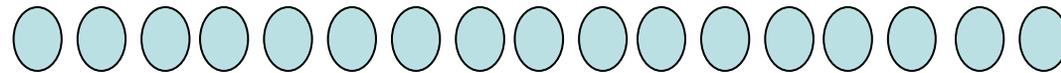
H_b (MeV)					
9.9923E+01					
ν_s (turn ⁻¹)	pdot (MeV s ⁻¹)	η	84	3.800E-01	0.000E+00
6.0523E-03	2.1216E-10	6.0508E-02			
τ (s)	S_b (eV s)	N			
1.0978E-06	3.8917E-02	340			



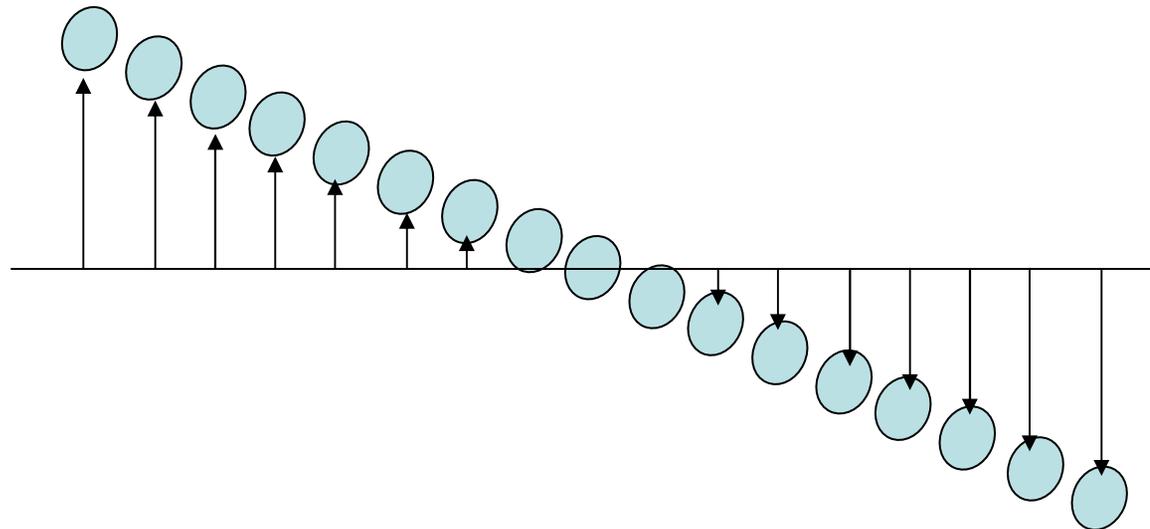
2nd Scenario

- A vernier-linac to give a tilt in the Longitudinal Phase-space

Bunch train before
the special
purpose pre-linac

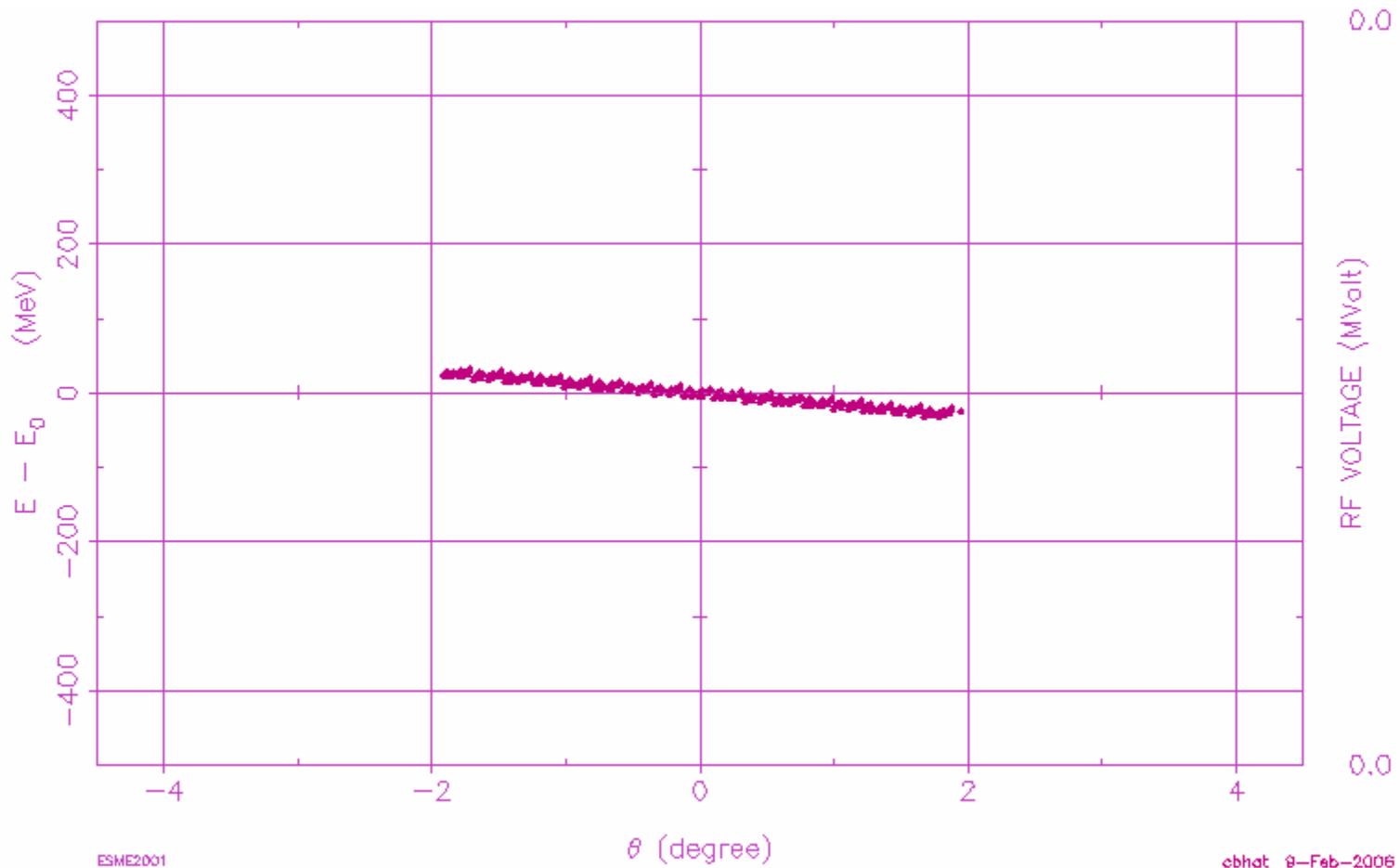


Muon Bunches
after pre-linac



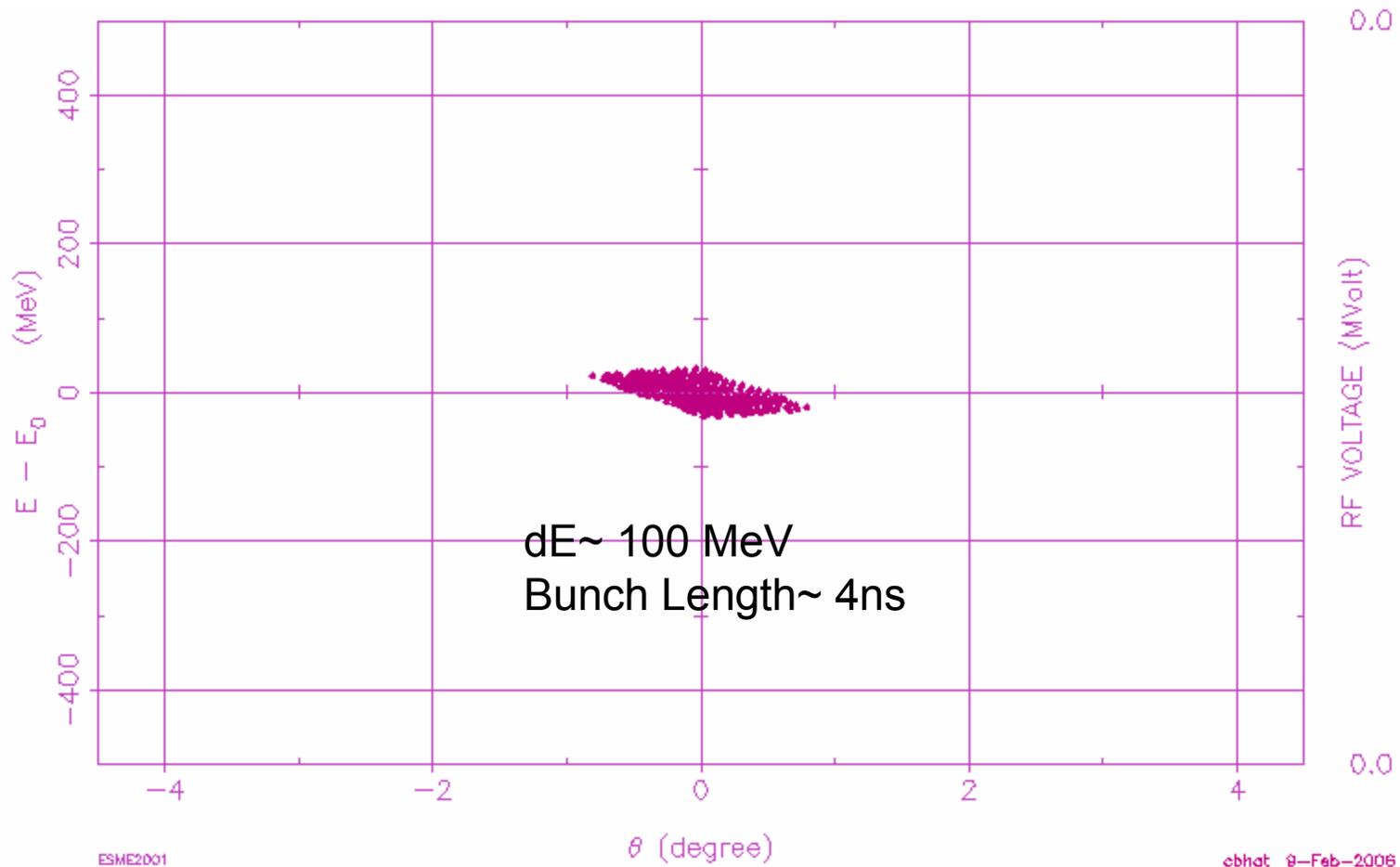
- And next inject the beam into the **Coalescing Ring**

Muon Bunch train in the Coalescing Ring T=0 sec



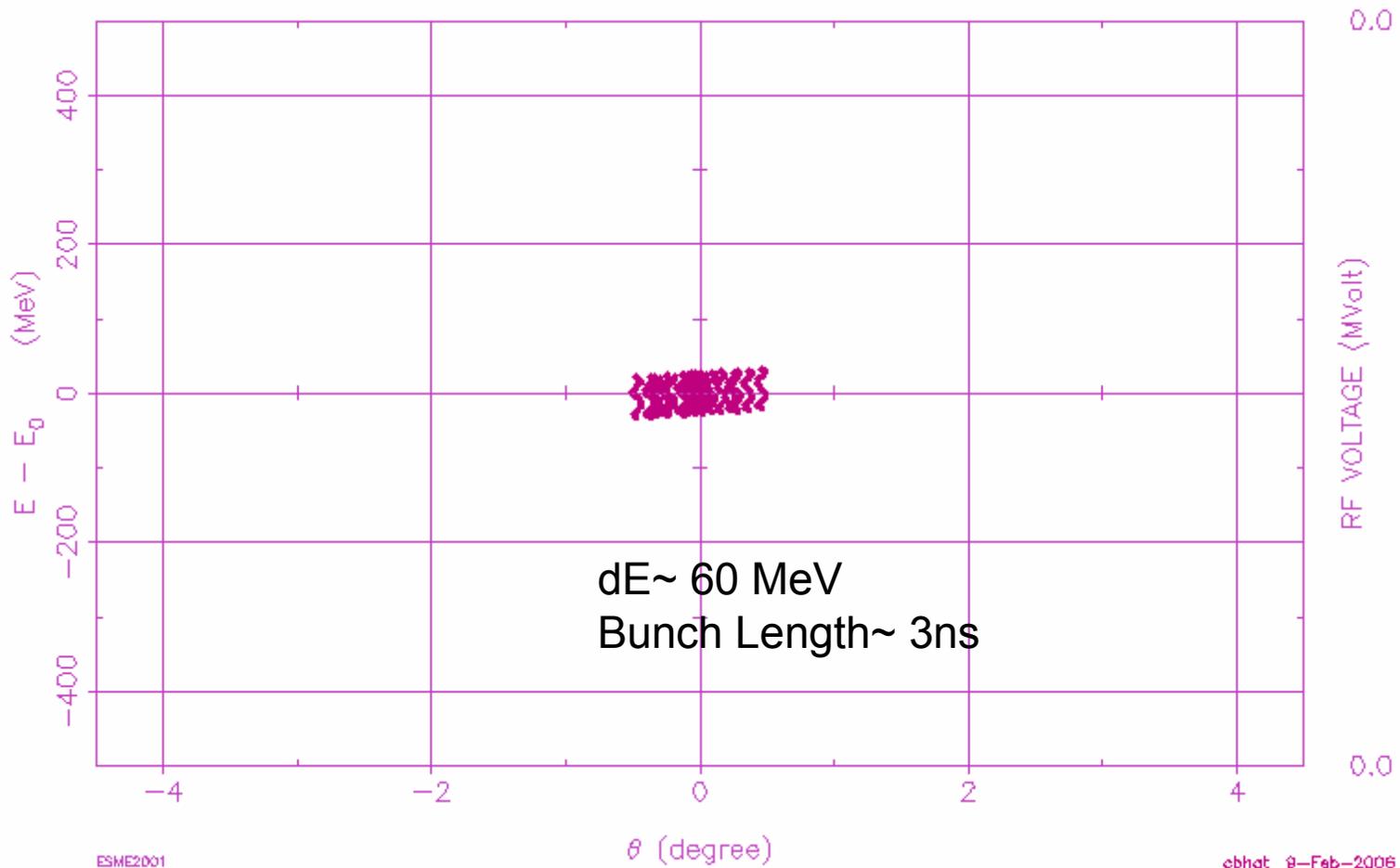
Muon Bunch train in the Coalescing Ring

$T=46 \mu\text{sec}$



Muon Bunch train in the Coalescing Ring

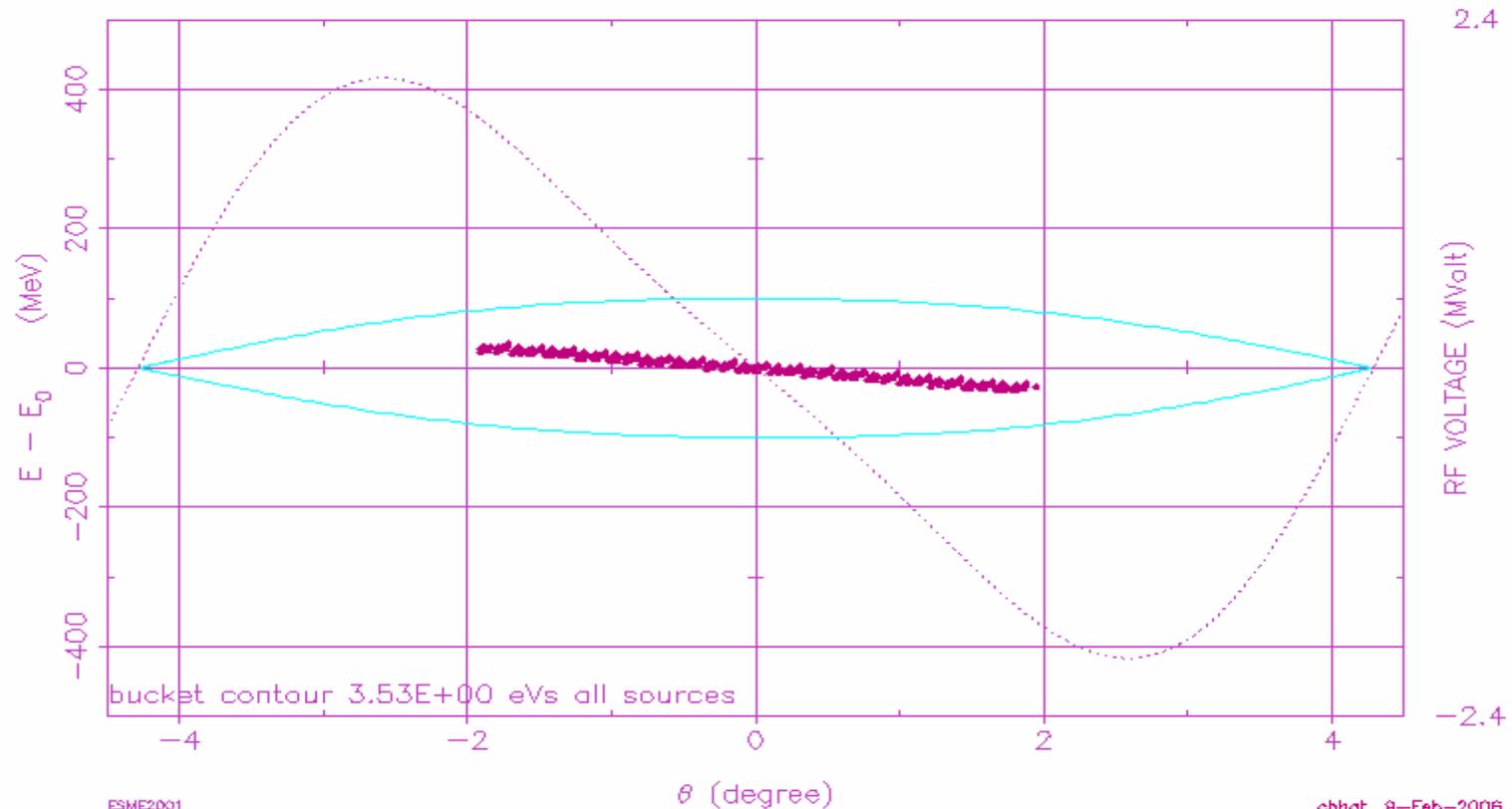
$T=71 \mu\text{sec}$



3rd Scenario

Muon Bunch train in the Coalescing Ring T=0 sec

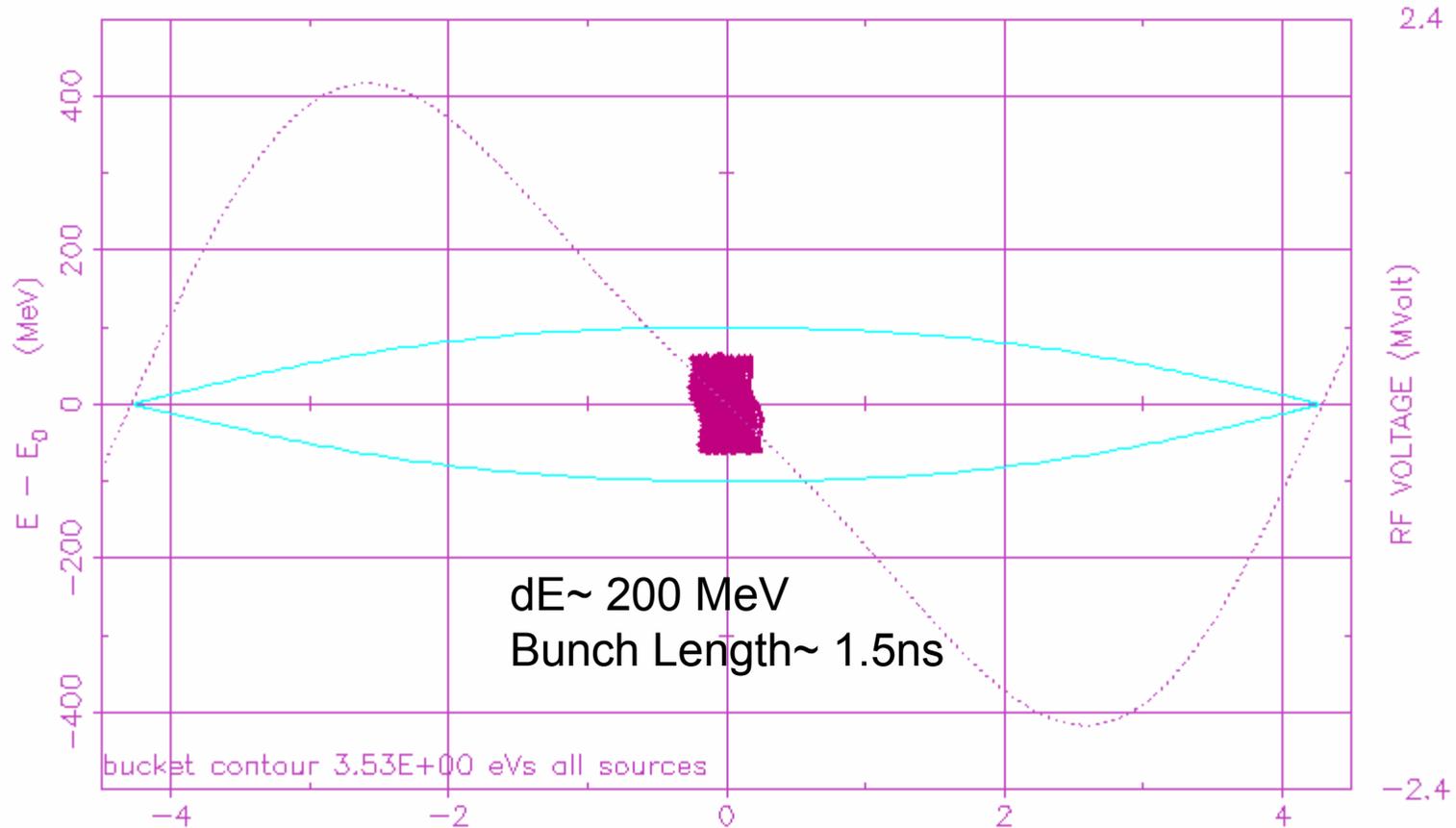
H_B (MeV)	S_B (eV s)	E_S (MeV)	h	V (MV)	ψ (deg)
9.9923E+01	3.5345E+00	2.1021E+04	42	1.900E+00	1.800E+02
ν_S (turn ⁻¹)	pdot (MeV s ⁻¹)	η	84	3.800E-01	0.000E+00
6.0523E-03	2.1216E-10	6.0508E-02			
τ (s)	S_b (eV s)	N			
1.0978E-06	3.8889E-02	340			



Muon Bunch train in the Coalescing Ring

T=38 μ sec

H_b (MeV)	$3.5345E+00$	$2.1021E+04$	42	$1.900E+00$	$1.800E+02$
ν_s (turn $^{-1}$)	\dot{p} (MeV s $^{-1}$)	η	84	$3.800E-01$	$0.000E+00$
$6.0523E-03$	$2.1216E-10$	$6.0508E-02$			
τ (s)	S_b (eV s)	N			
$1.0978E-06$	$3.8917E-02$	340			



Summary

- We have done a preliminary design of a 20 GeV ring for muon collider
- Discussed three scenarios for 20 GeV muon beam rf manipulations for up to 37 groups of 17 bunches of 1.3GHz
 - Scenario1: the muon bunch injection and coalescing (no vernier cavities before injection to the 20 GeV ring) ← takes about 54 μs
 - Scenario2: the muon bunch injection after giving an energy offsets to the leading and trailing bunches and no coalescing rf cavities ← takes about 46-54 μs
 - Scenario3: the muon bunch injection after giving an energy offsets to the leading and trailing bunches and with coalescing rf cavities ← takes about 38 μs