



# PARASITIC RESONANCES IN HIGH POWER PROTON LINACS

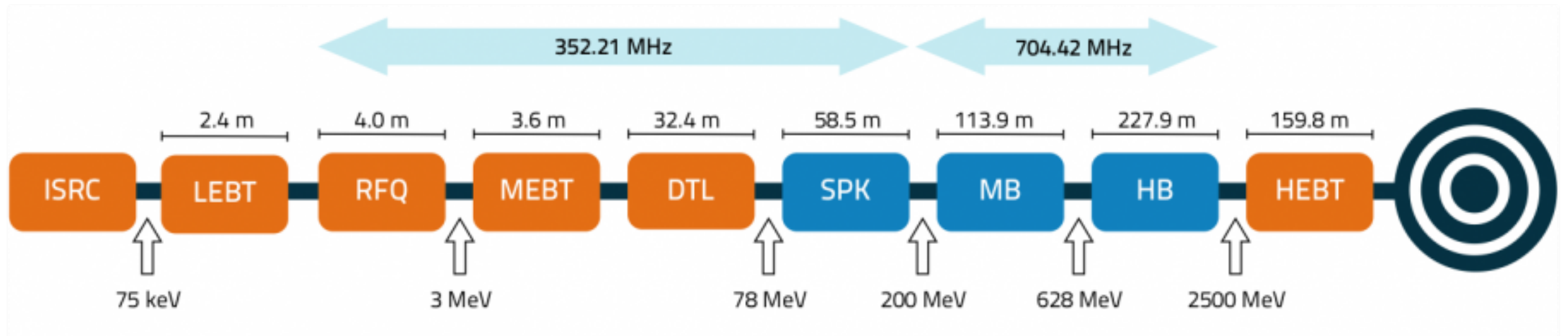
**Rob Ainsworth**

*John Adams Institute for Accelerator Science*

# OUTLINE

- European Spallation Source
- Cavity Modes
  - Spoke Cavities
  - Elliptical Cavities
- Influence of Parasitic Modes
  - Same Order Modes (SOMs)
  - Higher Order Modes (HOMs)
- HOM coupler designs
  - Multipacting

# EUROPEAN SPALLATION SOURCE

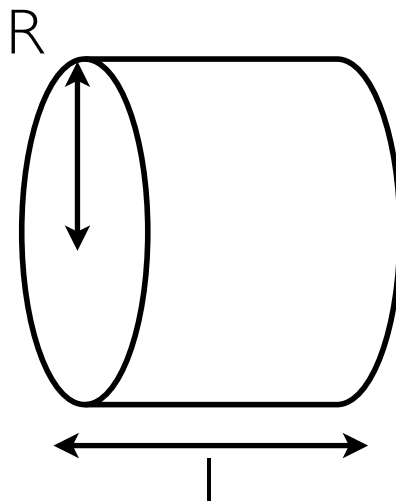


	Value	Unit
Final kinetic energy	2.5	GeV
Current	50	mA
Pulse repetition rate	14	Hz
Bunch frequency	352.21	MHz
Average power	5	MW
Peak power	125	MW

# CAVITY MODES



# PILLBOX CAVITY



Try simple azimuthally symmetric trial solution  $E_z(r, z, t) = R(r)e^{i\omega t}$

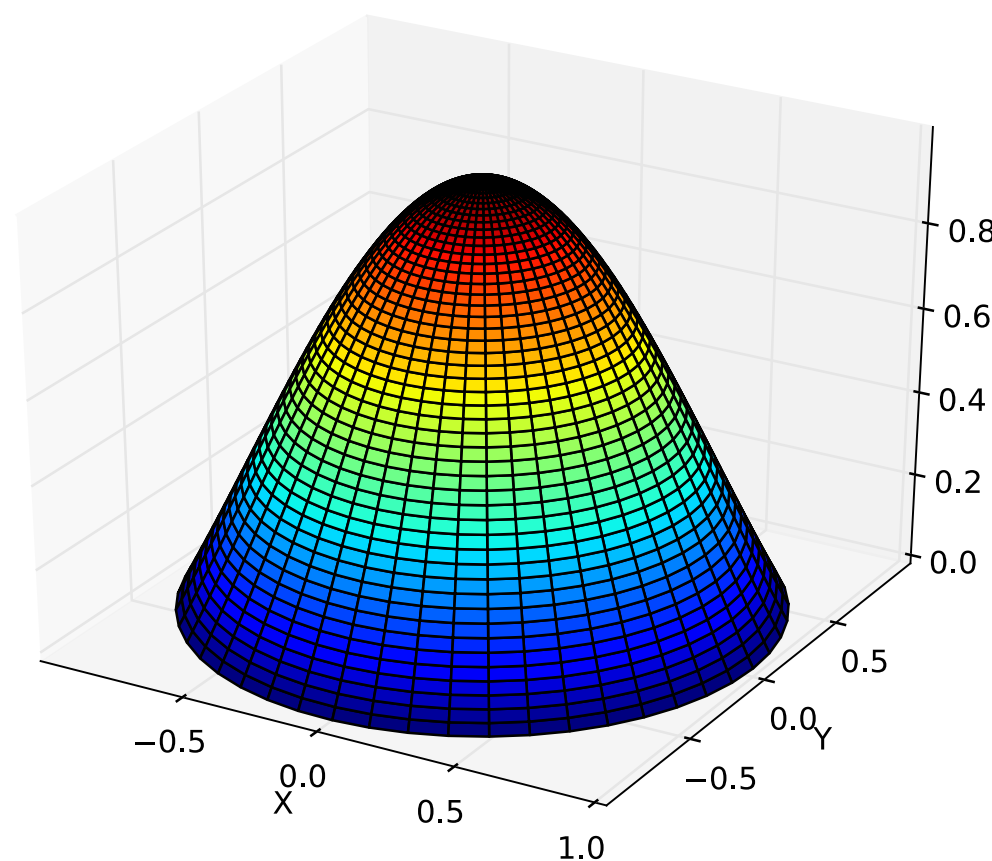
Wave Equation 
$$\frac{\partial^2 E_z}{\partial z^2} + \frac{1}{r} \frac{\partial E_z}{\partial r} + \frac{\partial^2 E_z}{\partial r^2} - \frac{1}{c^2} \frac{\partial^2 E_z}{\partial t^2} = 0$$

Boundary Condition: No tangential E field  
No normal B field

# ACCELERATING MODE

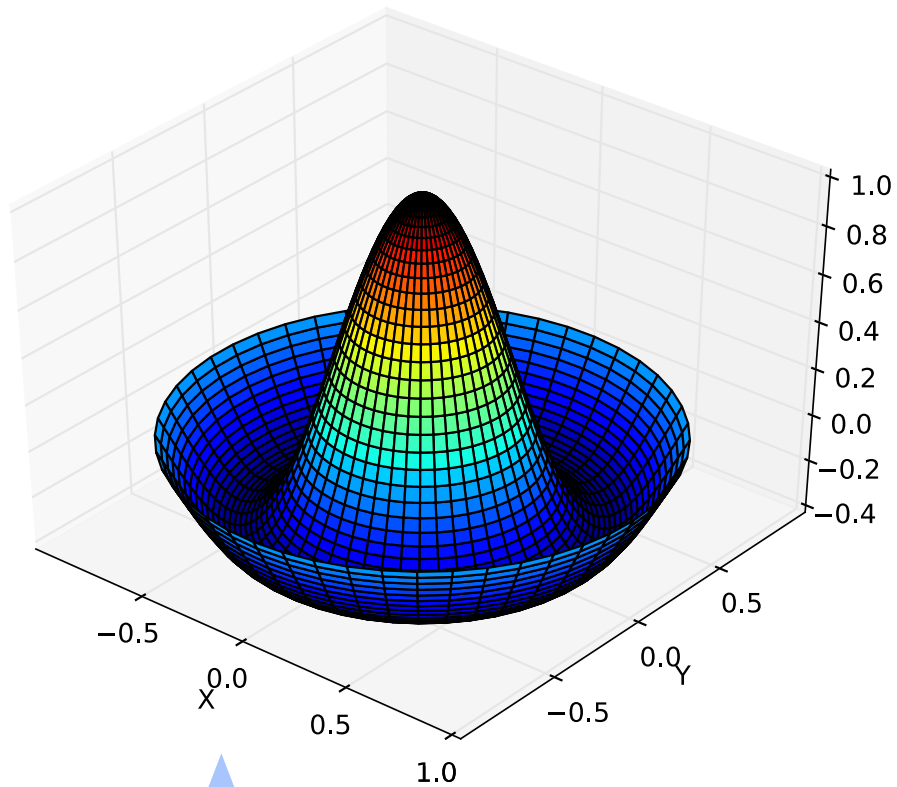
## Transverse Magnetic Mode (TM)

$$E_z = E_0 J_0(k_r r) \cos \omega t \quad B_\theta = -\frac{E_0}{c} J_1(k_r r) \sin \omega t$$



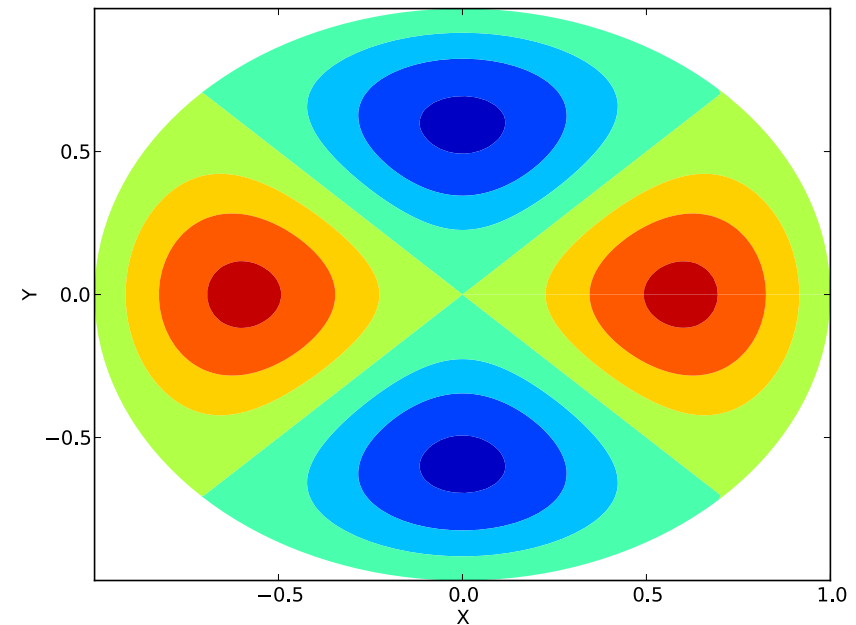
However, not the only mode . .

# HIGHER ORDER MODES

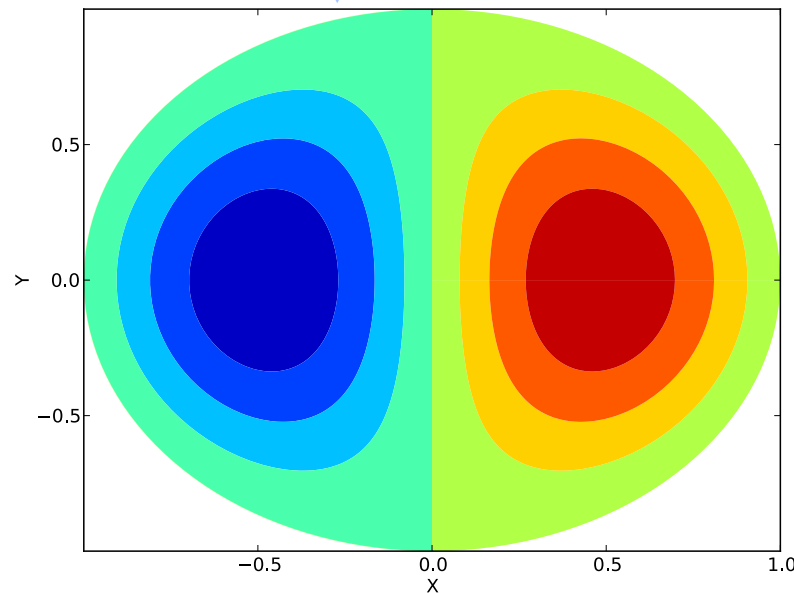


Higher  
order  
monopole

Dipole

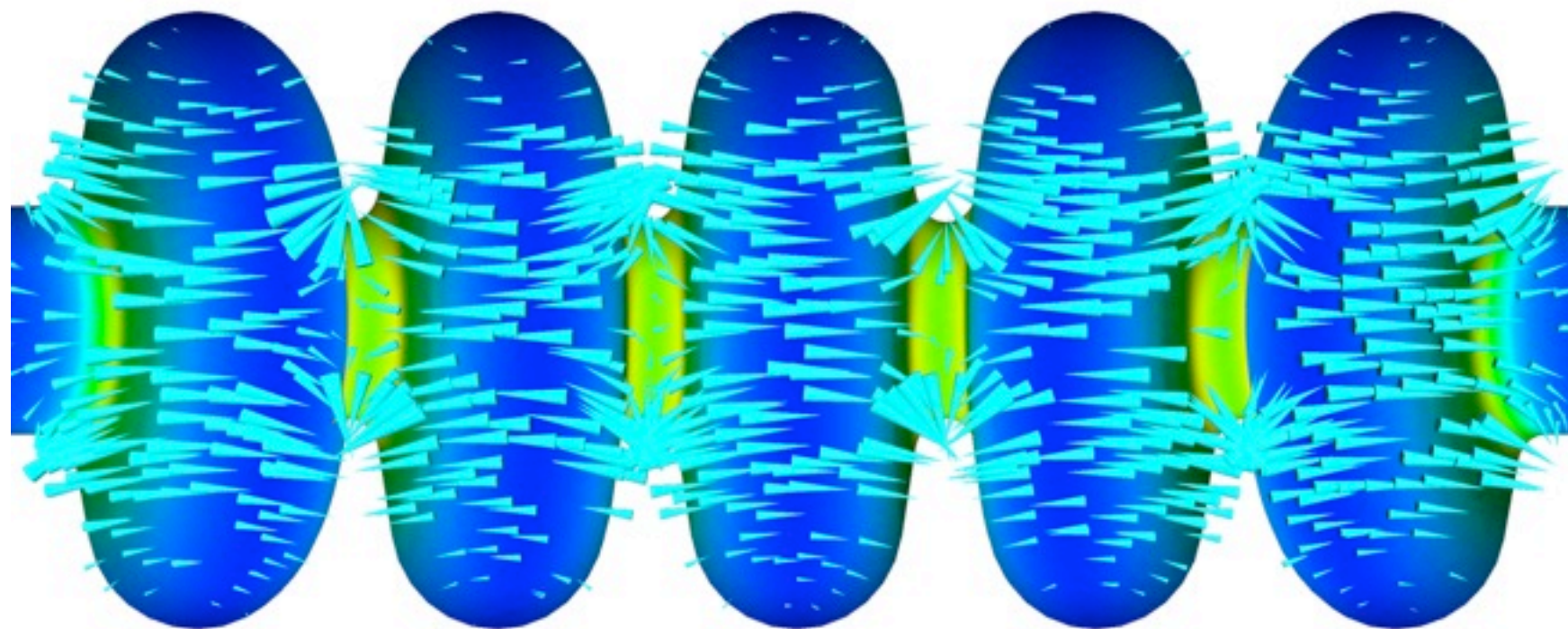


Quadrupole



And many more...

# ELLIPTICAL CAVITIES

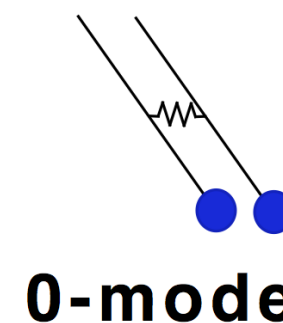


$$\beta_g \lambda / 2$$

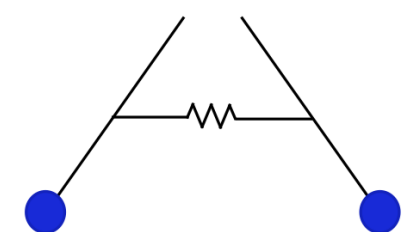
N coupled pillbox  
cavities

Modes split into  
passbands with differing  
phase advance per cell

Two families of ellipticals  
operating in  
 $\pi$  - mode  
@ 704.42 MHz



**0-mode**

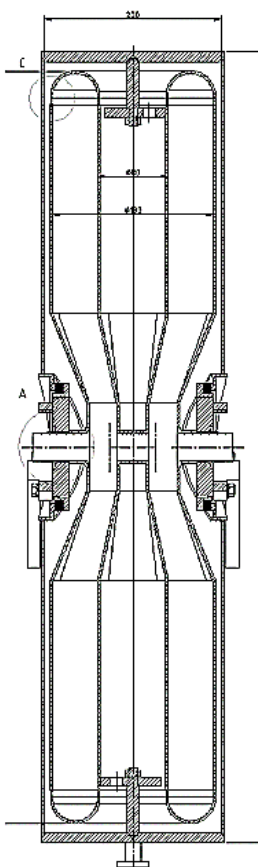
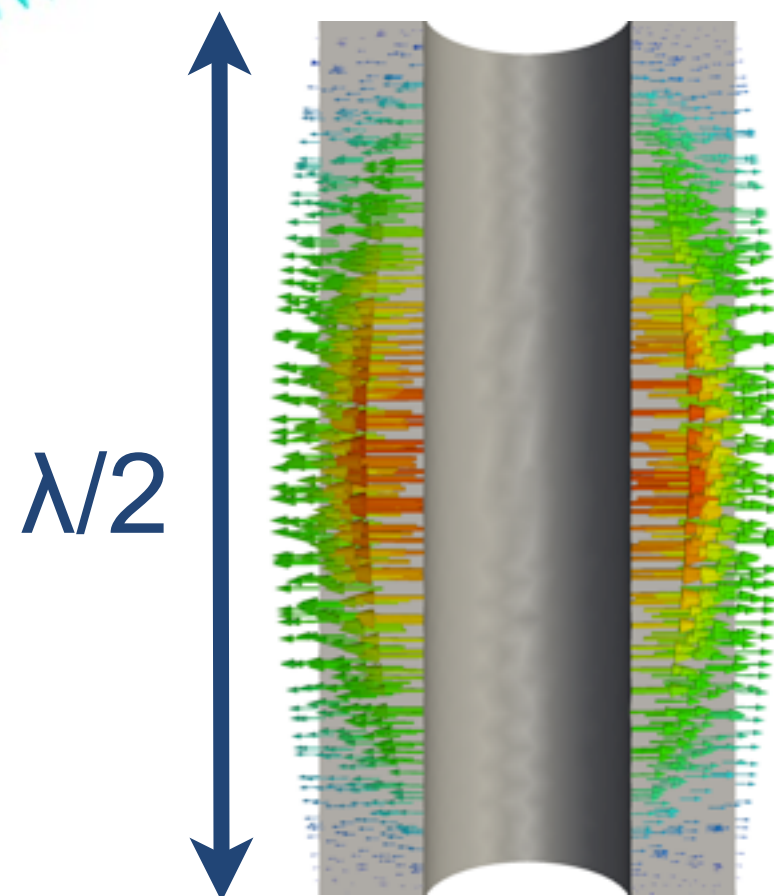
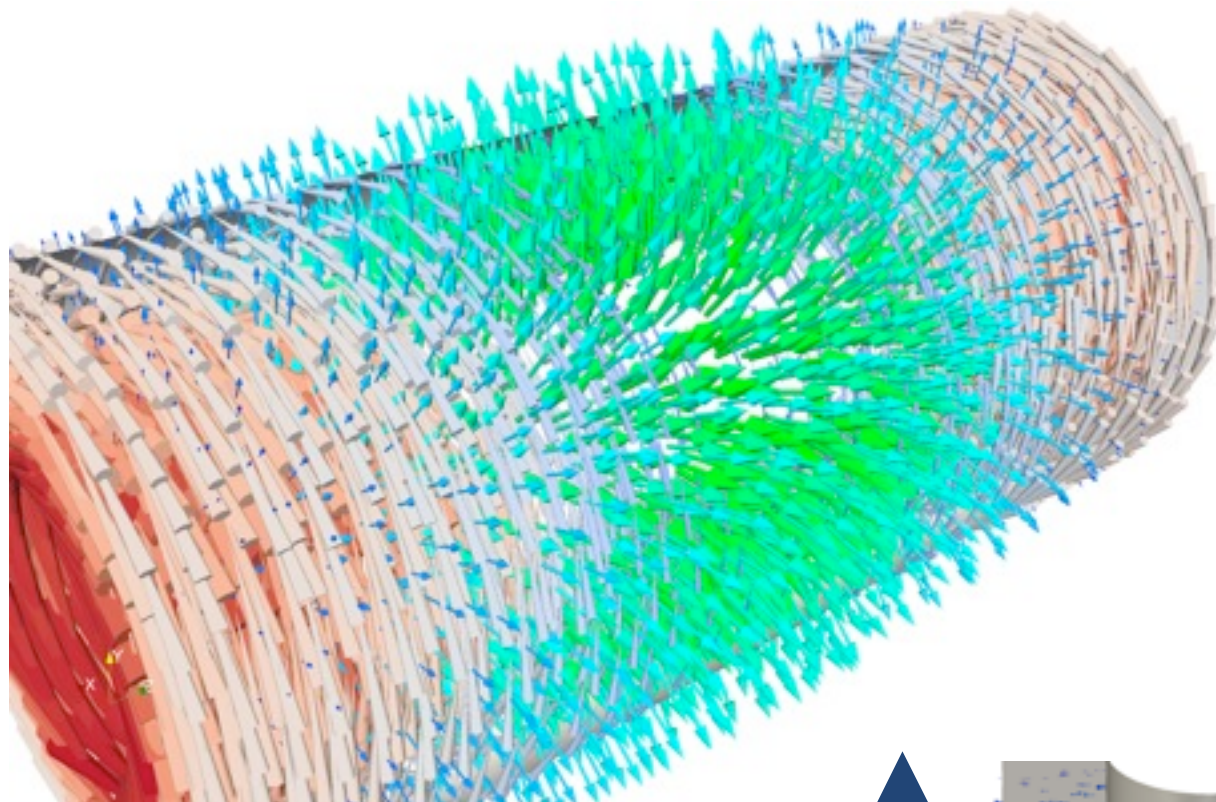


**$\pi$ -mode**



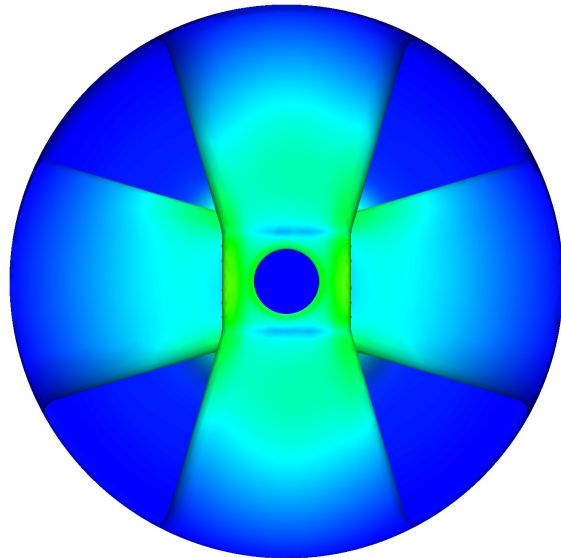
# TEM RESONATOR

# Transverse ElectroMagnetic Mode

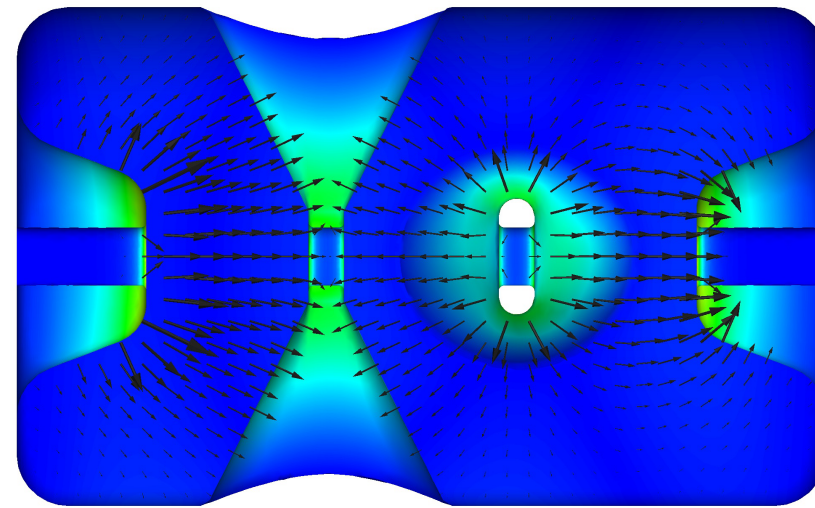


# Half-wave resonator

# SPOKE RESONATORS



Each spoke rotated by  $90^\circ$

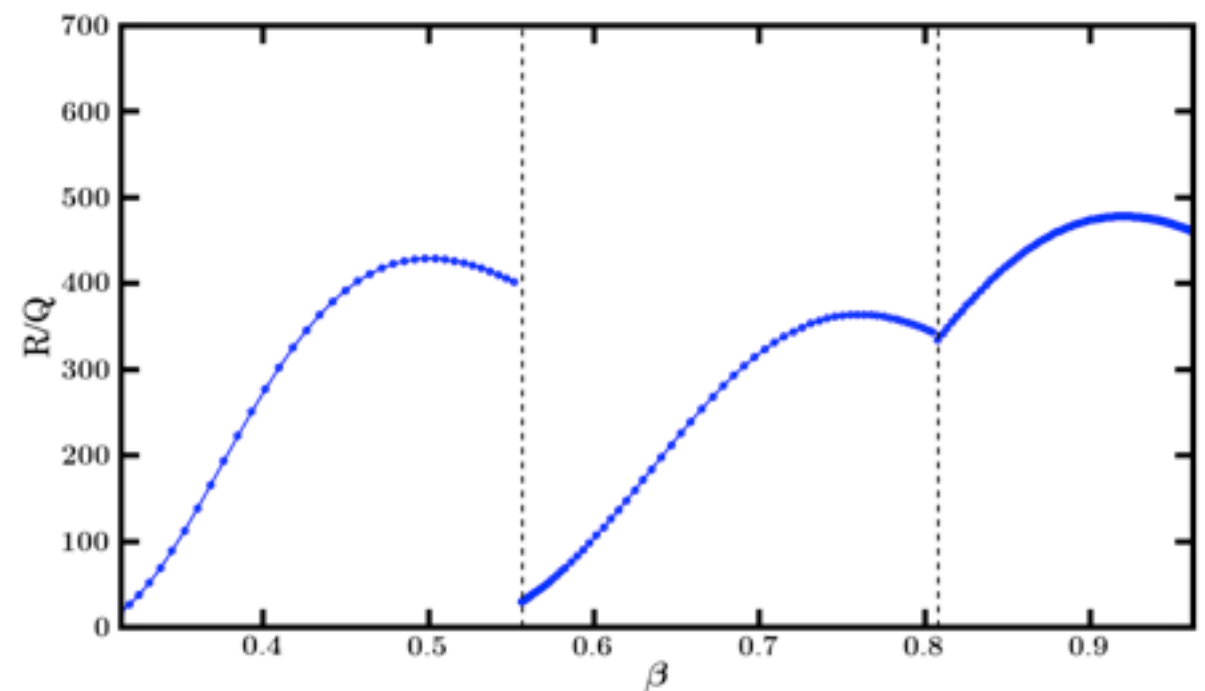


Variant of TEM cavity

$n$  stacked HWRs

# THE NEED FOR 3 FAMILIES

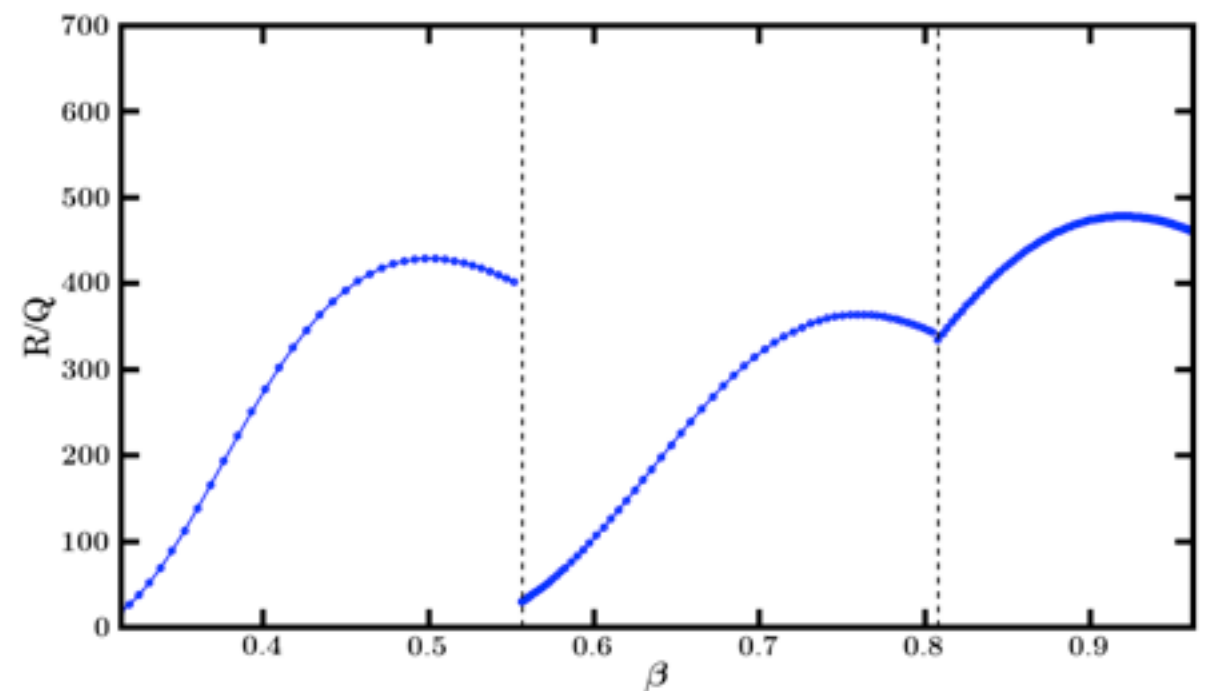
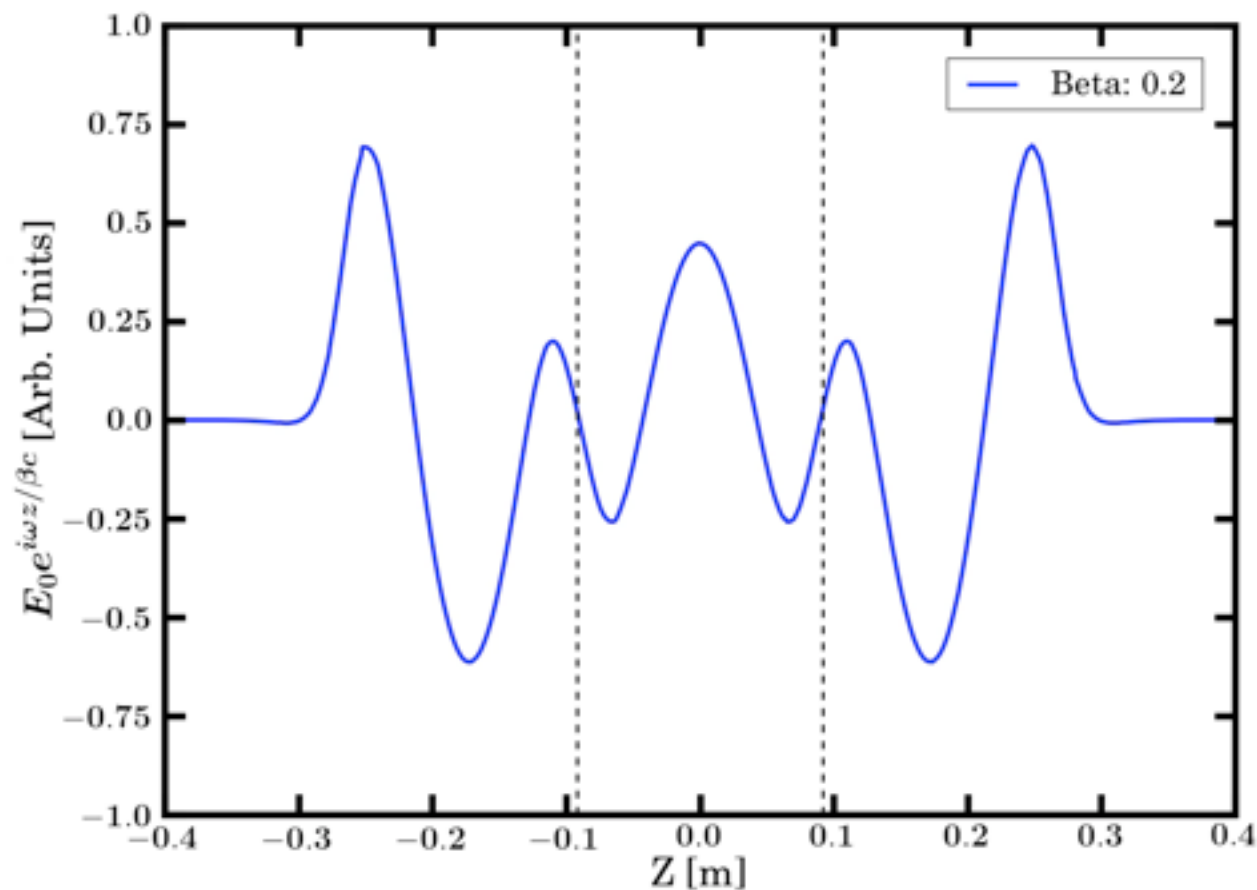
$$(R/Q)_n(\beta) = \frac{\left| \int_{-\infty}^{\infty} E_{z,n}(r=0, z) e^{i\omega_n \frac{z}{\beta c}} dz \right|^2}{\omega_n U_n}$$





# THE NEED FOR 3 FAMILIES

$$(R/Q)_n(\beta) = \frac{\left| \int_{-\infty}^{\infty} E_{z,n}(r=0, z) e^{i\omega_n \frac{z}{\beta c}} dz \right|^2}{\omega_n U_n}$$



# PARASITIC MODES

# MOTIVATION

**Beam induced modes** in SCRF cavities may drive the **beam unstable** and **increase the cryogenic load**, therefore **HOM couplers** are usually installed to provide sufficient damping.

....However, recent experience at SNS has shown **couplers may be unnecessary** and have **degraded performance** of the machine.

Questions:

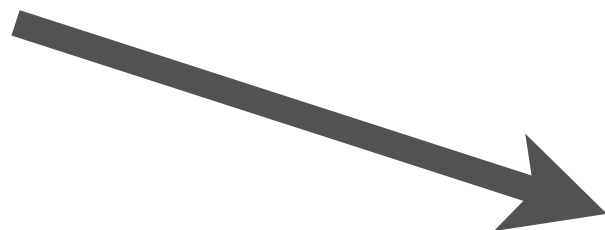
**Will SOMs mean the cavity design needs to be changed?**  
**Does ESS need HOM couplers?**

• **Beam dynamics**



Simulations performed by myself

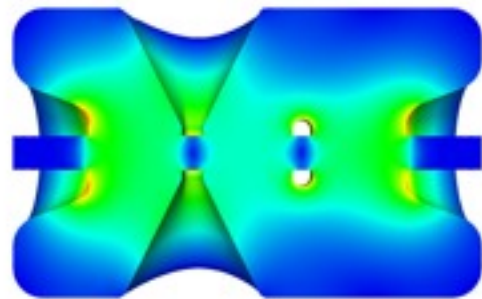
• **Power**



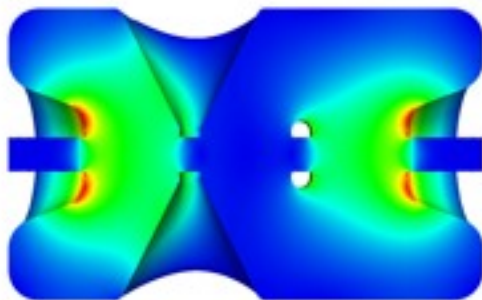
Simulations performed at CEA Saclay

# SAME ORDER MODES

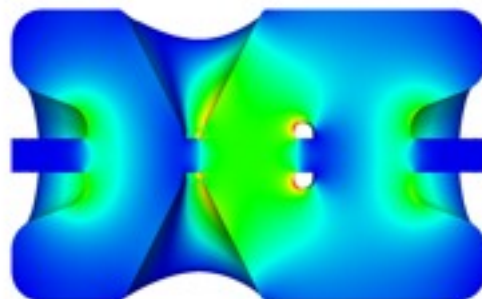
$\pi$ -mode  
352.21 MHz



0-mode  
362.69 MHz

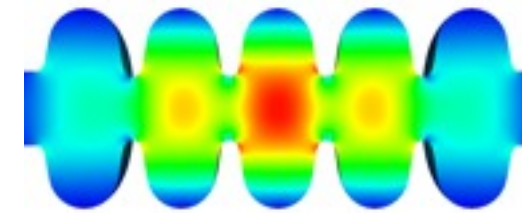


396.96 MHz

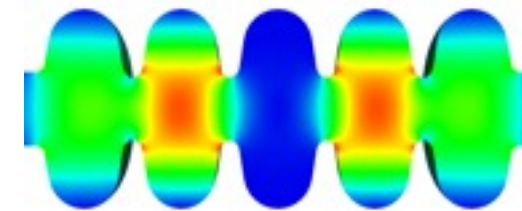


Part of  
same passband as  
fundamental

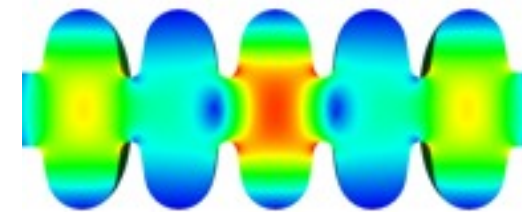
Same order, just  
different phase  
advance



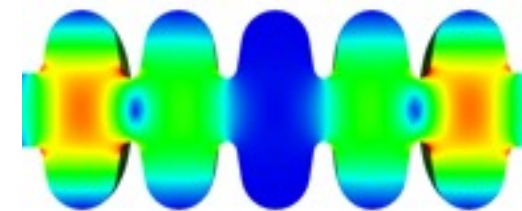
$\pi/5$  - mode  
693.19 MHz



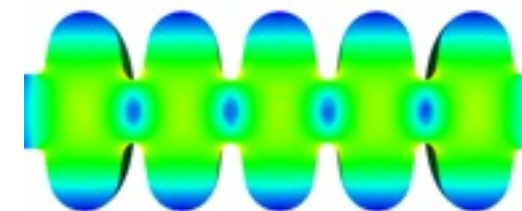
$2\pi/5$  - mode  
696.30 MHz



$3\pi/5$  - mode  
700.14 MHz



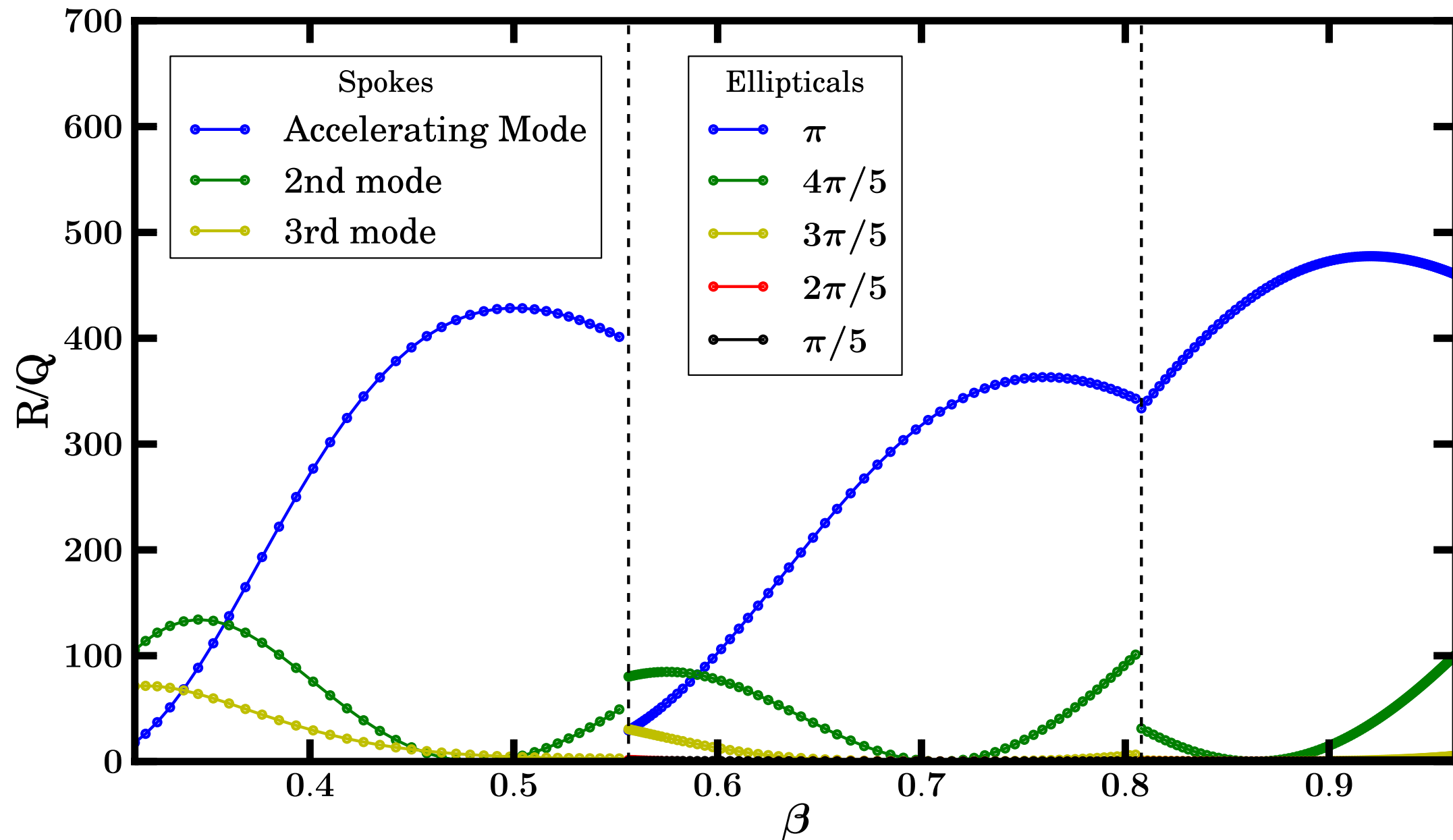
$4\pi/5$  - mode  
703.2 MHz



$\pi$  - mode  
704.42 MHz

Close in frequency to accelerating mode  
➡ Cannot damp using couplers

# SAME ORDER MODES



High  $R/Q$  with respect to accelerating mode

➡ Modify geometric beta

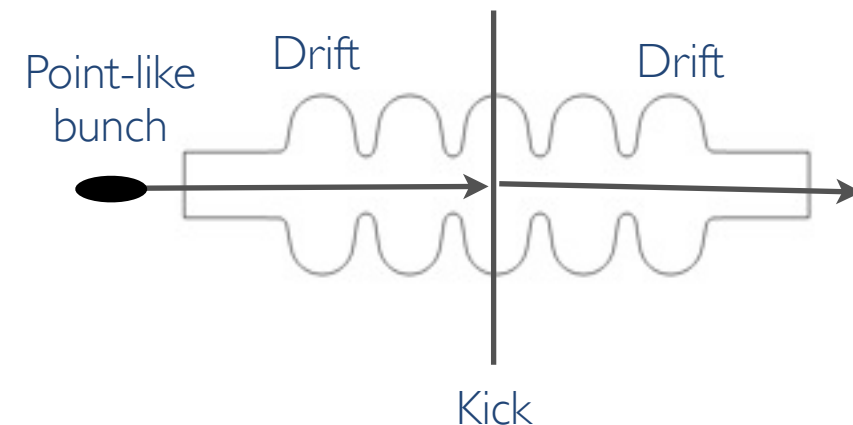
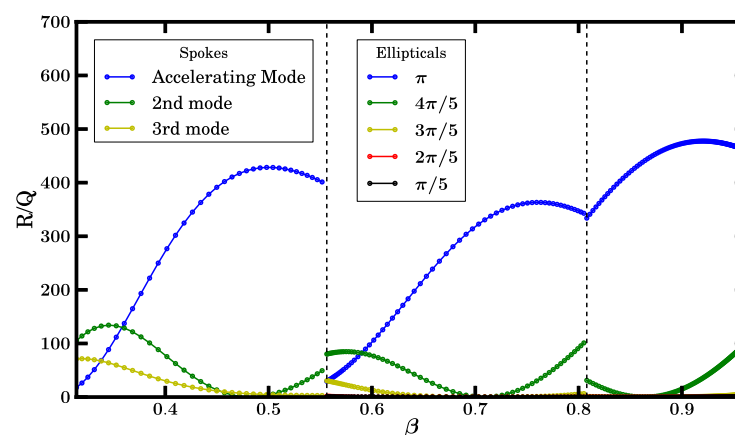
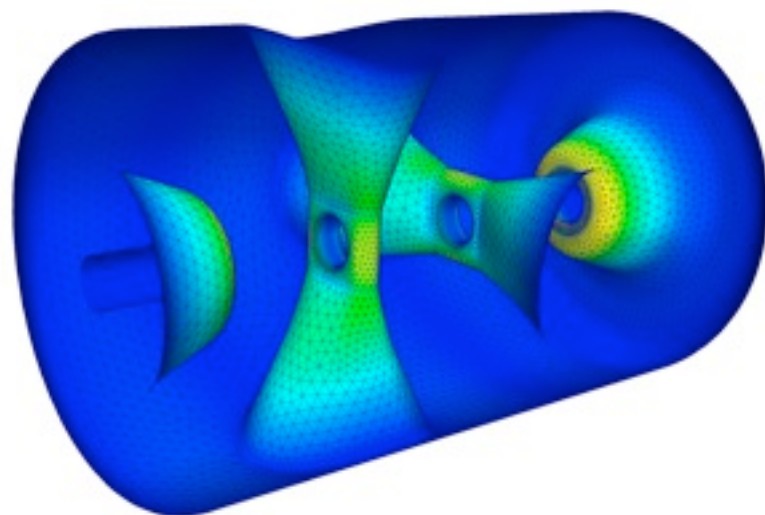
➡ Alter velocity partitioning

# SIMULATION INFO

Simulate cavity geometries to extract field-maps

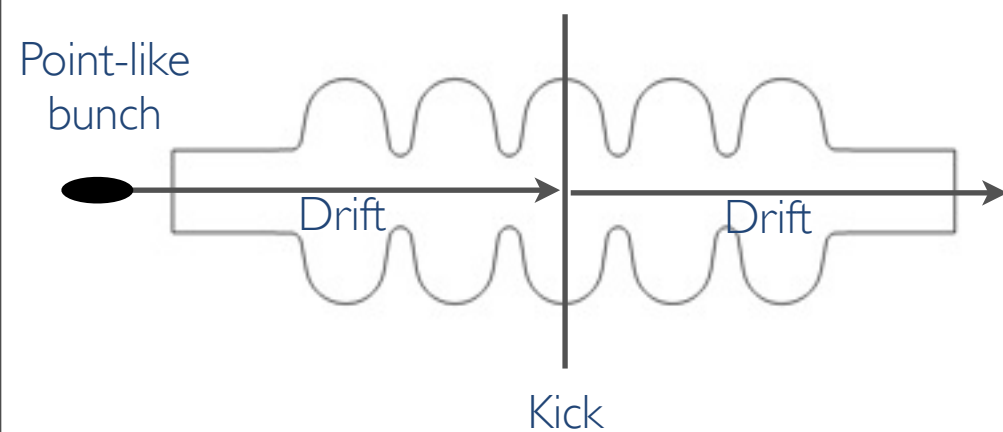
Determine R/Q, frequencies of modes below cutoff

Calculate the influence of modes of beam quality





# SIMULATION INFO



Energy and time error calculated at each cavity with respect to synchronous bunch

$$\Delta E^{(m+1)} = \Delta E^{(m)} + \Delta U_{RF}^{(m)} + \Delta U_n^{(m)}$$

$$\Delta t^{(m+1)} = \Delta t^{(m)} + (dt/dE)_E^{(m)} \cdot \Delta E^{(m)}$$

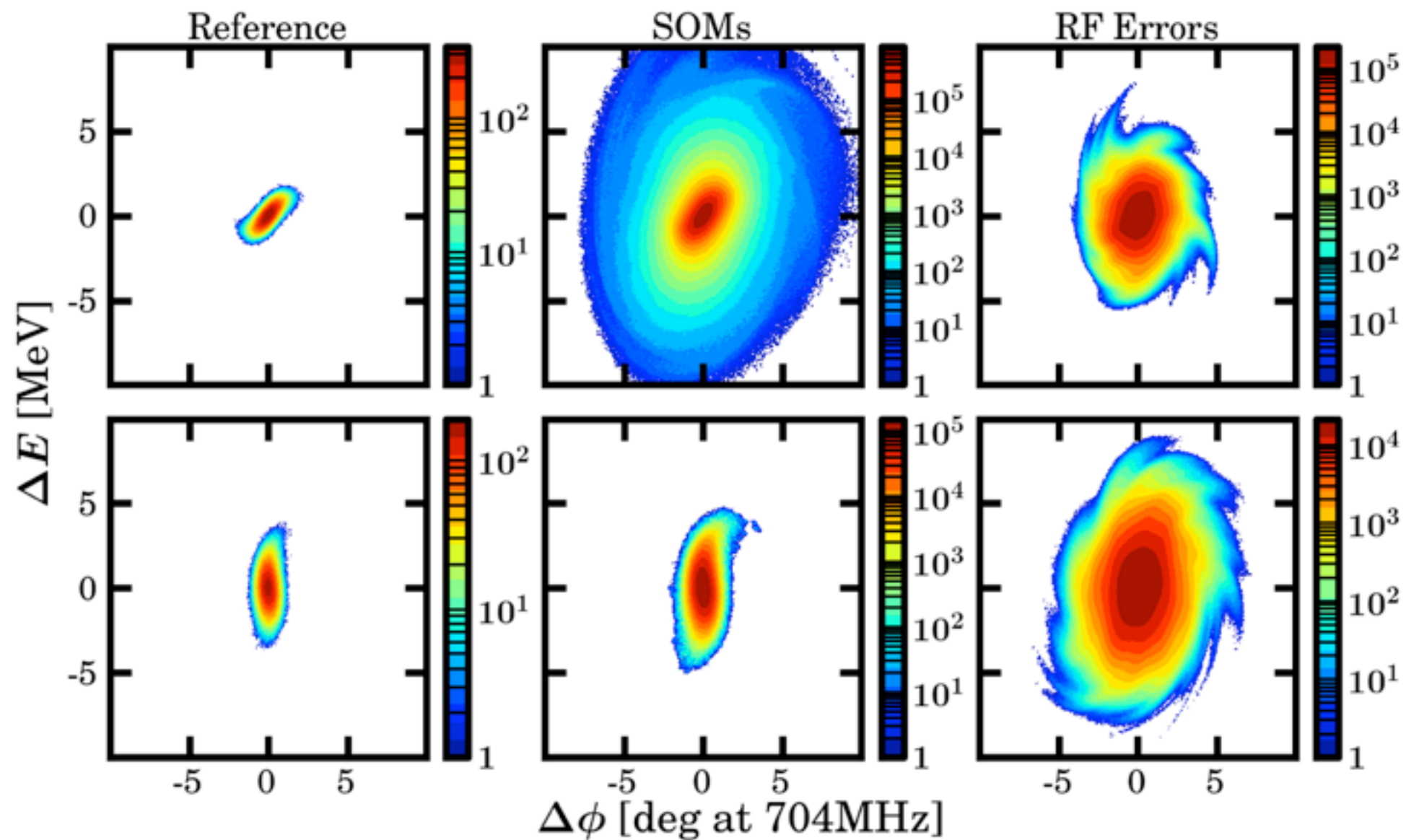
- 1 million point-like bunches tracked per linac
- SOM/HOM frequencies distributed with a gaussian spread
- $\sigma = 1.09 \times 10^{-3} \cdot |f_0 - f_{\text{hom}}|$

$$\Delta U_n = q(\Re(V_n) \cos(\omega_n dt) - \Im(V_n) \sin(\omega_n dt)) - \frac{1}{2} \Delta V_{q,n}$$

$$\Delta V_{q,n} = -q \frac{\omega_n}{2} (R/Q)_n(\beta)$$



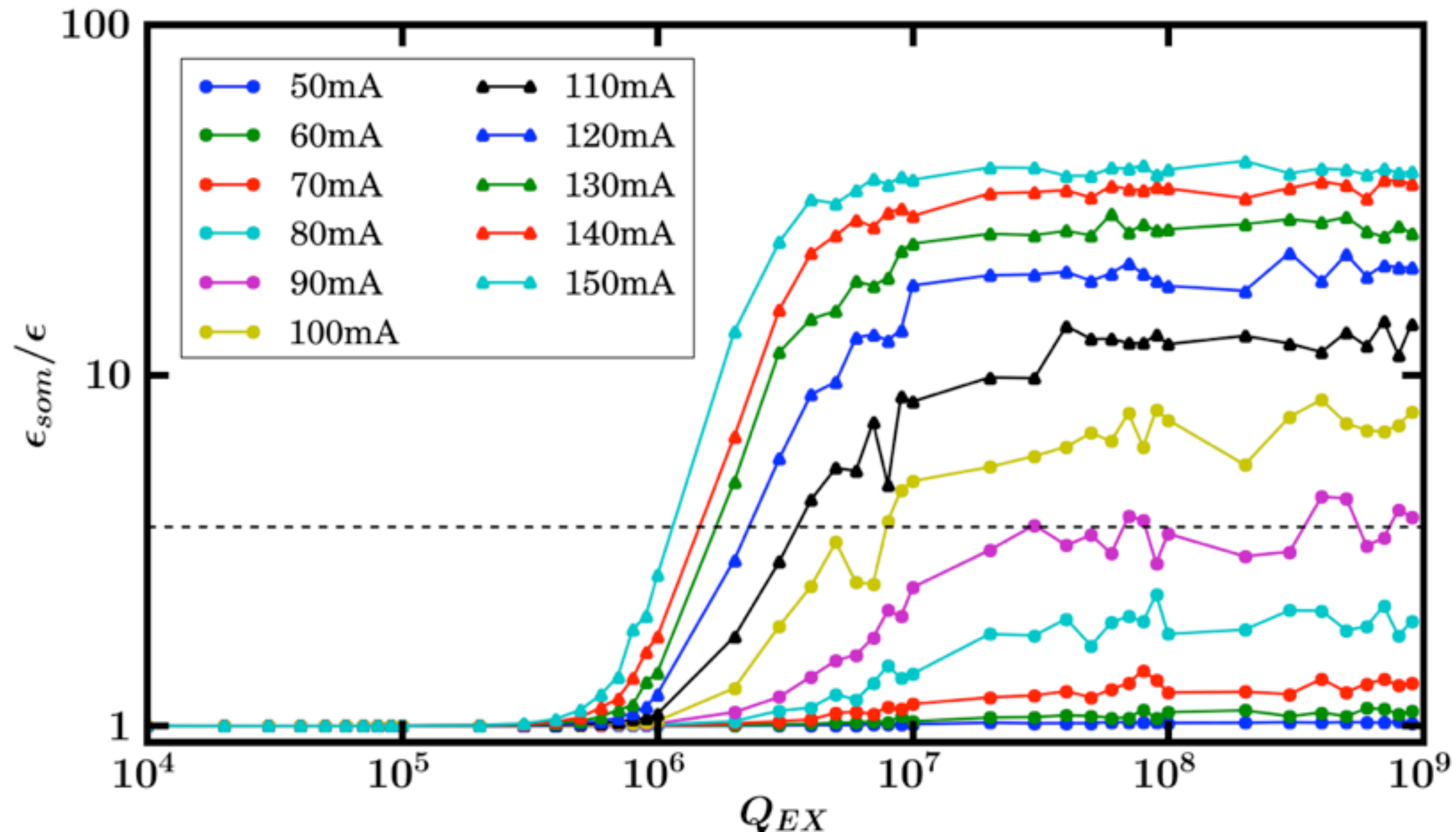
# COMPARISON OF LINACS



It is possible to design a linac susceptible to SOMs however the latest baseline shows no adverse effects

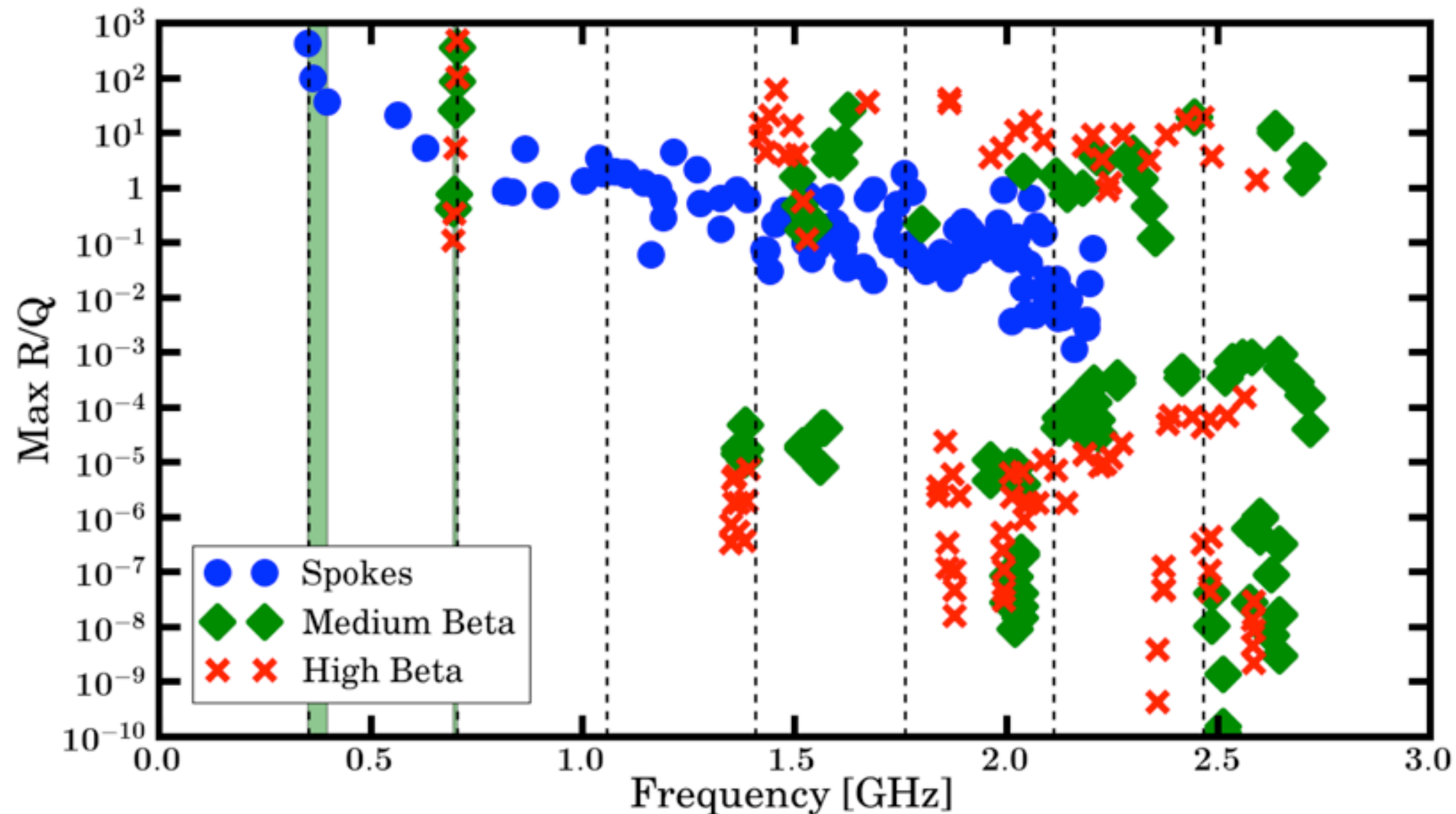
# CURRENT & DAMPING SCAN

$$T_{d,n} = 2Q_{L,n}/\omega_n \approx 2Q_{EX,n}/\omega_n$$



SOMs start to become problematic at ~90 mA

# HIGHER ORDER MODES

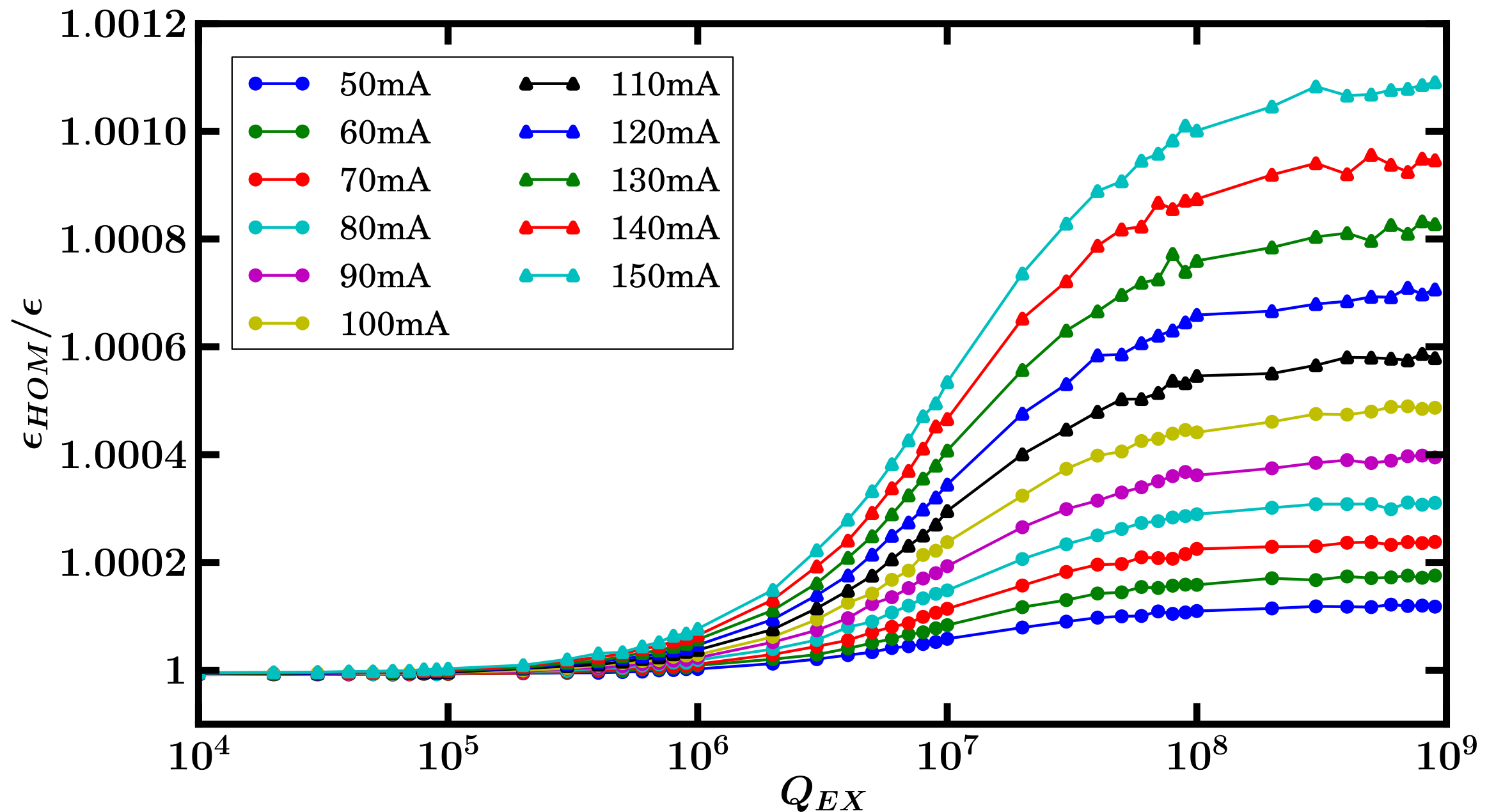


Need to determine if HOMs are a problem

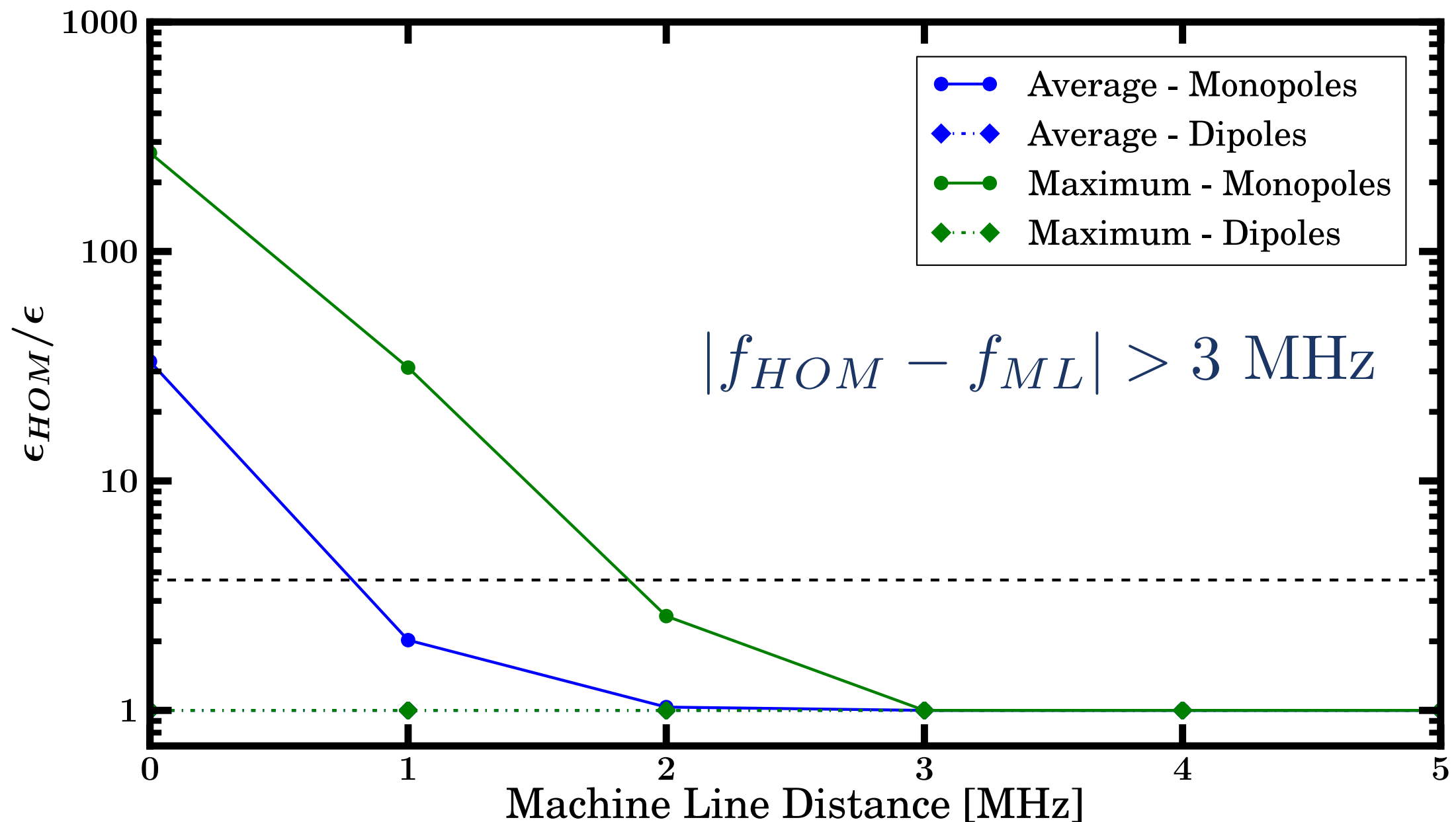
**Are HOM couplers needed?**

$$f_{ML} = n \cdot 352.21 \text{ MHz}$$

# CURRENT & DAMPING SCAN



# SAFE DISTANCE

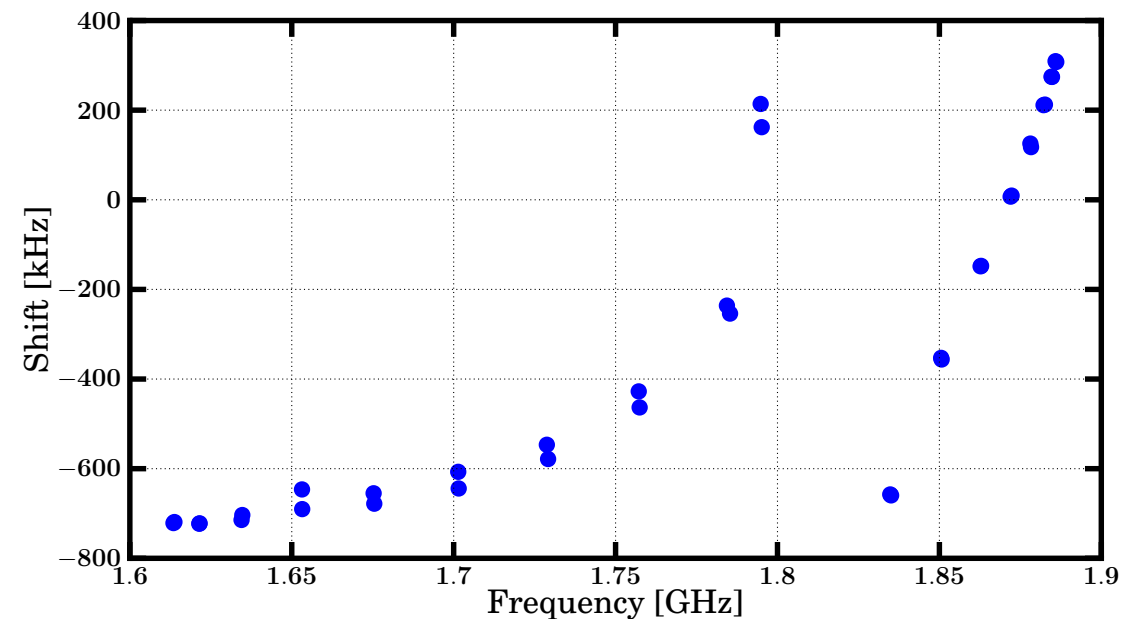
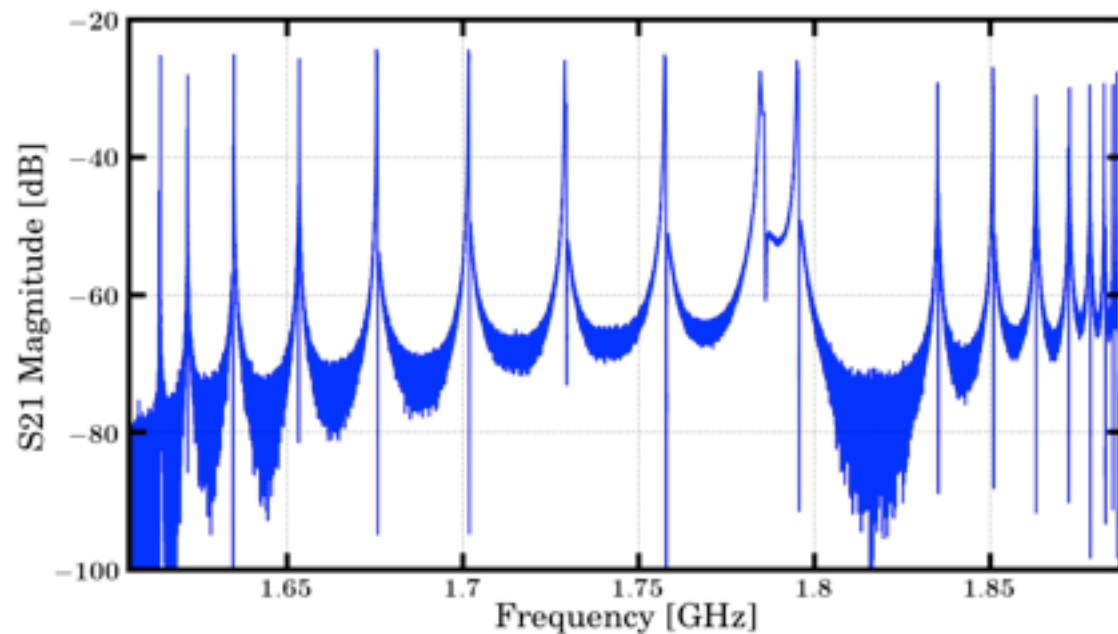
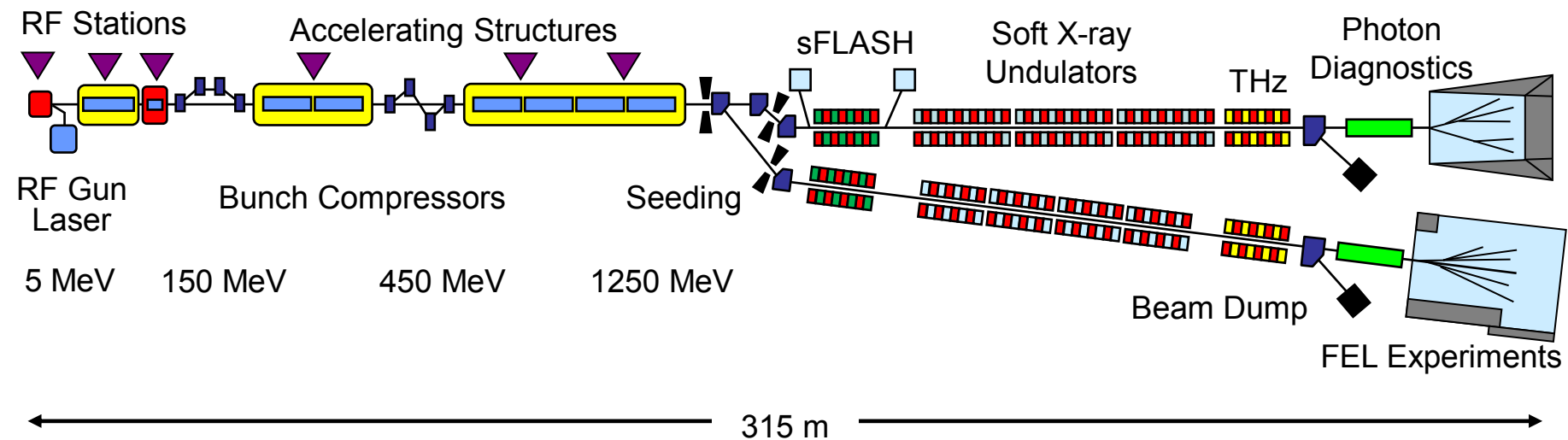


HOMs should be at least 3 MHz away from  
a machine line in cavity design

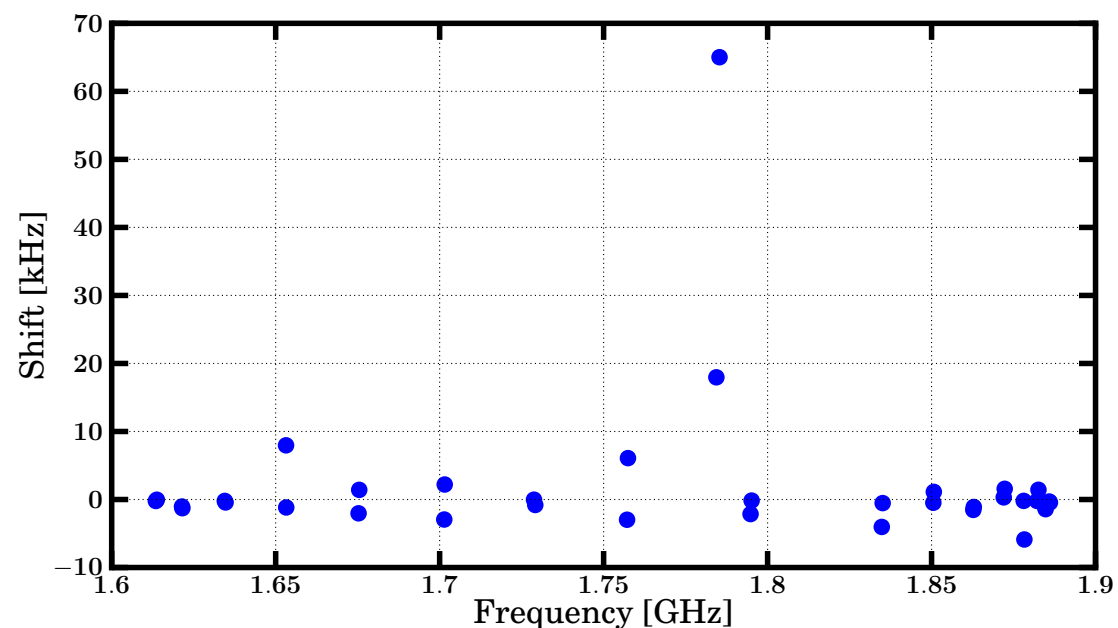
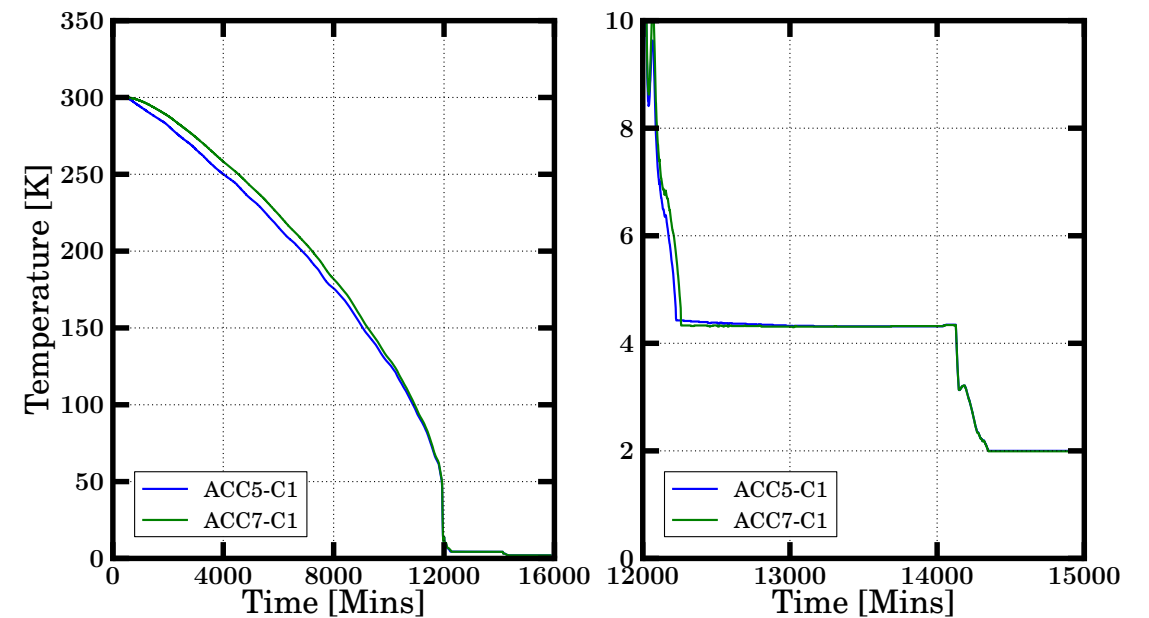
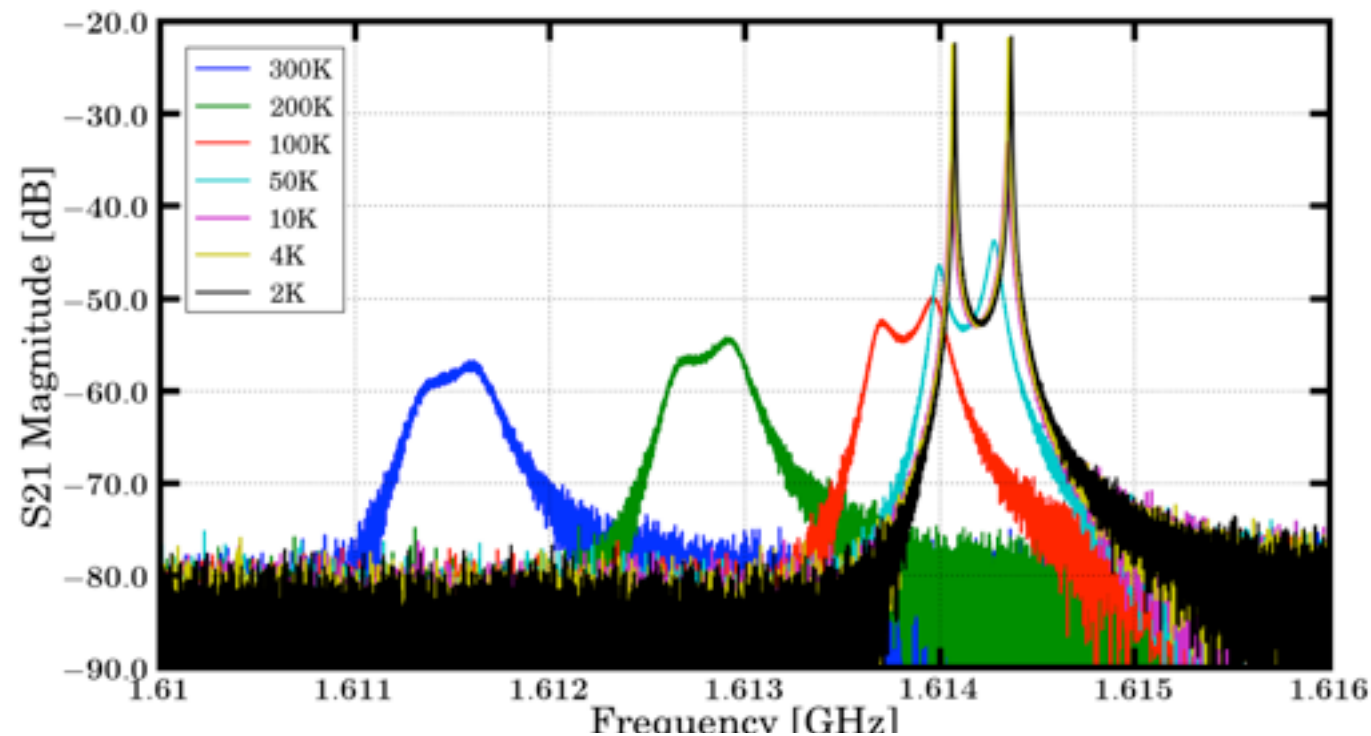
$$f_{ML} = n \cdot 352.21 \text{ MHz}$$



# DETUNING STUDIES



# WARMUP, COOLDOWN AND RETUNED

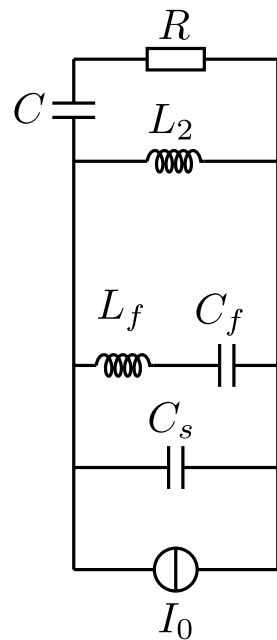
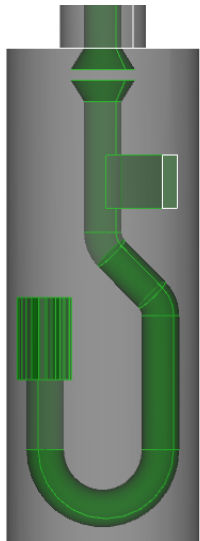


Total shift after all procedures  
on the order of a few kHz

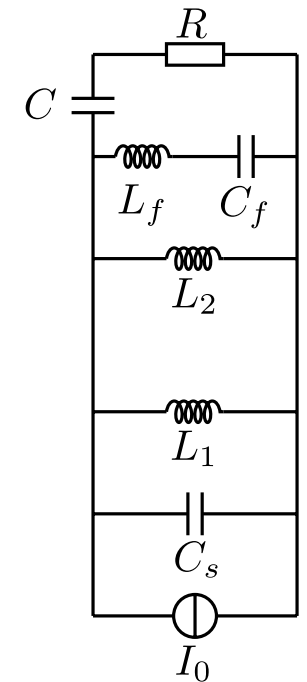
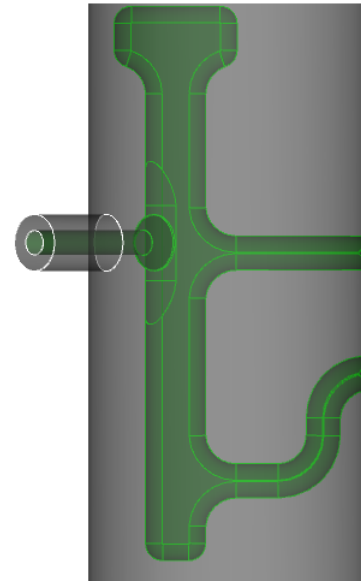


# HOM COUPLER STUDIES

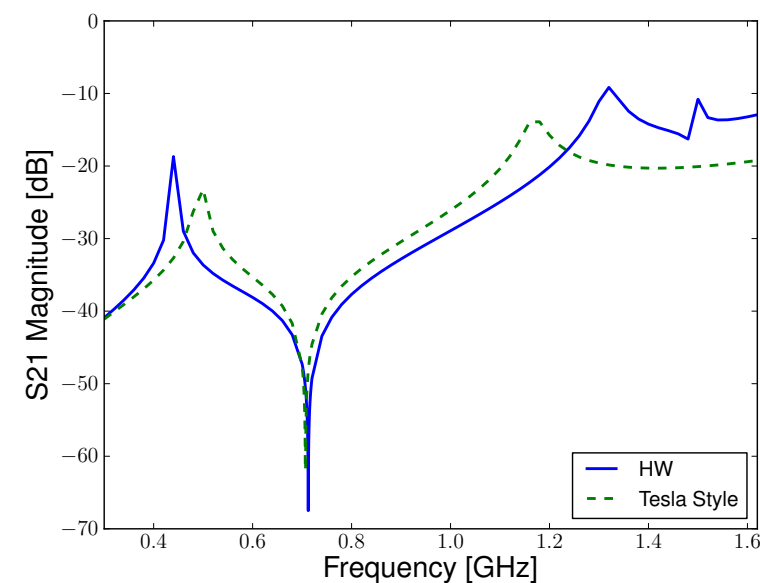
# INITIAL DESIGNS



Designed by Rostock  
University  
(C. Potratz, H.W. Glock)



Rescaled SNS  
coupler (R. Calaga)



# MULTIPACTING

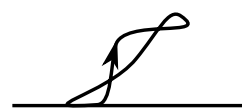
One point

Two point

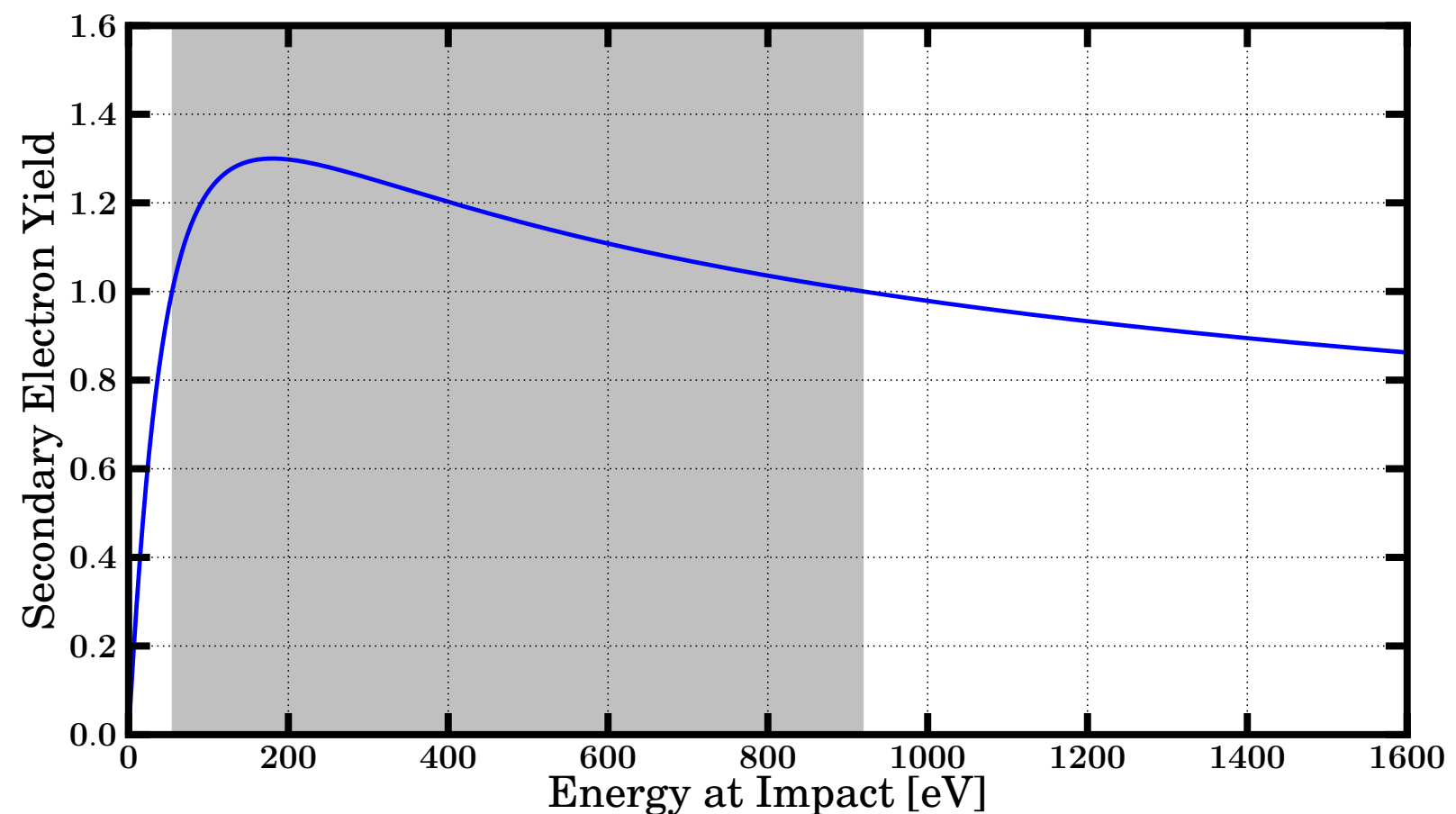
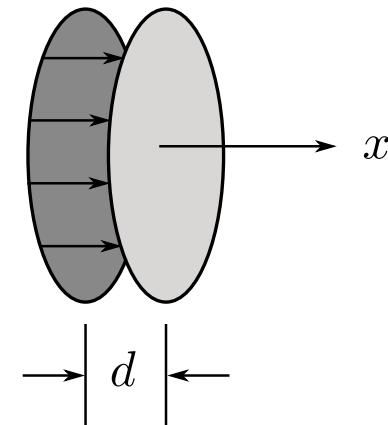
1st Order

2nd Order

3rd Order



$$E_x = E_0 \sin(\omega_g t)$$



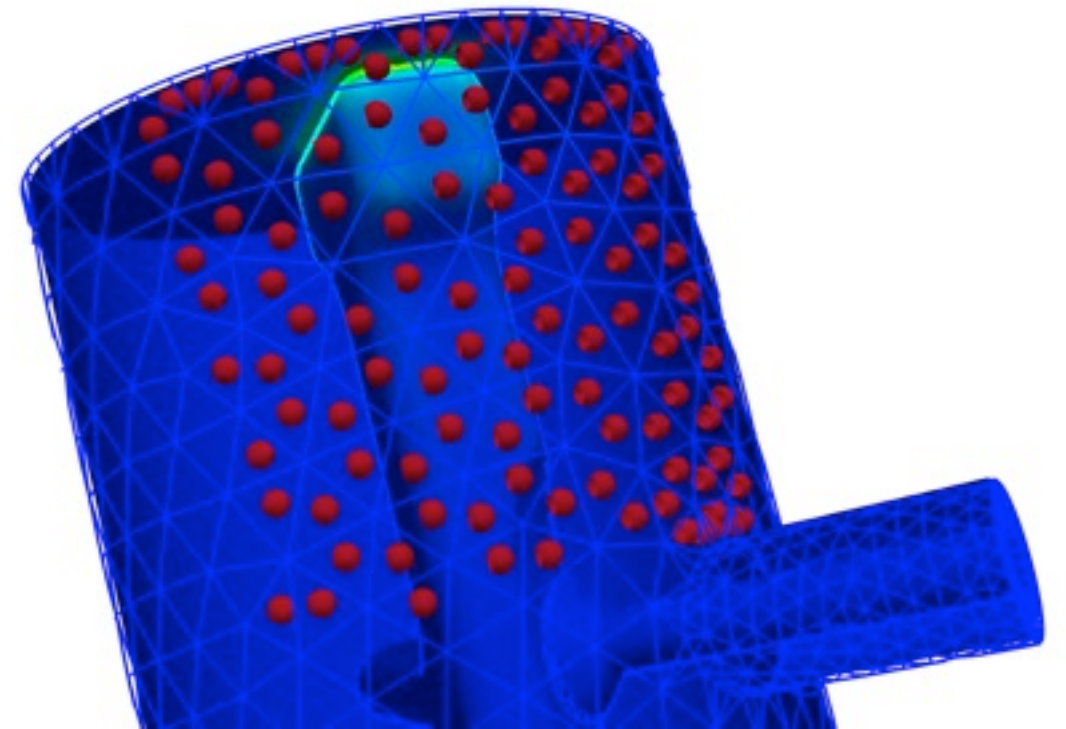
# TRACK3P

Define bounding box for emission

Particles emitted from centre of mesh elements within box

Occurs every  $3.6^\circ$  for 1 RF cycle

Particles tracked for a further 19 RF cycles



# TRACK3P

Upon impact with a surface

If phase conditions correct

Particle re-emitted normal to surface at 2eV

Particle survives more than 4 impacts

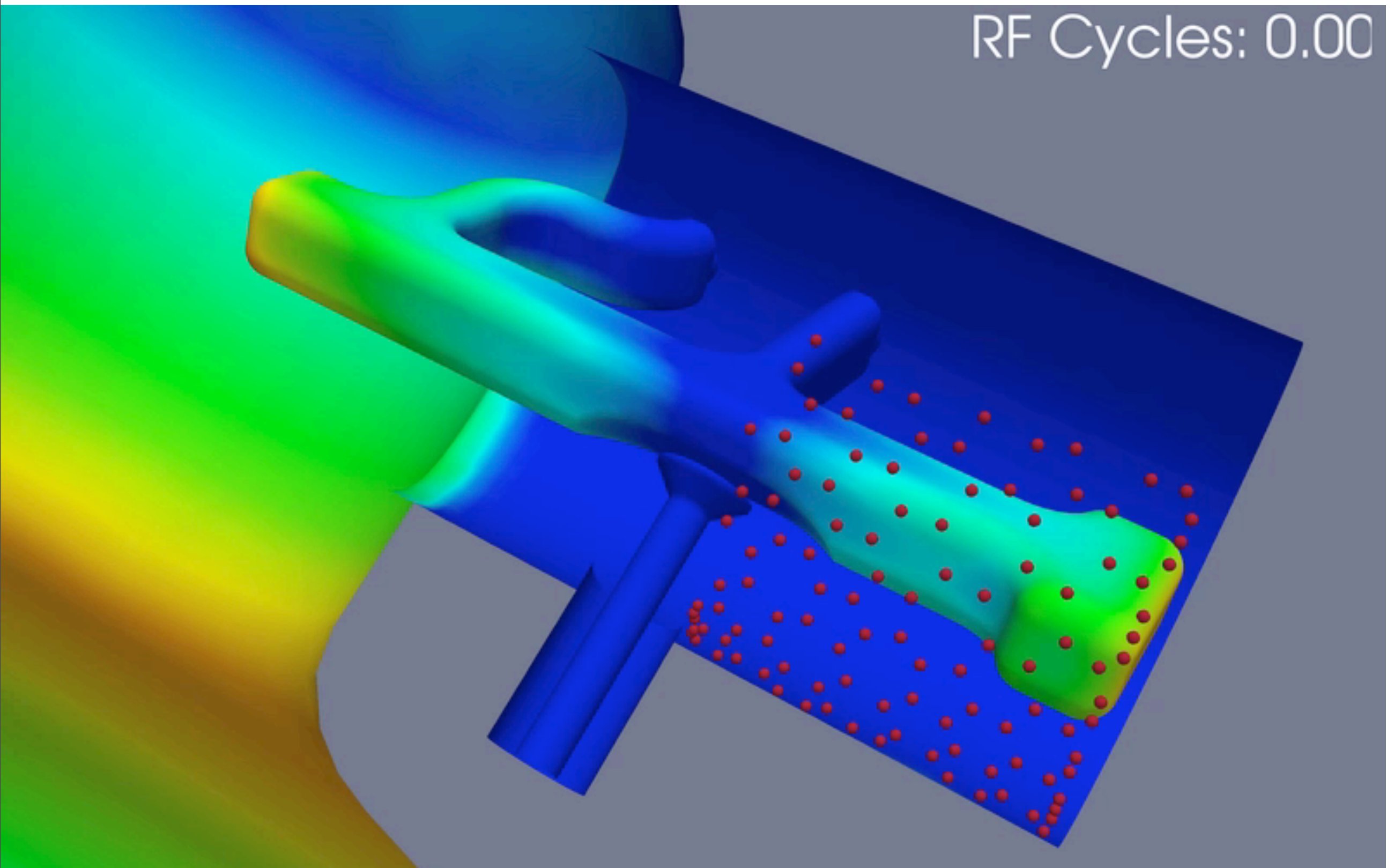


**RESONANT**

Note: 20RF cycles means cannot resolve trajectories higher than 5th order

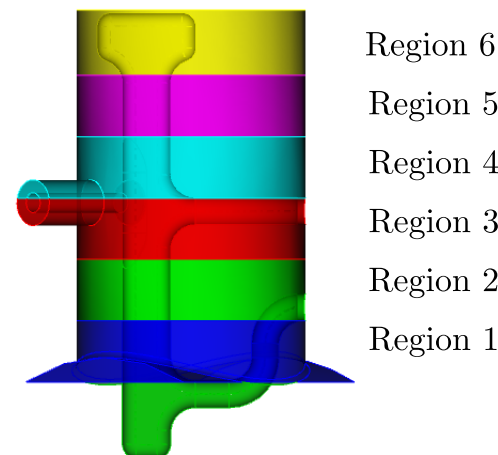
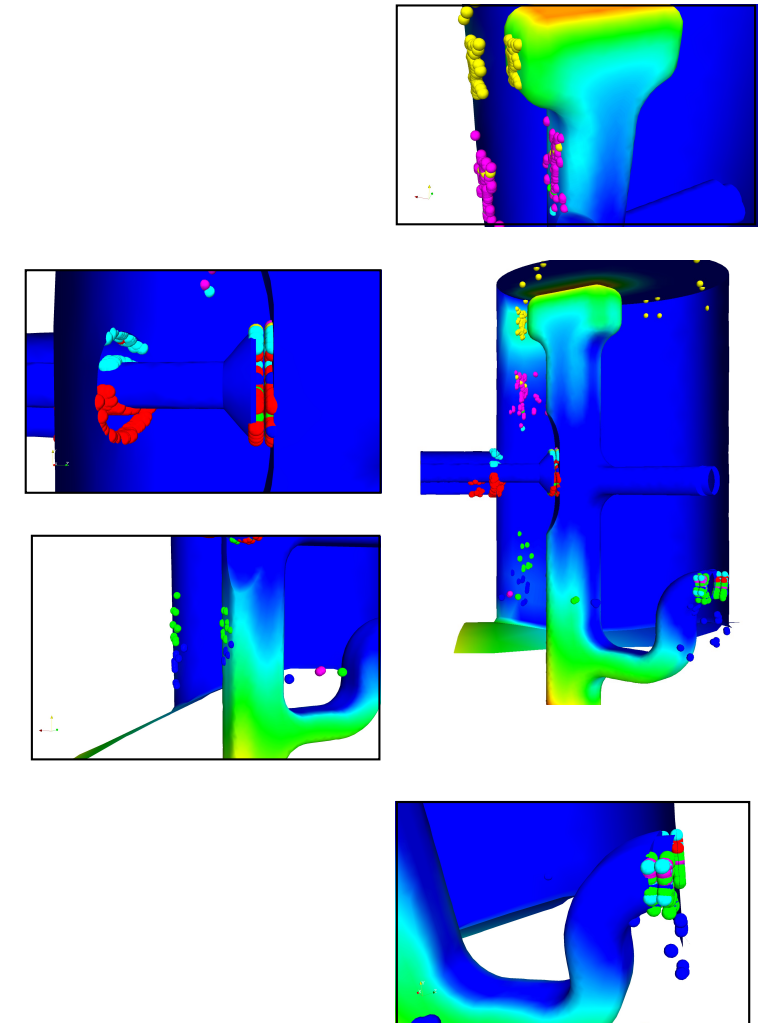
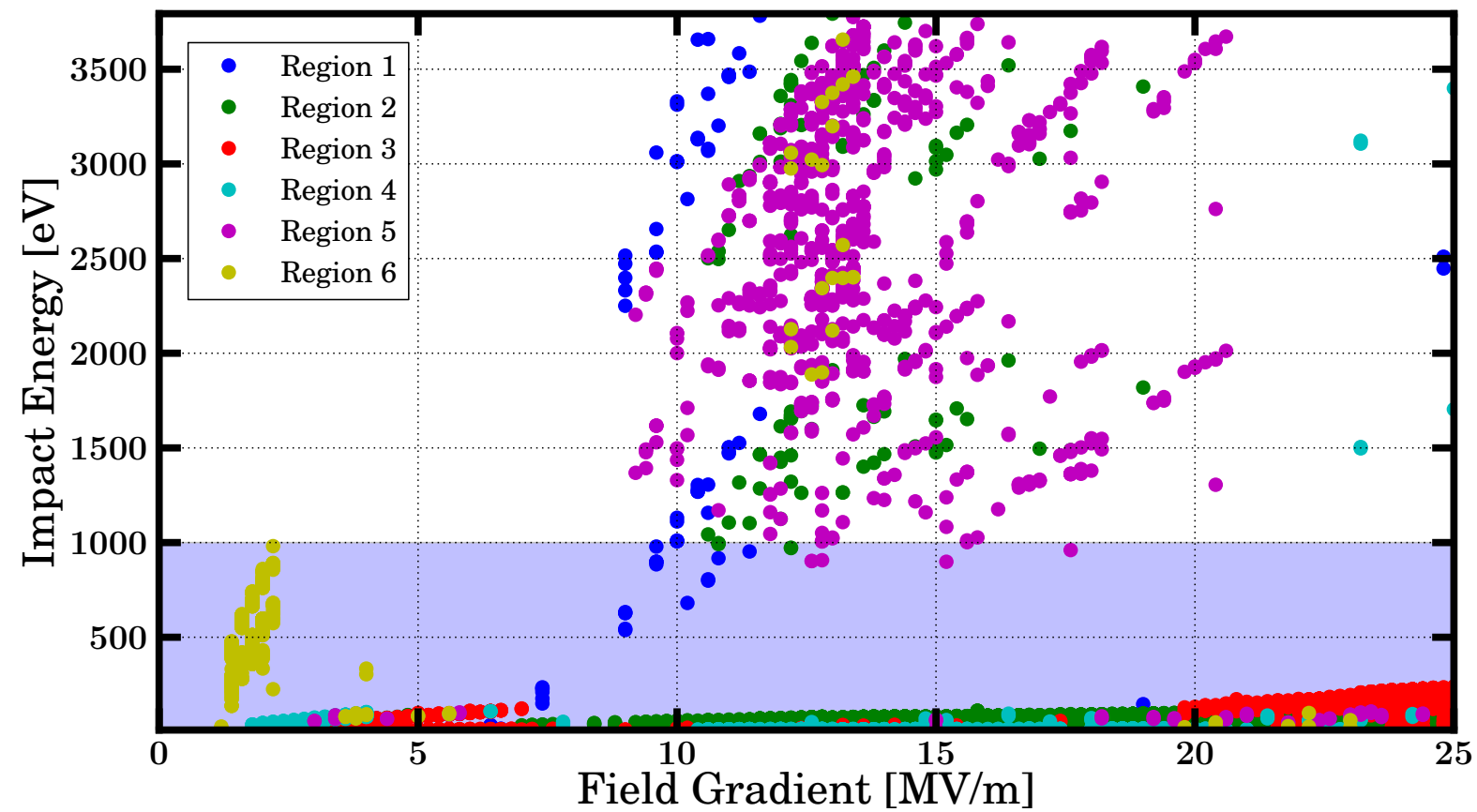
# MULTIPACTING

<http://twiki.ph.rhul.ac.uk/twiki/pub/PP/Public/RobAinsworthRCDesign704/RC-Coupler-highQuality.mov>



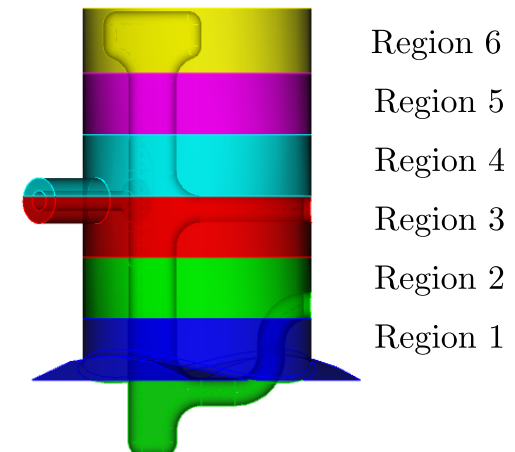
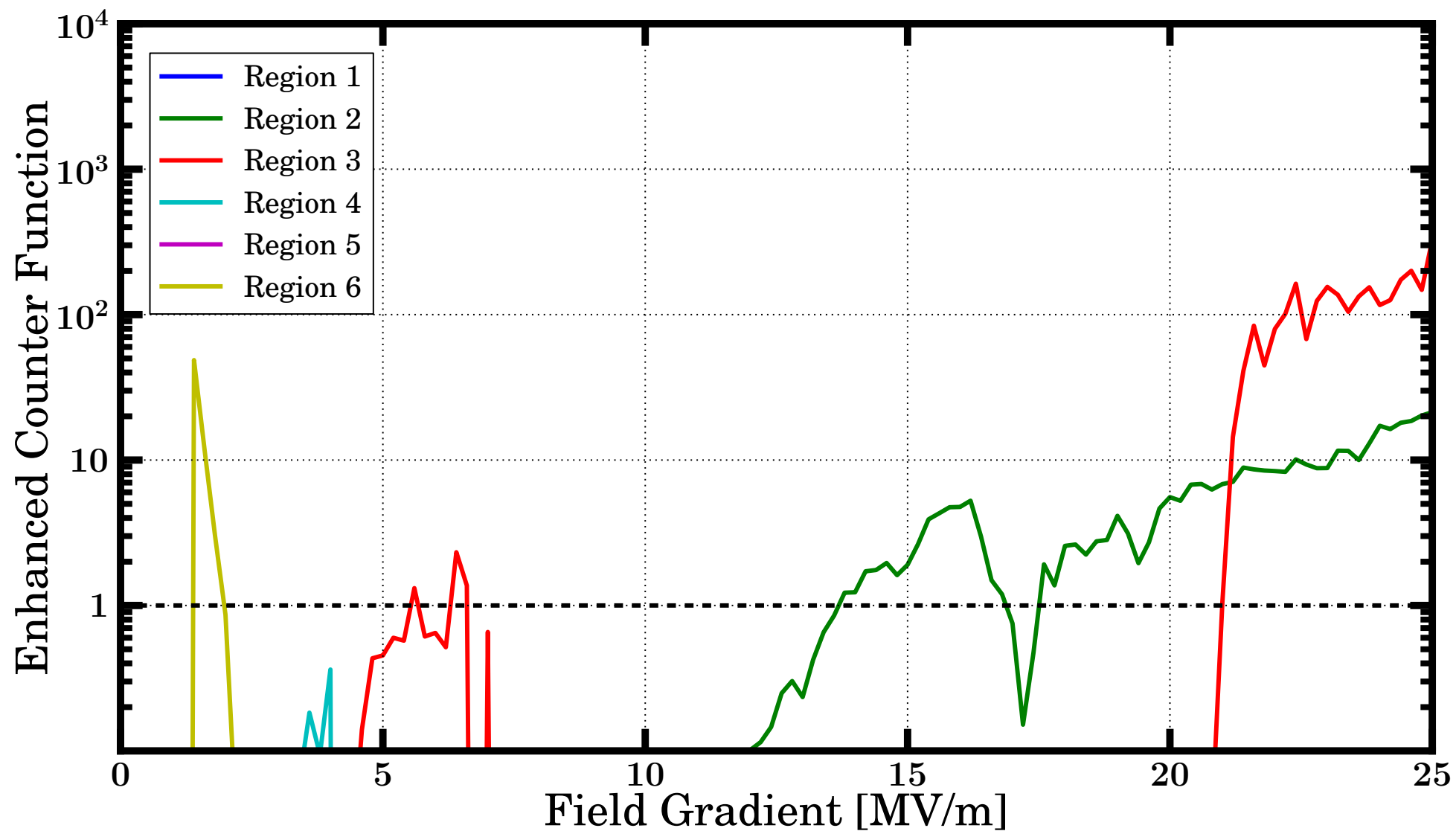


# MP IN TESLA STYLE

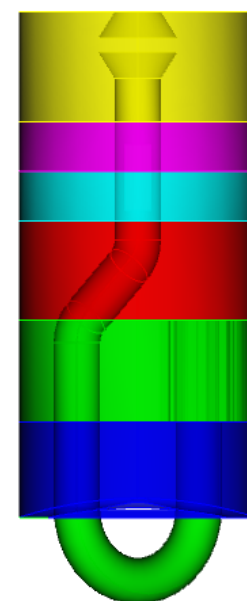
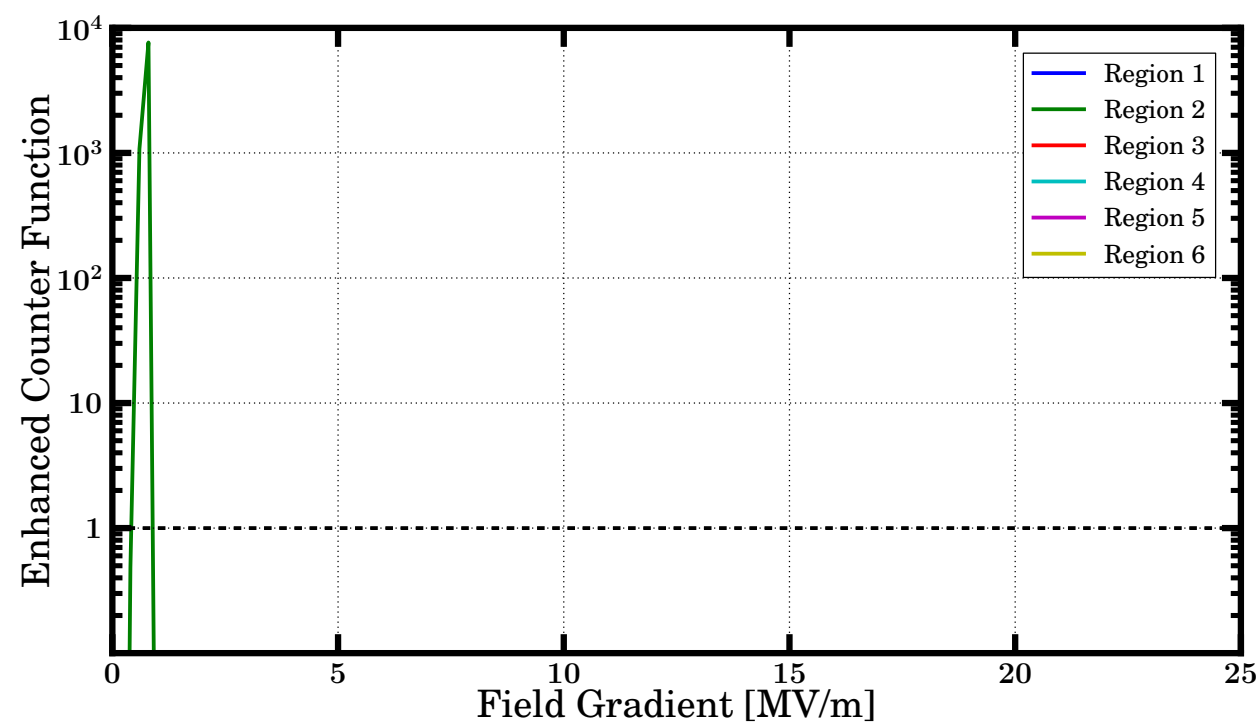
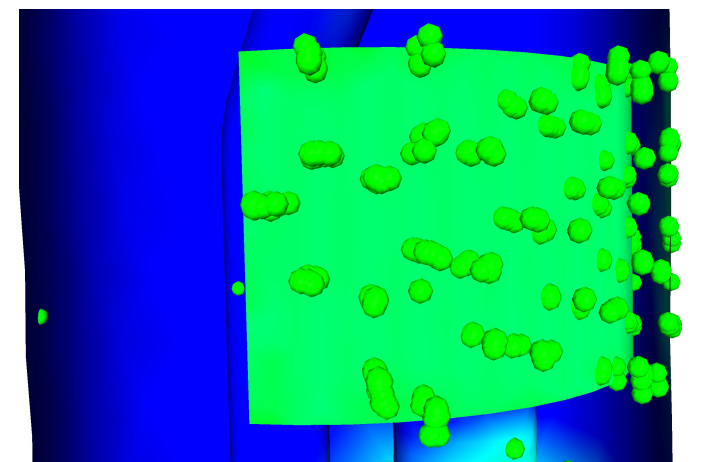
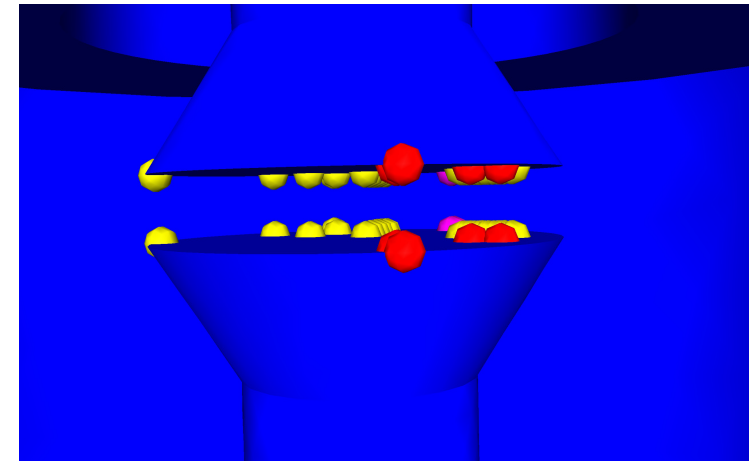
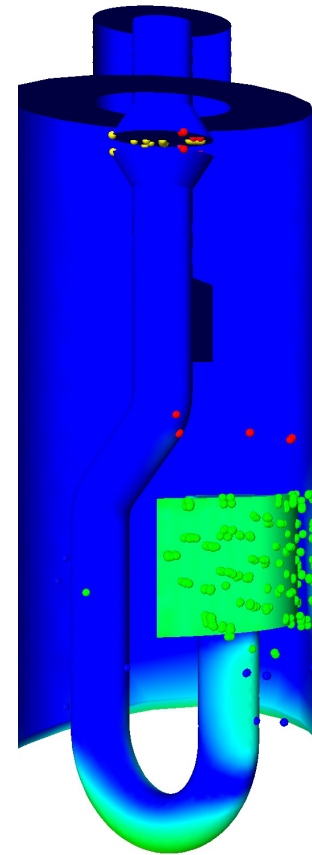
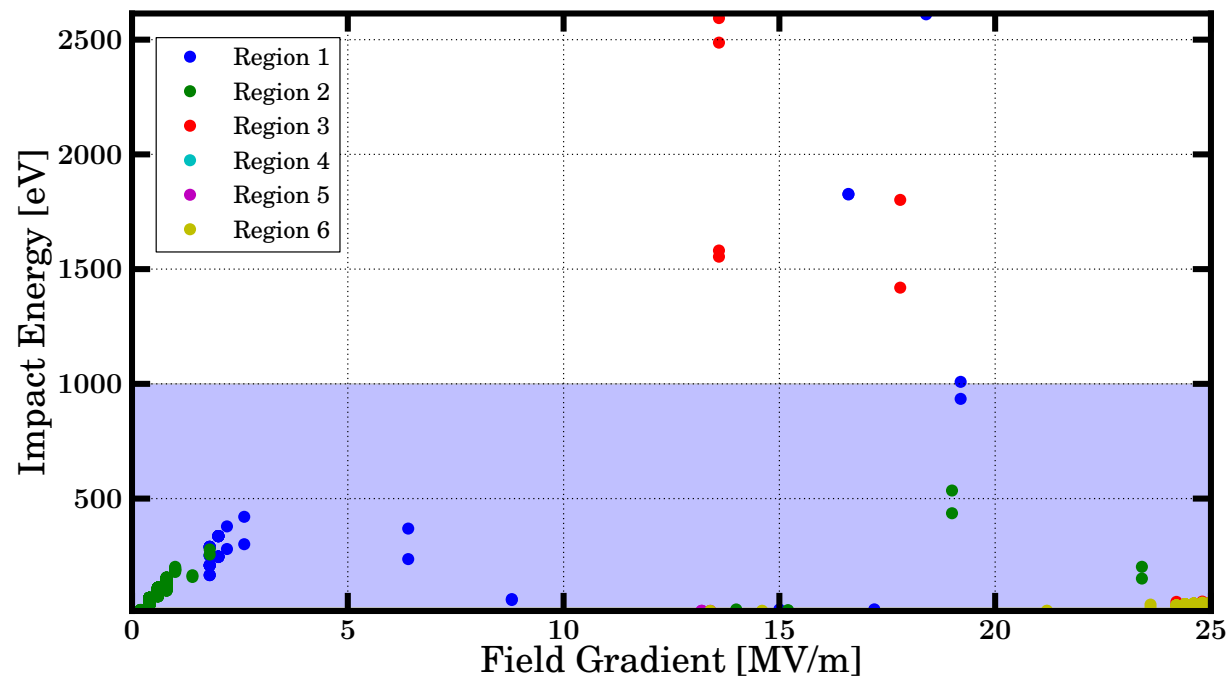




# MP IN TESLA STYLE

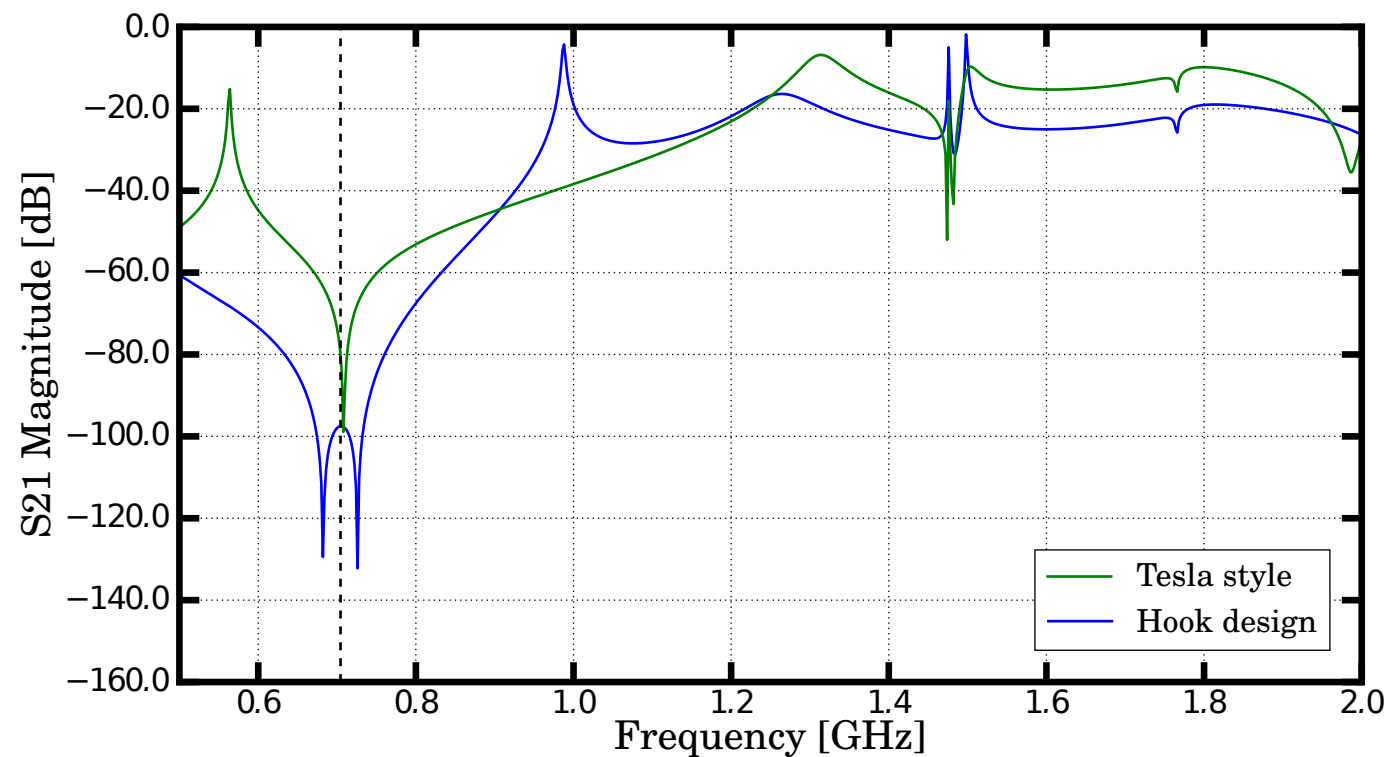
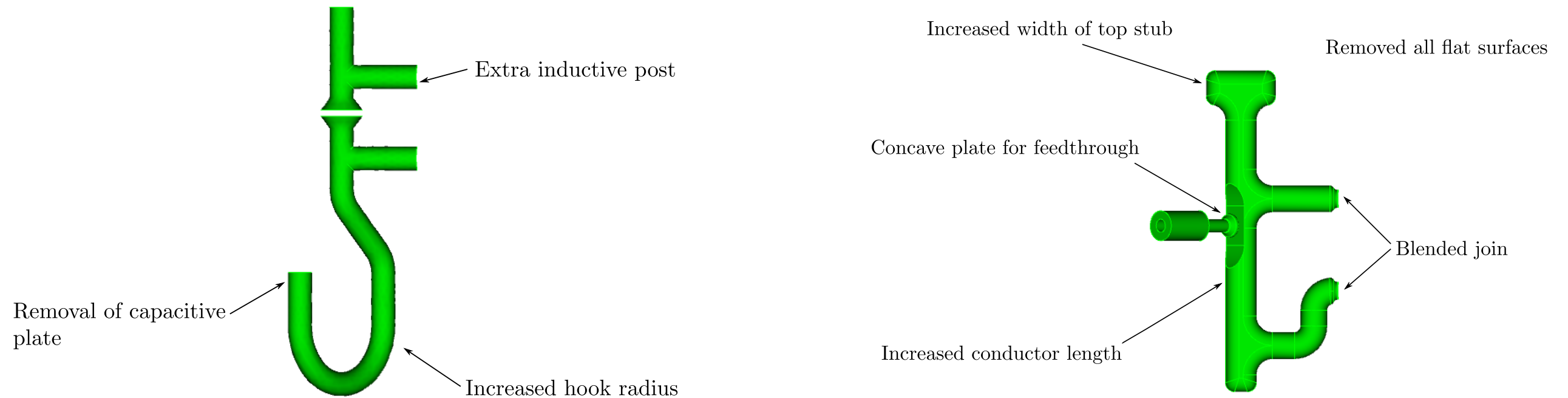


# MP IN ROSTOCK DESIGN



Region 6  
Region 5  
Region 4  
Region 3  
Region 2  
Region 1

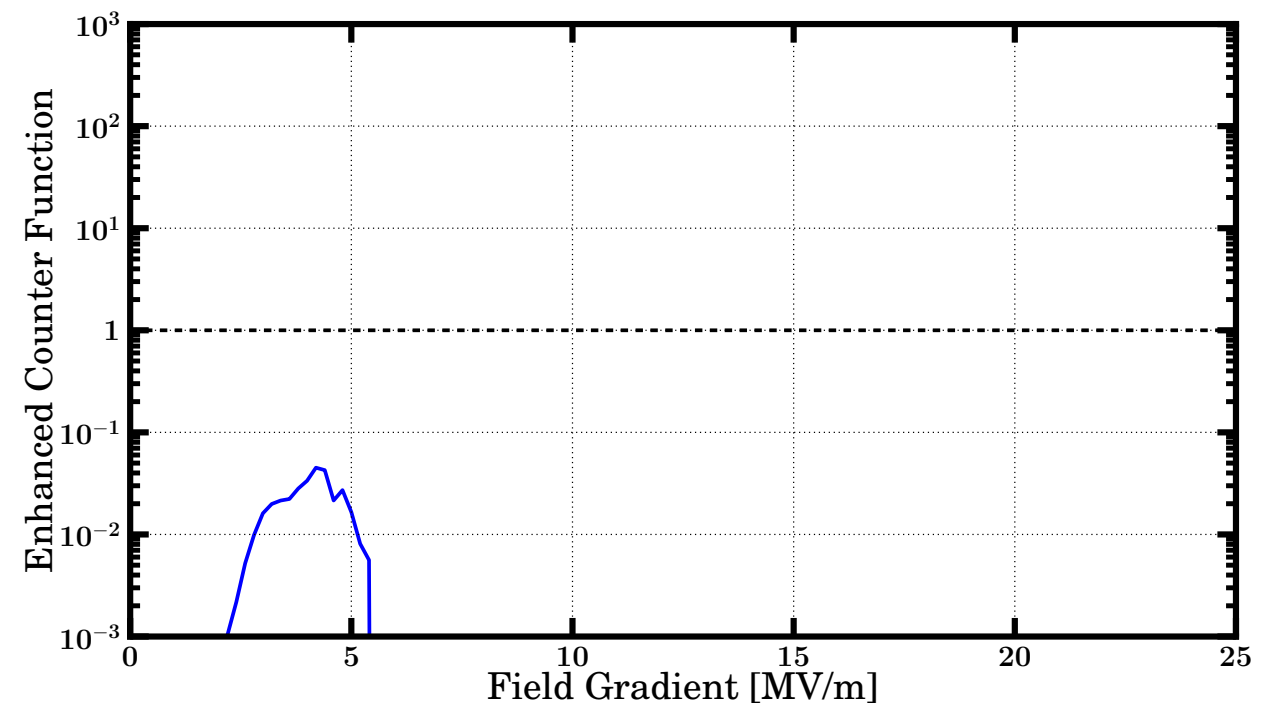
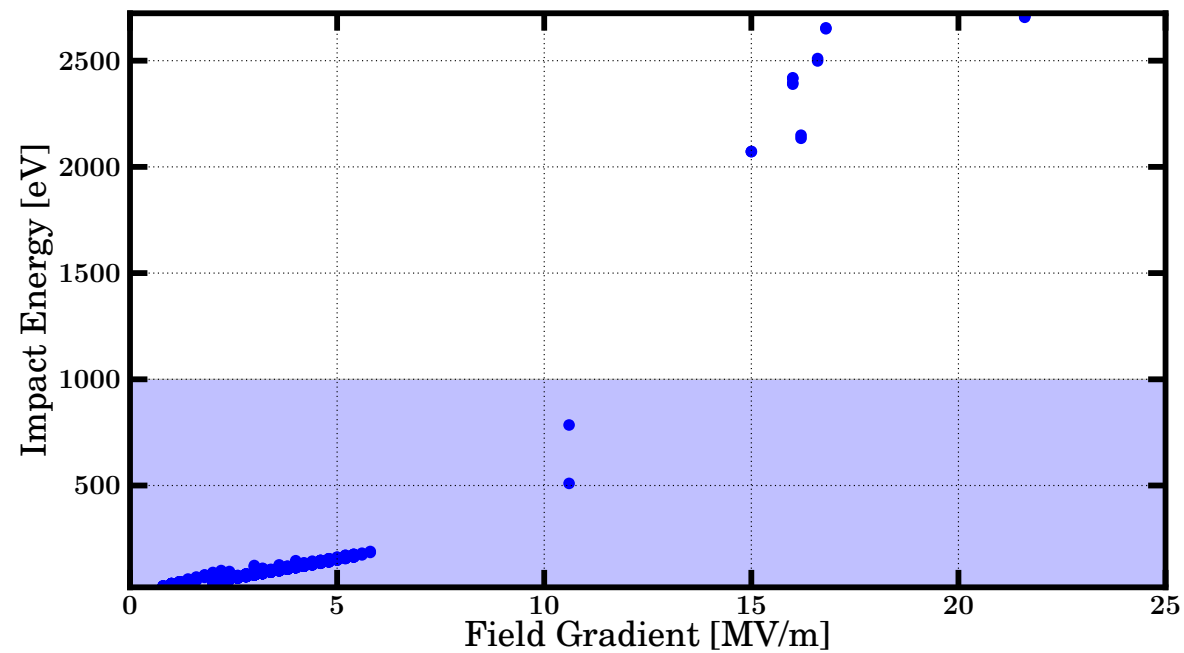
# MODIFICATIONS



# SUMMARY

- SOMs
  - It is possible to design a linac susceptible to SOMs
  - May baseline shows no problems up  $\sim 90$  mA
- HOMs
  - High R/Q modes are not a concern far from ML
  - $|f_{\text{hom}} - f_{\text{ml}}| > 3$  MHz
  - HOM Couplers are not required!
    - ➔ Limits future flexibility (chopping schemes  $> 100$  kHz)
- Modified HOM couplers to reduce multipacting

# MODIFIED HOOK



# TRANSVERSE

