

Characterization of Transverse Beam Motion in Booster

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Fermilab

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Measurement Procedure

- Signals of from damper pickups are digitized with 0.4 ns sampling time for about 1/3 of Booster cycle (6236 turns out of ~20,000) in the middle of accelerating cycle (covers transition crossing)
 - ◆ Hybrid is used to generate sum and difference signals
 - Effective pickup radius (half aperture) - $a=32$ mm
- Data for vertical and horizontal motions were acquired at different cycles

■ Data processing

- ◆ Boundaries for each RF bucket are found
- ◆ Beam positions for each bunch are computed

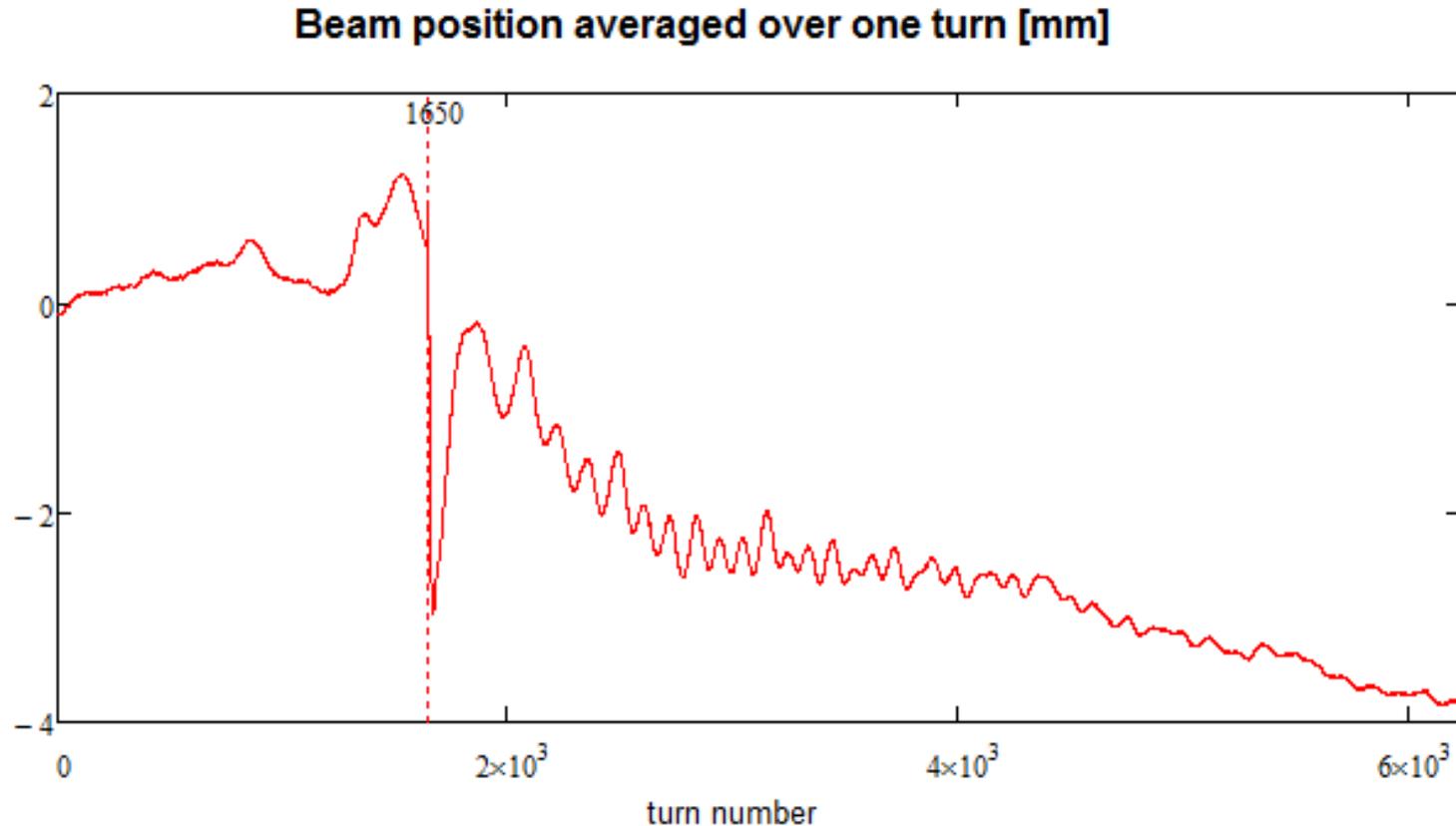
$$x_n = A_n a \quad \text{where } A_n \text{ is computed using RMS fitting } \vec{D}_n = A_n \vec{\Sigma}_n + C_n$$

■ Presentation of data

- ◆ Bunch positions turn-by-turn for each bunch
- ◆ Bunch positions averaged over one turn
- ◆ Spectra of bunch motion
- ◆ Dependences of longitudinal modes of bunch motion on time

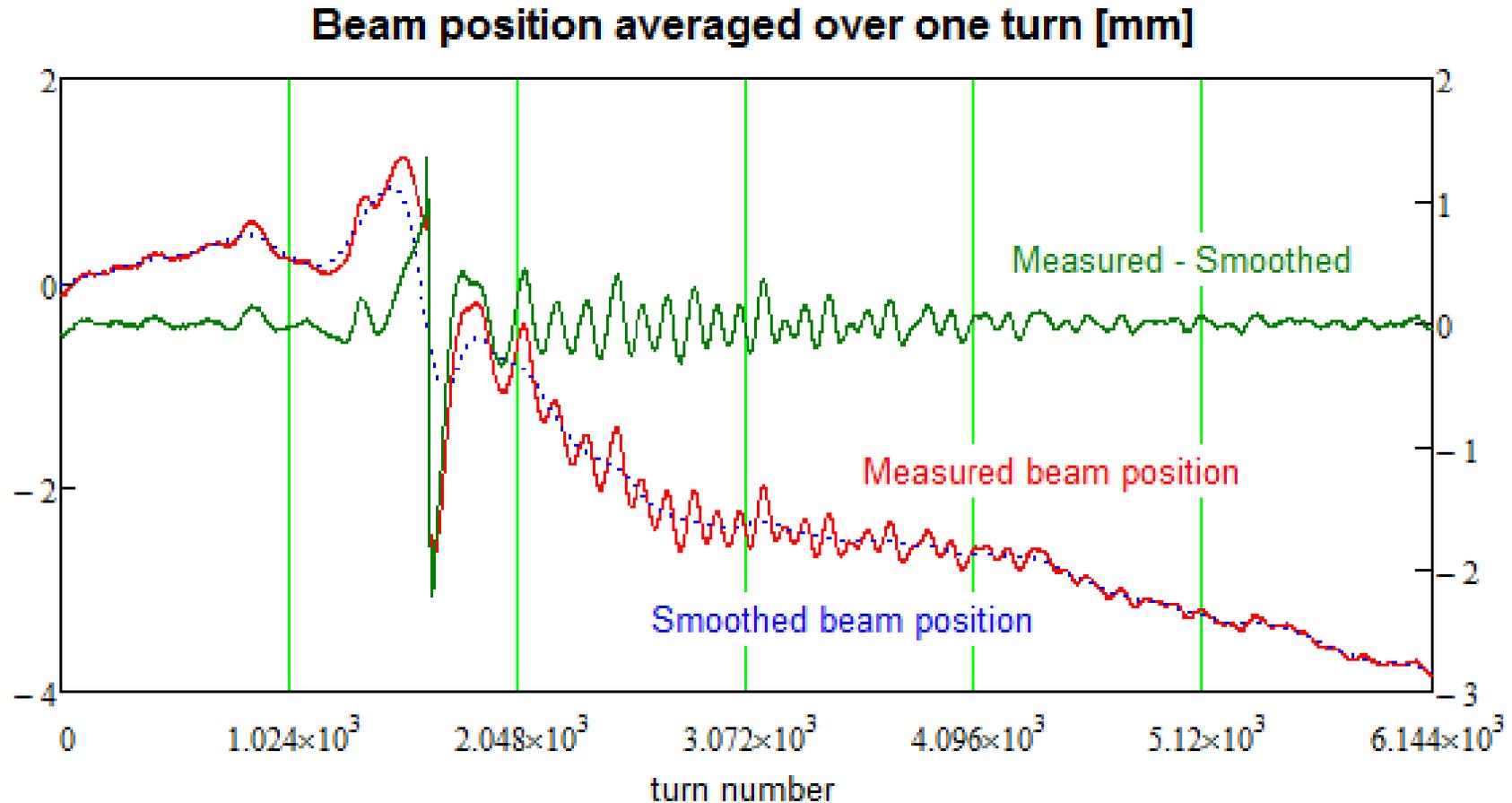
Horizontal Bunch Motion Averaged over One Turn

- Positions of all bunches at a given turn are averaged (except the gap)



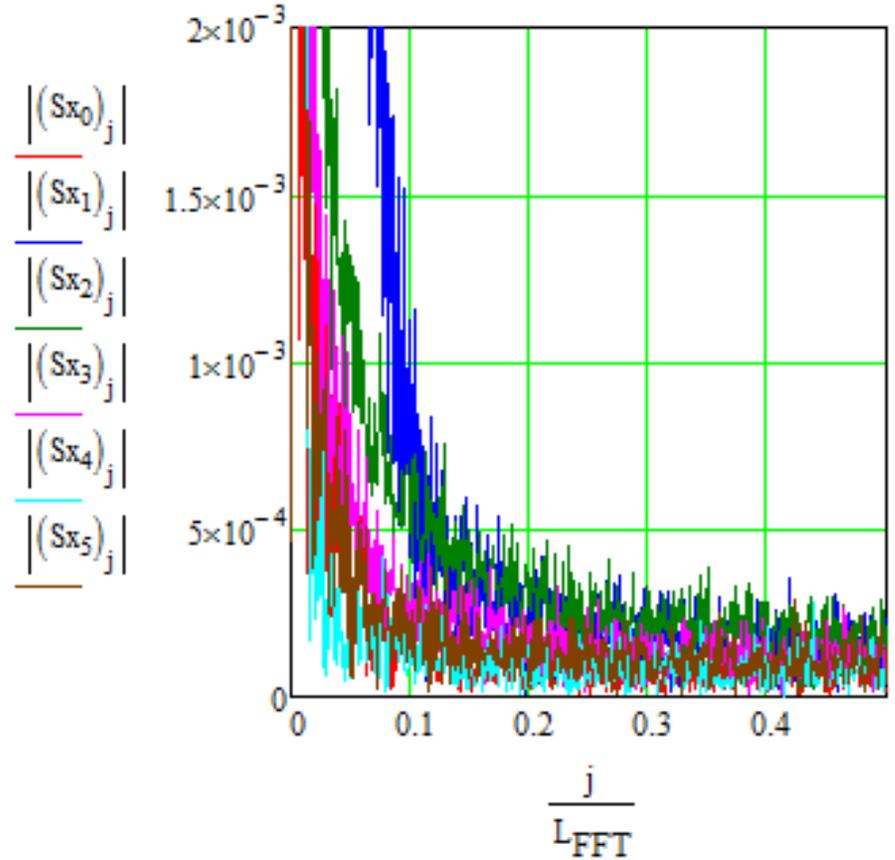
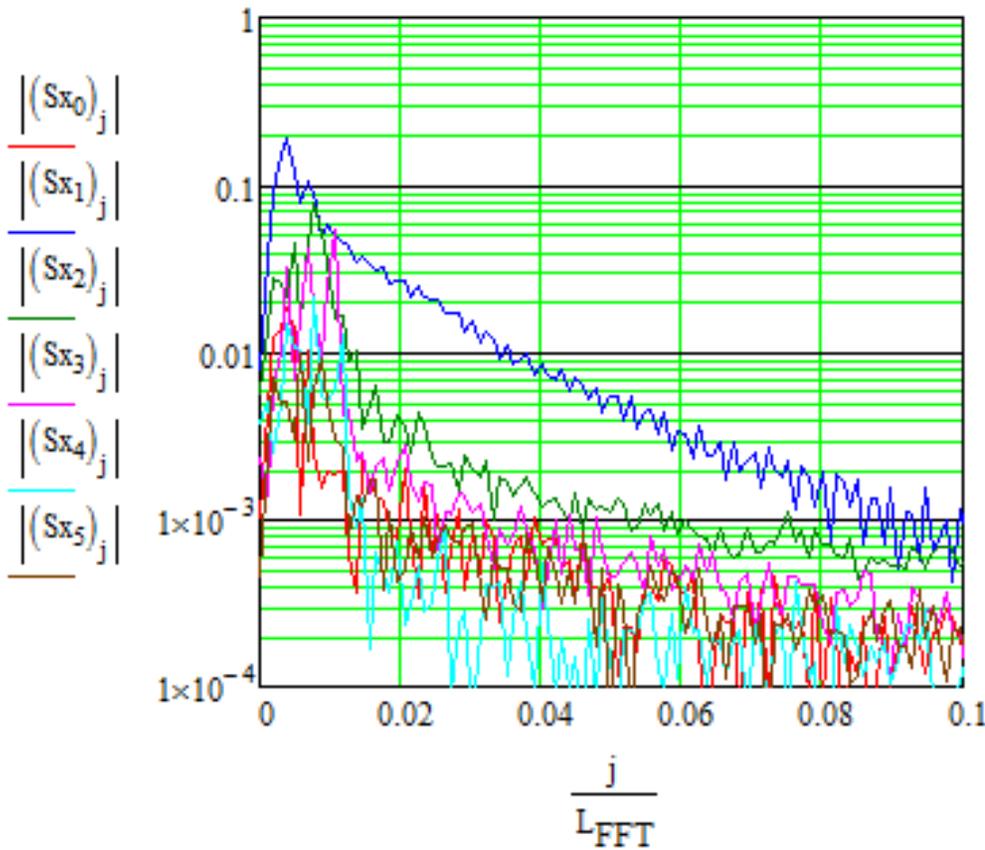
- Transition crossing is clearly seen at turn number of ~ 1650 (counted from the beginning of data acquisition)
- Excellent accuracy of the beam position measurement:
RMS deviation due to noise is about $3 \mu\text{m}$
 - ◆ Digitization noise is the main source of errors (8 bit scope)

Spectrum of Horizontal Beam Motion of All Bunches

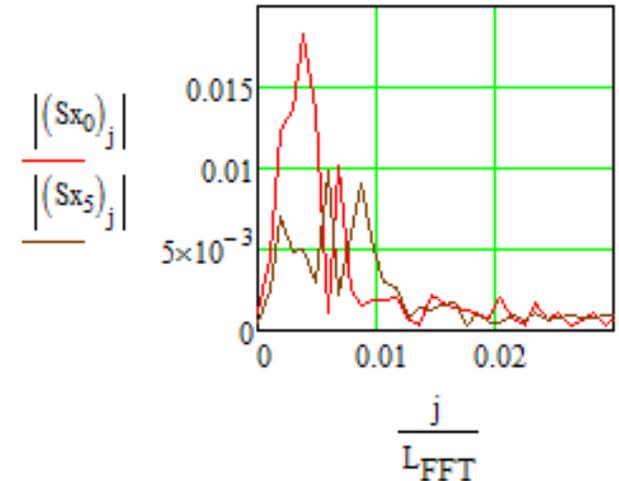


- Two remove low frequency noise the smoothed beam motion was subtracted from its measured value
- All data were split in 6 regions
- FFT was done for each of 6 regions numbered 0 to 5; 1024 turns (points) per region

Spectrum of Horizontal Beam Motion of All Bunches (2)

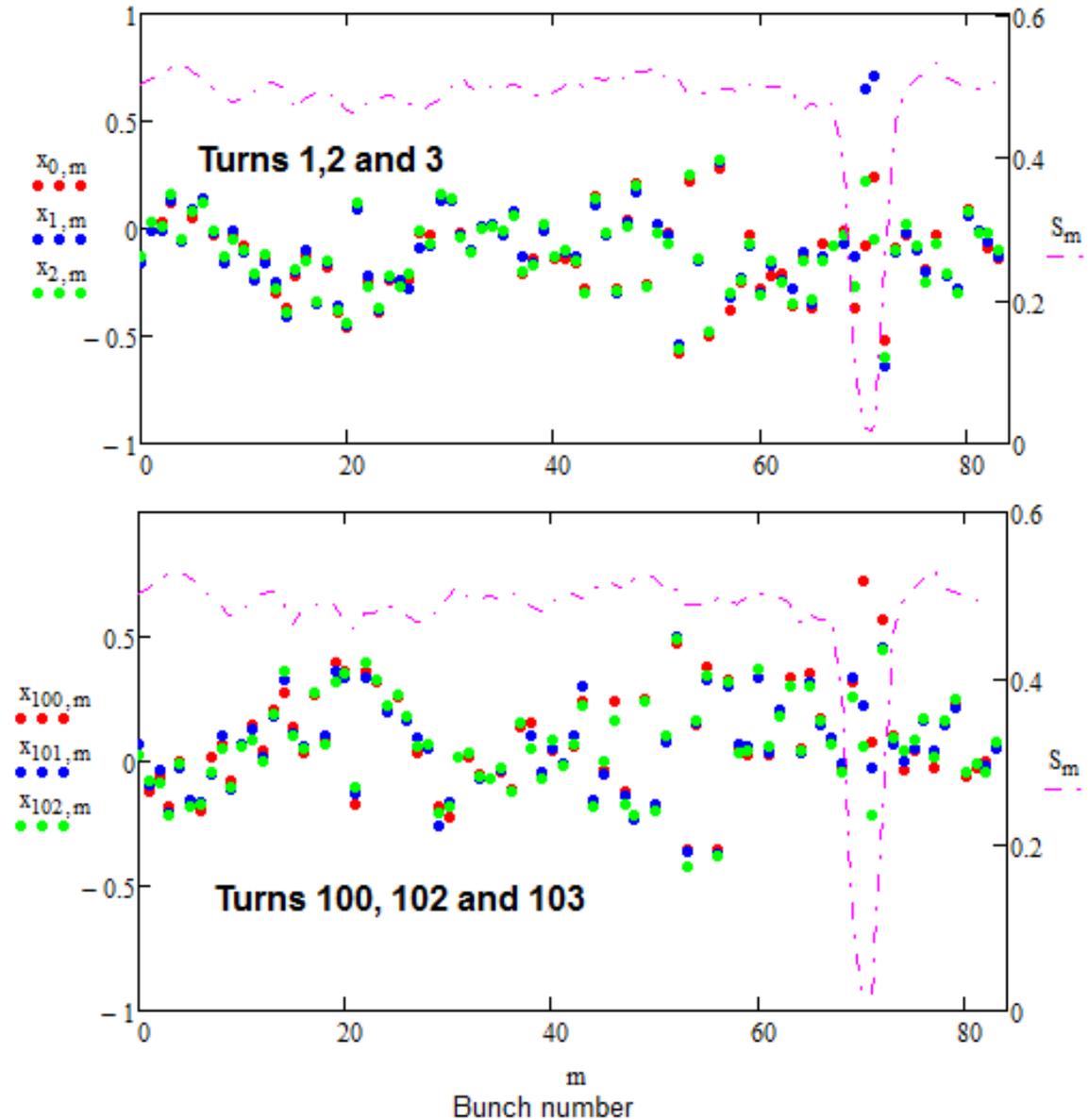


- Region 1 where transition crossing happens has significantly larger spectrum
- There is no measurable motion at the betatron frequencies. Low frequency motion $Q < 0.015$ ($f < 10$ kHz) is present with the rms values $< 50 \mu\text{m}$

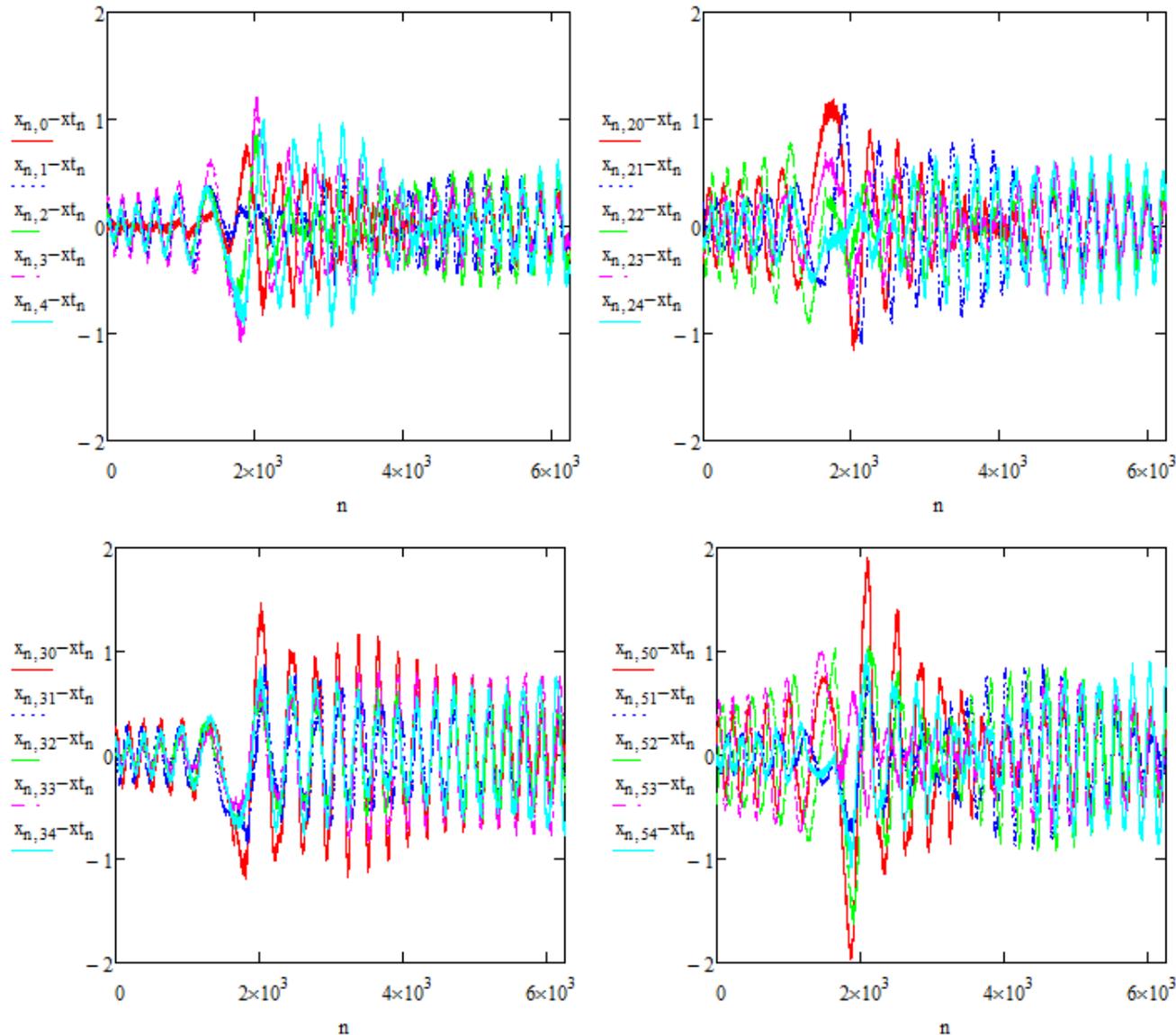


Horizontal Motion of Separate Bunches

- There is considerable bunch displacements relative to the average beam position, about ± 0.5 mm
- Positions at nearby turns are close but changes significantly with time
- Many harmonics of bunch positions are present



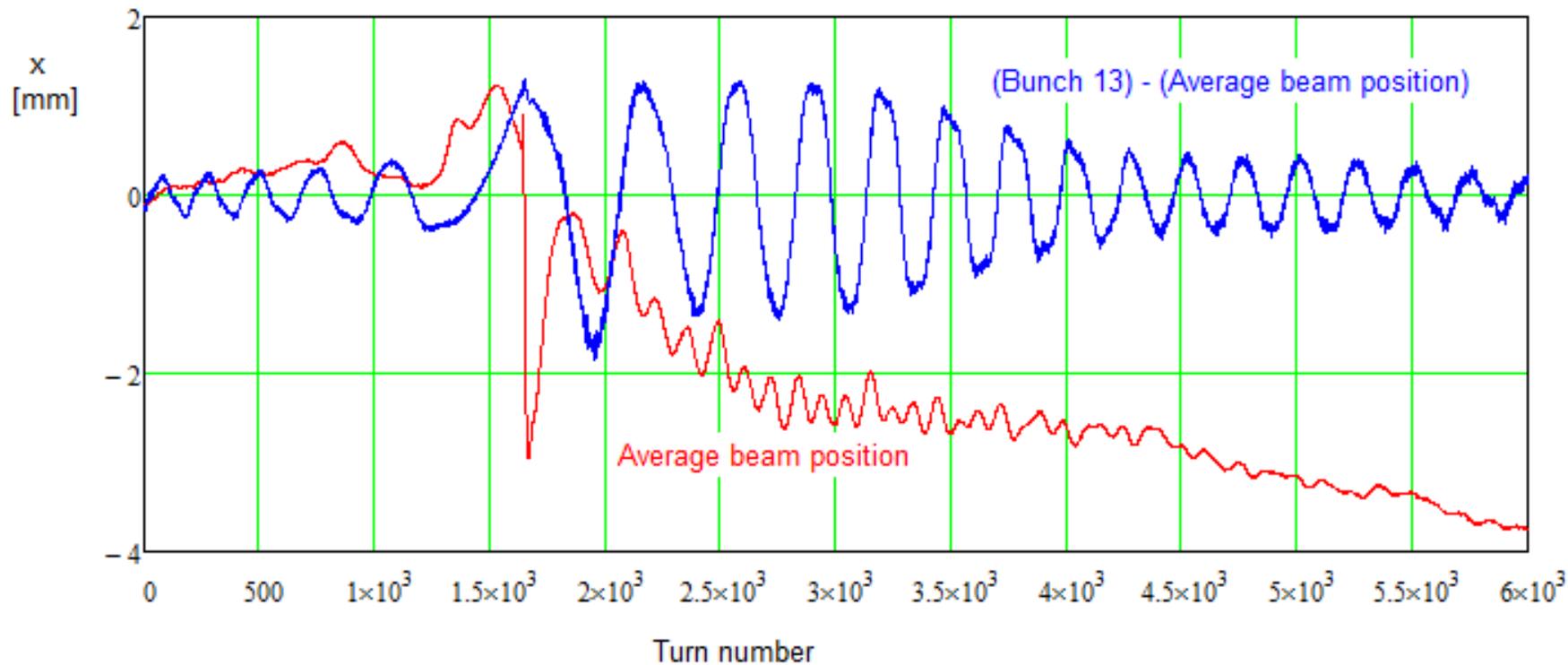
Horizontal Motion of Separate Bunches (2)



Bunch positions on the turn number relative to the average beam position for bunches 0-4, 20-24, 30-34, 50-54

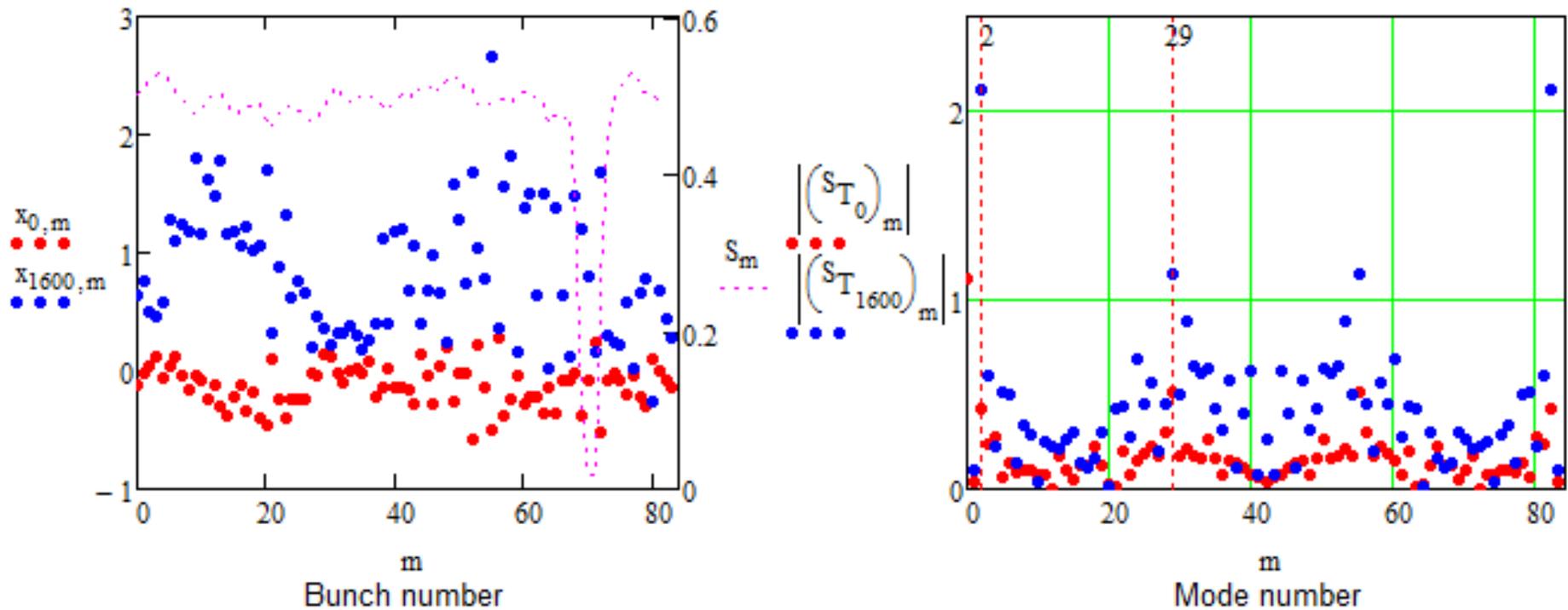
- Positions of bunches are oscillating at synchrotron frequency

Horizontal Motion of Separate Bunches (3)



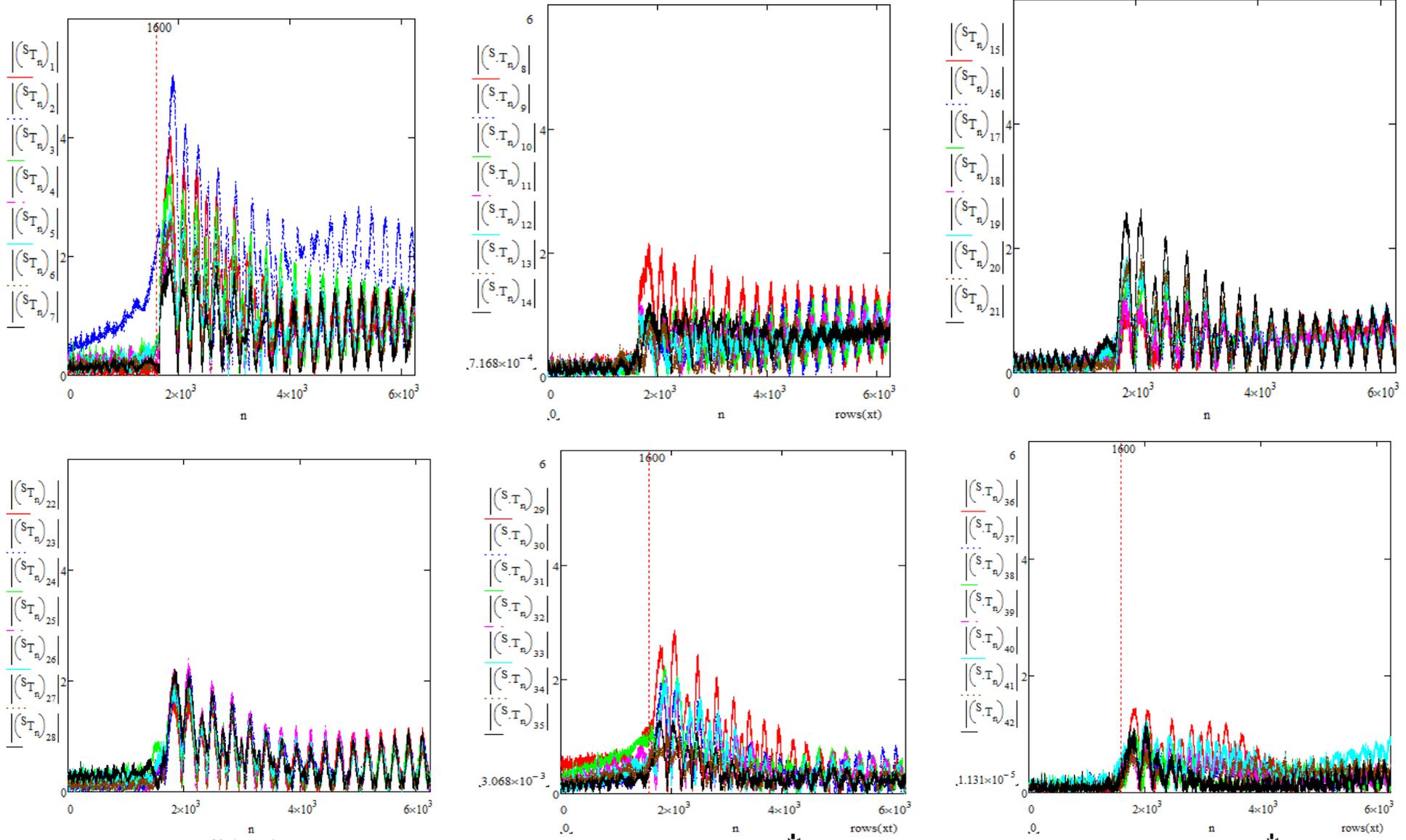
- Bunches are moving at the synchrotron frequency relative to the average beam position
- The transition crossing excites motion of the average beam position
 - ◆ The motion is damped (LLRF helps but how much?)
 - ◆ It happens at frequency of longitudinal quadrupole motion
 - Approximately double synchrotron frequency
 - Frequency is shifted up by particle interaction (impedance)
 - Bunch length changes \rightarrow changes in bunch deceleration \rightarrow energy change

Modes of Relative Horizontal Bunch Motion



- Synchrotron motion results in energy variations which we observe as bunch position variations
- There many harmonics in relative bunch motion
 - ◆ Modes 2 and 29 (or 80 and 55) dominate at both the turns 0 and 1600

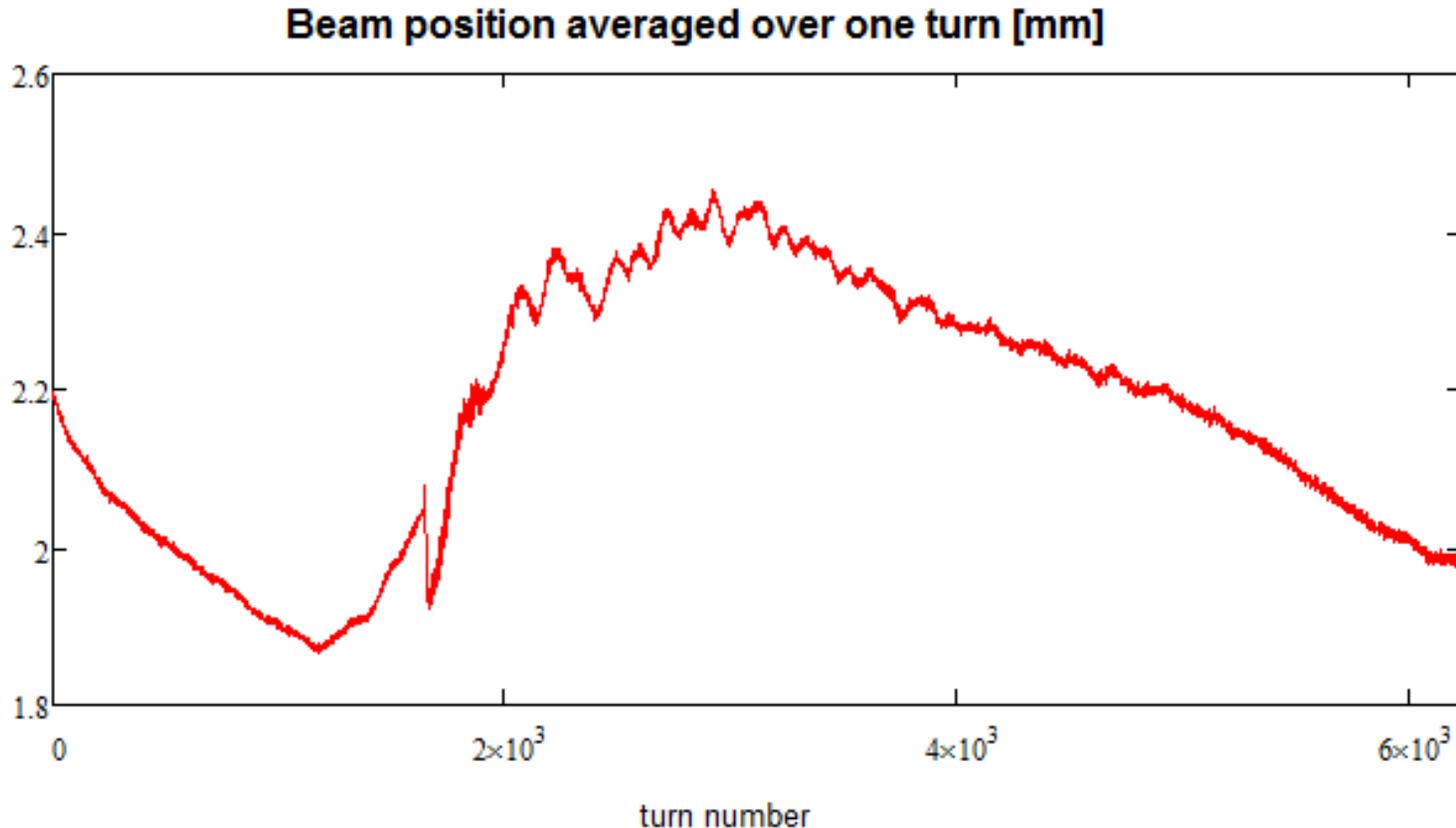
Modes of Relative Horizontal Bunch Motion (2)



- Modes 2 and 29 are most unstable before transition
- Mode 2 looks as a real problem and needs to be damped.

Vertical Bunch Motion Averaged over One Turn

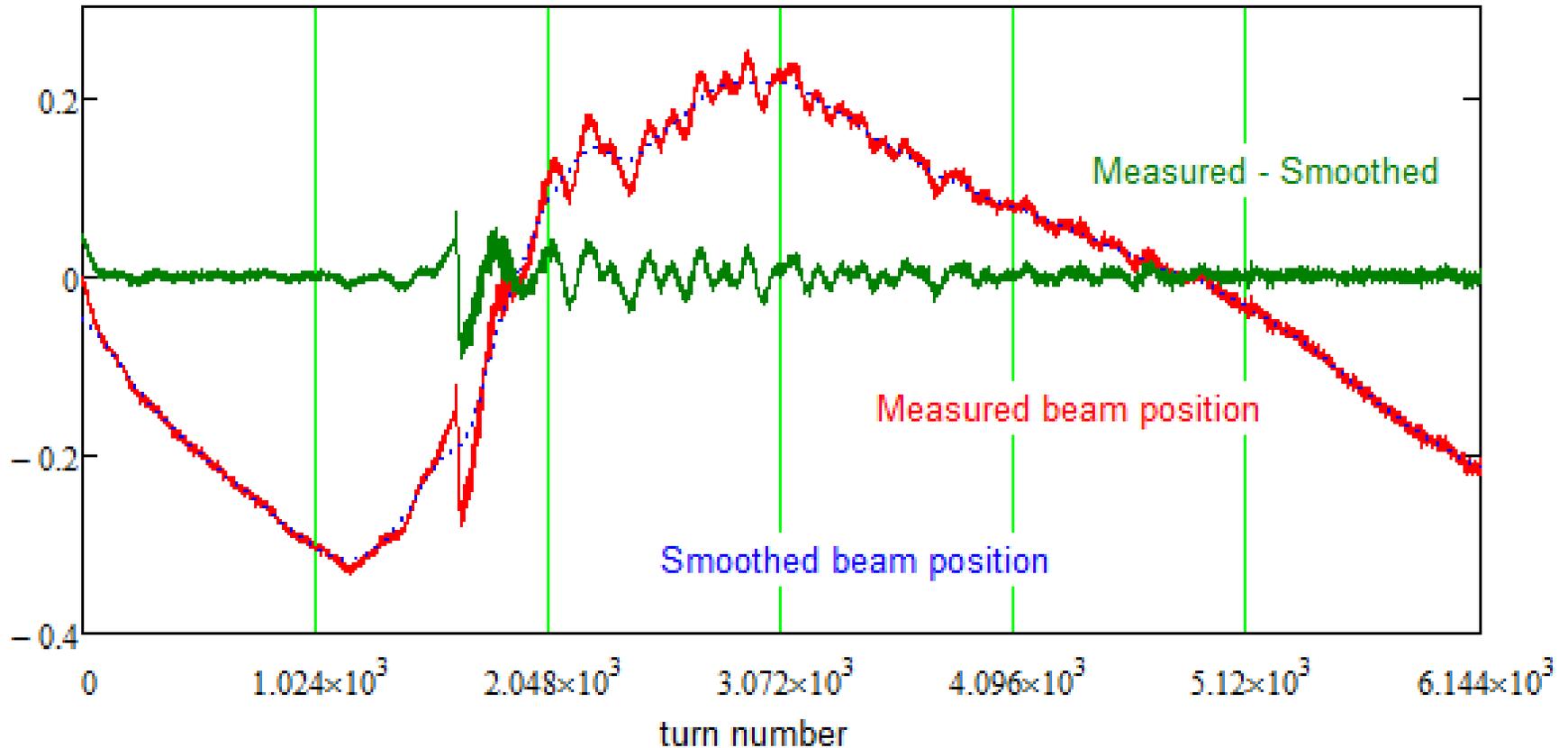
- Positions of all bunches at a given turn are averaged (except the gap)



- Transition crossing is also clearly seen at turn number of ~ 1650 (counted from the beginning of data acquisition)
- Excellent accuracy of the beam position measurement: RMS deviation due to noise is about $3 \mu\text{m}$
 - ◆ Digitization noise is the main source of errors (8 bit scope)

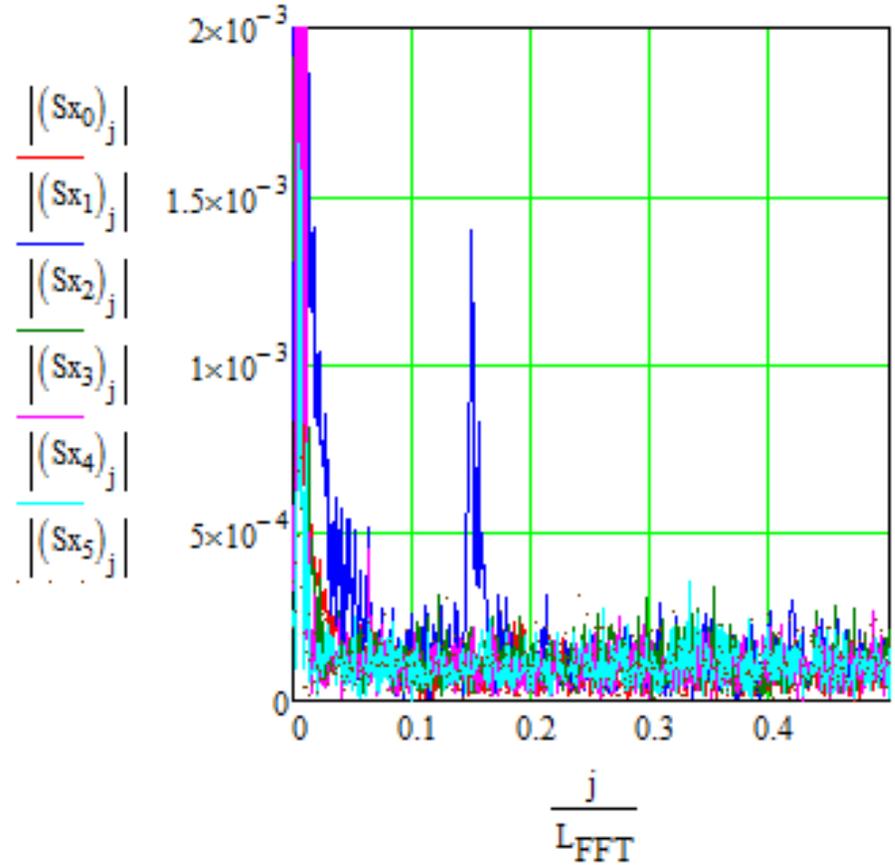
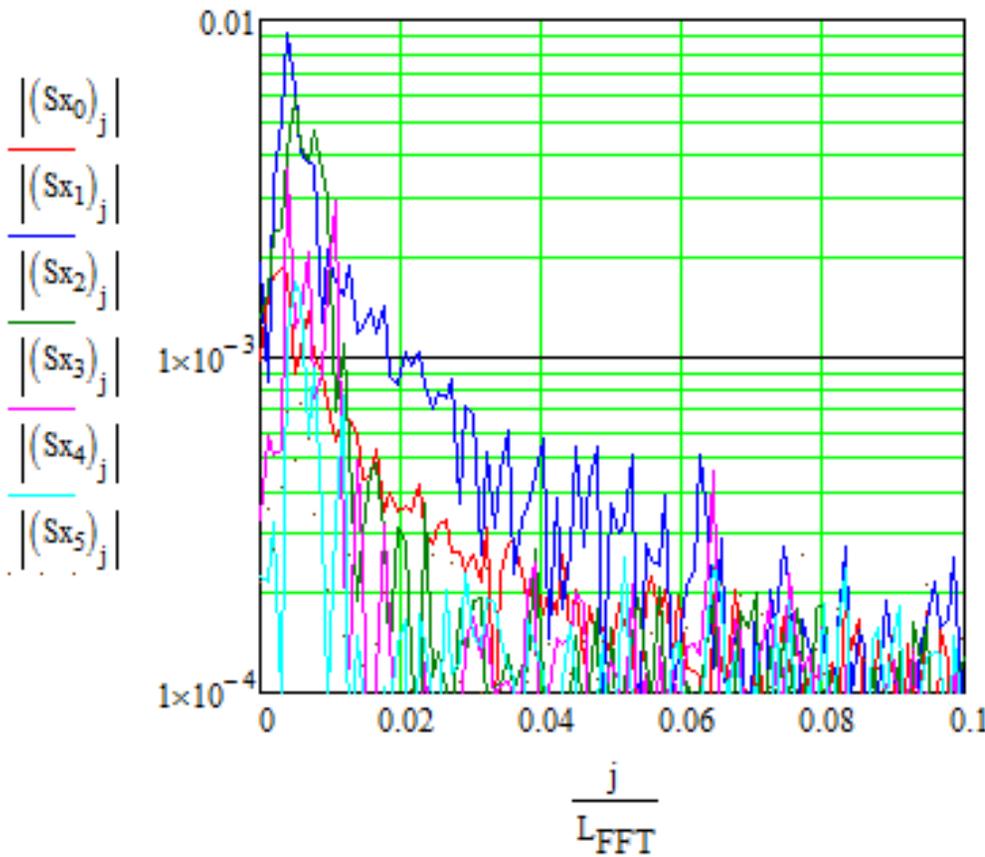
Spectrum of Vertical Beam Motion of All Bunches

Beam position averaged over one turn [mm]

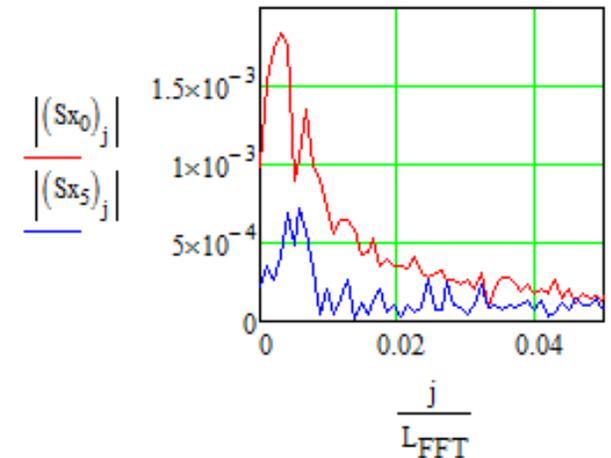


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- FFT was done for each of 6 regions numbered 0 to 5; 1024 turns (points) per region

Spectrum of Vertical Beam Motion of All Bunches (2)

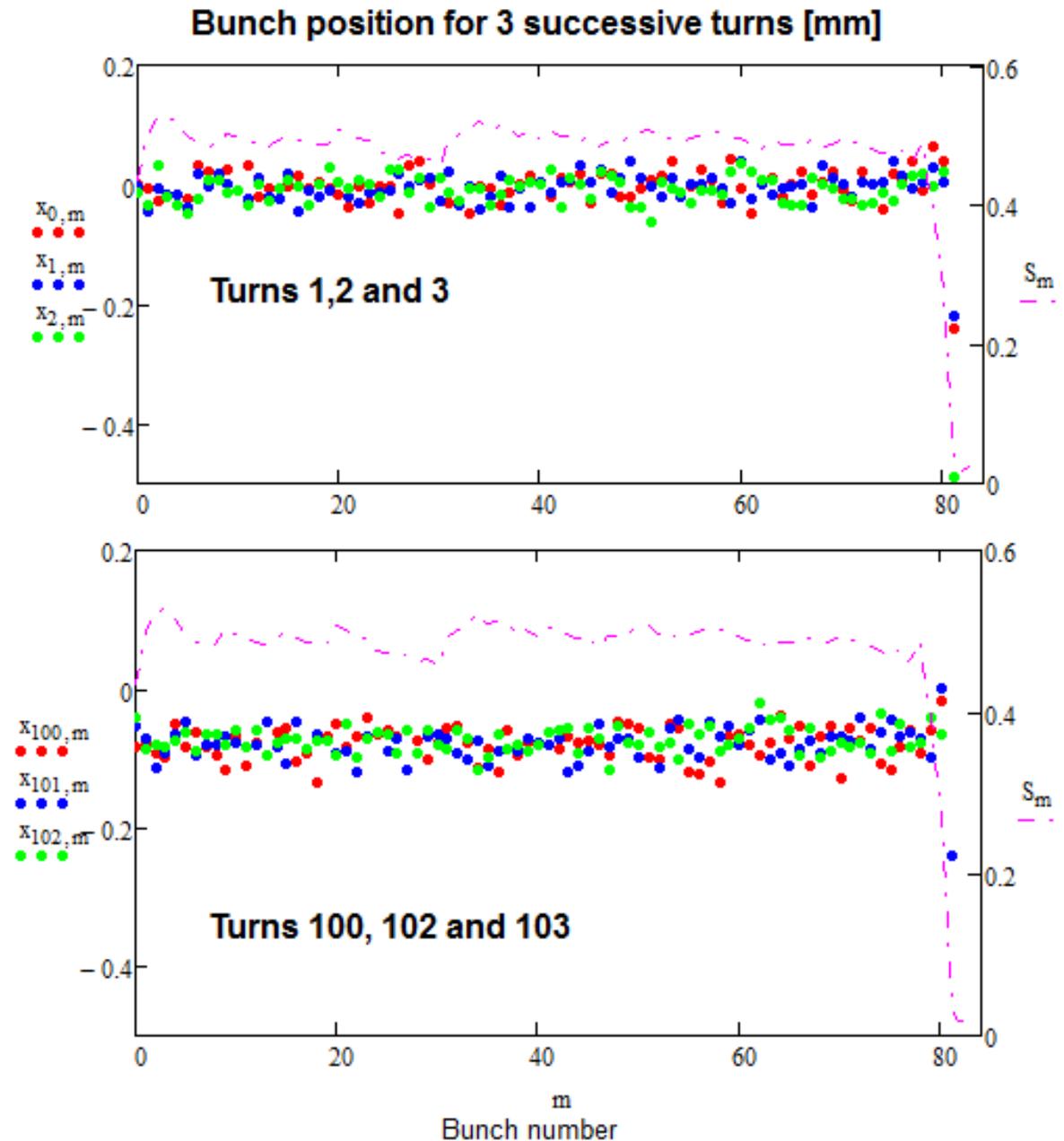


- Region 1 where transition crossing happens has significantly larger spectrum
- Transition excites the betatron motion; the betatron frequency ~ 0.85
- Low frequency motion $Q < 0.015$ ($f < 10$ kHz) is present with the rms values $< 10 \mu\text{m}$

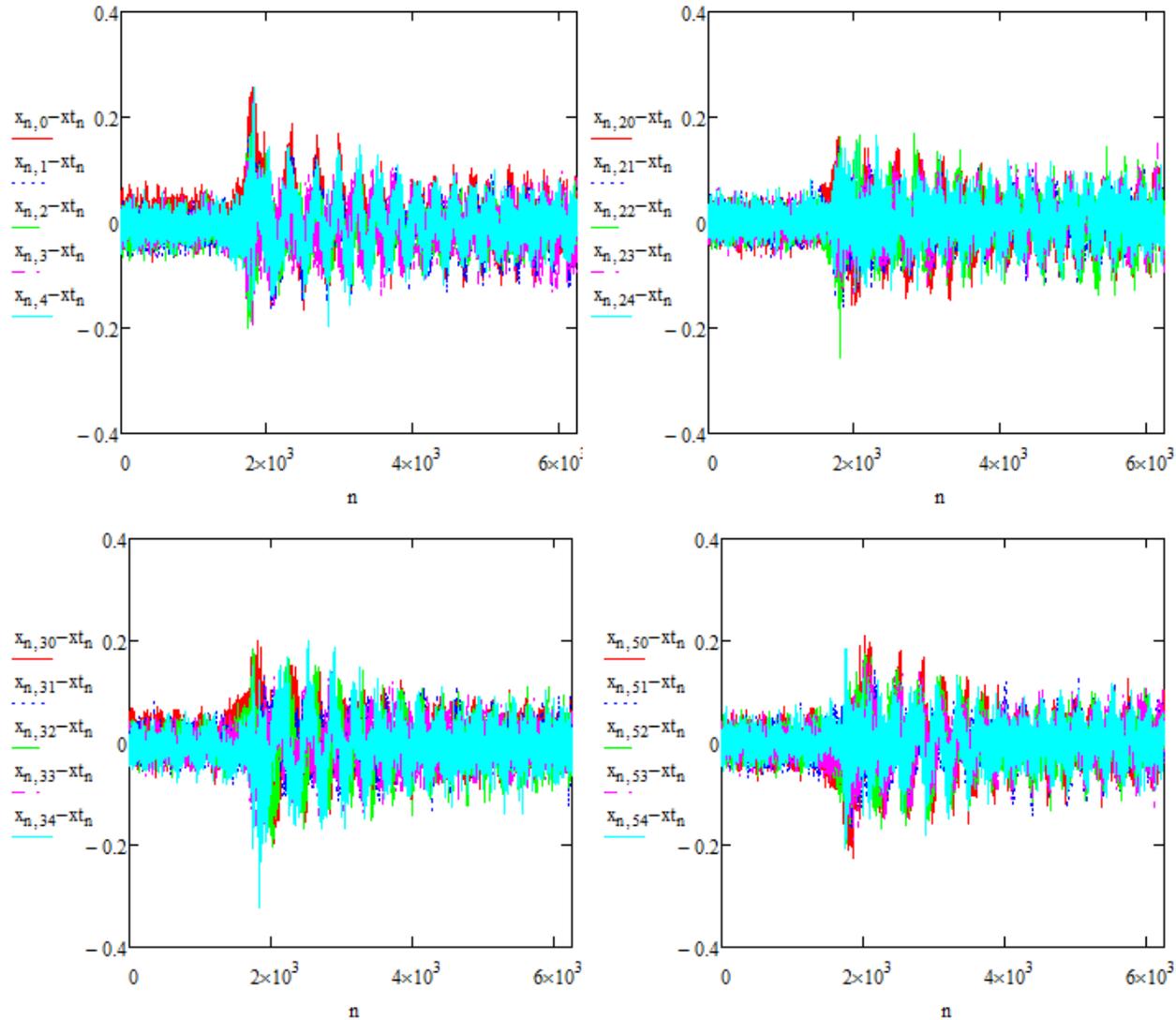


Vertical Motion of Separate Bunches

- In difference to the horizontal plane there is now observable motion of bunches relative to the average position before transition



Vertical Motion of Separate Bunches (2)



Bunch positions on the turn number relative to the average beam position for bunches 0-4, 20-24, 30-34, 50-54

- Transition excites oscillations at the synchrotron frequency with about 5 times smaller amplitude